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Experimental study on the effectiveness of strengthening over-deformed segmental tunnel lining by steel plates

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Abstract: The method of using steel plates to strengthen existing tunnel linings has been widely applied in many tunnel rehabilitation projects around the world. However, the effectiveness of the strengthening resulting from this method is still unclear, especially for conditions when the segmental linings are deformed to a relatively large extent. In this paper, a series of physical model tests conducted in 1-g plane strain conditions were designed to study the strengthening effectiveness of steel plates for over-deformed segmental tunnel linings. The results show that the segmental tunnel linings affected by the ground surface surcharge will deform nonlinearly, as the complex behaviour of the segment joints at different positions lead to a gradual degradation of the tunnel overall performance. Once the deformed segmental tunnel linings were strengthened by steel plates, the stiffness and capacity of the tunnel were improved by 190% and 69%, respectively, compared to those without strengthening. Subsequently, the strengthening effectiveness of tunnels strengthened at different deformation stages are compared quantitatively. It is found that an increase in the tunnel deformation before strengthening led to a decrease in the stiffness and an increase in the total capacity of the tunnel after strengthening, while the increased capacity was

less affected.

Keywords: Segmental tunnel lining, Steel plate strengthening, Model test

1. Introduction

Shield-driven tunnels play an important role in the development of urban underground infrastructure systems. Once constructed, these tunnels are usually expected to last for a hundred years. However, due to unpredictable changes in the surrounding environment and the constructed characteristics of segmental linings themselves, the tunnels can face high risks of being disturbed or even damaged by potential accidents throughout their lives. Accidents related to operating tunnels being adversely affected by external disturbances are often reported from time to time, for example from adjacent excavations (Chang et al., 2001a), from piling constructions (RAIB, 2014), from ground surface surcharge (Huang et al., 2016), and from flooding (Van Empel et al., 2006). The affected segmental linings were severely damaged in these accidents, which threatened the safety of the tunnel systems. Therefore, effective rehabilitation measures for damaged tunnels after such events are important to guarantee their continued safety during the future service.

There are several ways to strengthen damaged tunnel linings, amongst which the steel plates strengthening method has been widely adopted due to its various advantages (Chang et al., 2001b, Kiriya et al., 2005, Shao et al., 2016). The main phases of this method can be summarized as: First, the steel plates sections are manufactured according to the inner profile of the tunnel that needs to be strengthened; Second, the steel plate sections are installed and welded to form an inner steel ring connected to the existing tunnel linings; Third, the gap between the new steel plate linings and the original concrete segmental linings is filled with mortar or epoxy resin to ensure that

the two components behave as a composite lining system. In this way, the increasing lining deformation is controlled and the capacity of tunnel structure can be enhanced.

Although this strengthening method has been widely applied to repair tunnels in soft soils, there is always a question on when is the optimal time to conduct the strengthening treatment of a deformed tunnel. It is obvious that the time determines not only the safety of tunnel lining structure, but also the cost of the whole tunnel repair project. Therefore, it is essential to understand the influence of existing degree of damage on the post-strengthening tunnel performance, as only then will the most appropriate time for strengthening be determined.

There has been some research focusing on tunnel strengthening using steel plate linings. Liu et al. (2017) performed a full-scaled structural test on a segmental lining ring strengthened by steel plates. In this experiment, a real RC (reinforced concrete) segmental ring was strengthened by additional bonded steel plate linings, and 24 hydraulic jacks were utilized to apply a system of point loads to simulate the soil pressure. The steel plates were installed inside the deformed segmental lining ring with the load being applied, and then the strengthened tunnel was loaded continuously until failure occurred. The test result demonstrated the effectiveness and failure mode of this strengthening method, and some parametric analyses were conducted by Zhao et al. (2016) using a new simplified numerical approach. However, using jacking loads neglects the important soil-structure interaction, and the high demand in terms of cost, space and equipment of such a full-scale experimental approach make it hard to repeat and conducted for other arrangements. Zhang et al. (2019a) presented a numerical study of steel plate strengthened segmental tunnel linings using FE (finite element) tools, where the soil-structure interaction and the tunnel-steel interface were appropriately simulated. However, the influence of the structural damage before strengthening, and

66 the phenomenon of strengthening failure was difficult to simulate due to limitations with the
67 numerical techniques.

68 Therefore, further studies are required to better understand this tunnel strengthening method. In
69 the field of geotechnical engineering, physical model tests have always been a useful and
70 fundamental way to study sophisticated geo-structure problems (Wood, 2014). Compared with full-
71 scaled testing, small-scaled model tests have advantageous for following reasons: (1) they can be
72 performed with better control on the model details, (2) they allow the information about the expected
73 patterns of response to be obtained more rapidly, (3) they can be performed repeatedly at relative
74 low cost. Generally, laboratory tests for buried tunnels can be performed either under natural (single)
75 gravity conditions (1-g) (Kojima and Yashiro, 2005, Chapman et al., 2006, Zhang et al., 2015) or in
76 a centrifuge, which applies multiple gravities to be applied in a test (Mair et al., 1993, Meguid et al.,
77 2008, Kiani et al., 2016). In this research, a 1-g model test was designed and performed to study
78 the steel plates strengthening method for segmental tunnel linings, so that: (1) the operation of the
79 steel plates strengthening can be performed manually during test, which could not be easily
80 achieved in a centrifuge environment; (2) the tunnel models required relatively larger scale ratio in
81 this research to reveal detailed patterns of segmental tunnel lining behaviours with and without
82 steel plates strengthening, which would have been difficult to conduct in an ordinary centrifuge.

83 In this paper, a scaled physical model tests for segmental tunnel linings strengthened by steel
84 plates performed in 1-g plane strain conditions are described. The techniques for modelling of soil,
85 concrete segments, segmental joints and steel plates strengthening are introduced in sequence.

86 The effectiveness of the steel plate strengthening are demonstrated by comparing the results
87 obtained from the tests for tunnels with and without strengthening. Subsequently, the behaviour of

the tunnel strengthened at different deformation stages are summarised and analysed to show the influence of the degree of deformation on the post-strengthening lining performance.

2. Physical model test

2.1. Prototype

As reported by Huang et al. (2016), hundreds of rings of segmental tunnel linings with an outer diameter of 6.2m of Shanghai Metro Line 2 were severely disrupted due to an unexpected surface surcharge, where a maximum transverse lining deformation in term of horizontal convergence ratio reached 35.7‰. During the tunnel repair process, steel plate linings were adopted to strengthen the damaged tunnel sections. This tunnel and related ground conditions have been used as the prototype in this research. Detailed information on this tunnel strengthening project can be found from previous literature (Zhao et al., 2016, Zhang et al., 2019b).

The scaling law (Wood, 2014) has been applied to set up the relationship between the prototype and the model. The scale factor for length n_l was first determined as 1:15, based on the soil tank dimensions. In the 1-g experiment condition, since sand is utilized to model ground soil, the scale factor for its unit weight n_γ is determined as 1:1. Therefore, the scale factors for other quantities were determined by using dimensional analysis as shown in Table 1. It should be noted that the listed scale ratios are the ideal values which were difficult to achieve perfectly. Therefore, some compromises had to be adopted when making decisions related to the tunnel and soil model materials, which will be explained in the following paragraphs.

2.2. Experimental apparatus

A soil tank with a size of 2m high, 2m wide and 0.4m thick was used for the experiments. As shown in Fig. 1 and Fig. 2, the soil tank has rigid side walls with a smooth inner surface made from ceramic. There are two square-shaped openings with a size of 0.8m×0.8m at the middle of the walls covered by 40 mm thick transparent Perspex plates. On one side, there is a circular opening with a radius of 175mm in the Perspex plate, allow access for the strengthening operation and installation of the sensors and wires. On the other side, a camera was placed focusing on the tunnel to capture the deformation profiles of the deforming tunnel. A jack with a rigid plate footing was placed on the top soil surface to provide surcharge load on the ground surface during the experiment. The tunnel lining deformation was measured by four 40mm-LVDT (linear variable differential transfer) devices placed at positions of the tunnel crown, invert and spring-line. Circumferential strains on both the inner and outer surfaces of the lining segments were measured by RSG (resistance strain gauge) every 45° around the tunnel section.

2.3. Modelling of the soils

A true model can be obtained only when governing laws for all qualities are satisfied. However, for 1-g model tests associated with geotechnical problems, it is necessary to make things achievable with an adequate model, which maintains a “first order” similarity (Harris and Sabnis, 1999). Since large transverse tunnel deformations were measured in actual case mentioned before, observable lining deformation was required in the 1-g model tests, which closely related to the compressibility of the model soil. Therefore, a mass of rubber particles with good compression characteristics was used to model the soil layer near the tunnel, while dry medium sand was used for the rest of the

ground soil to provide gravity stresses (as shown in Fig. 2). The soil material is placed and tamped in layers 20cm thick so that the tank was filled to as similar degree of homogeneity and density as possible for all the tests.

The model soil materials are shown in Fig. 3. Their physical properties and grain characteristics were tested and the corresponding parameters are listed in Table 2. In addition, compressibility tests and direct shear tests were conducted on both materials to capture their mechanical properties, and the results are shown in Fig. 4. The compression modulus of rubber particles is determined as 0.51MPa, considering the scale ratio in Table 1, and the corresponding compression modulus of prototype soil was 7.65MPa. The prototype soil layers in which the real tunnels were constructed are layers ③-⑤ Shanghai silty clay, and this material has the compression modulus varying between 1.32~11.5 MPa (Huang et al., 2016). Therefore, the rubber particles are appropriated for use as the model soil in this experiment.

2.4. Modelling of the segmental tunnel linings

One of the main challenges for the model test in this research was how to model the segmental tunnel linings properly. It is acknowledged that the existence of joints is definitely the most vital structural characteristic for segmental linings of shield-driven tunnels (Do et al., 2013). To date, there are two main modelling strategies for segmental tunnel linings. One approach is using model segments made of solid materials (e.g. metal, Perspex), which are easy to be cut into segments from a tube so that they can then be assembled as rings (Lee and Ge, 2001, Ye et al., 2014, Standing and Lau, 2017, Zheng et al., 2017). Using this approach, the joint behaviour can be modeled appropriately, but the influence of fragility property and cracks are ignored. The second

approach is to cast a whole tunnel lining using a mortar material (e.g. cement mortar, gypsum mortar) using a specific mould (Zhang et al., 2015, Wang et al., 2019b). In this way, the segmental joints are usually modelled by grooves at appropriate positions. The advantage of this approach is that the mortar casting materials are similar to concrete, which can simulate the lining cracking and crushing behaviour while being stressed. However, since the discontinuous rotations between adjacent segments at the joints are the main cause of the large transverse deformation of segmental tunnel linings in soft soils (Huang et al., 2016), the continuous lining rings with simply a reduction in thickness at the joint positions can't reflect either the complex joint behaviour or the lining overall deforming pattern. In addition, the failure of steel plates strengthened tunnels always occurs as a thin layer of the lining concrete at the interface being pulled off (Liu et al., 2017). Therefore, the tunnel model material with a mechanical characteristic similar to concrete is important to achieve modelling of the strengthening failure mode. A tunnel model considering both casting and joint characteristics is proposed and applied in this research.

The tunnel model was designed as shown in Fig. 5 and 6 with the dimensions listed in Table 3. The tunnel model was made of gypsum mortar, iron wire and iron pieces. There were two iron pieces placed at every position of the segmental joint, and the wires were circled through the iron pieces with the aim of modelling the bolt connection of the joints, as seen in Fig.6 (b). Based on the study of Wang et al. (2019a), the gypsum mortar mix using water, gypsum and diatomite in a proportion of 1:1.3:0.1 was selected to meet the scale ratio required in this research. The mechanical parameters of the lining gypsum were measured using uniaxial compression tests. The parameters are listed in Table 4.

When the overall deformation of the segmental tunnel linings occurs as shown in Fig. 7, segments

rotate relative to the adjacent ones at the joints. In this way, the wire will be placed in tension and behave as bolts. Therefore, the stiffness of the iron wires is a key parameter which considerably influences both the joint stiffness and overall stiffness of a lining ring. In this research, the requirement of wire size is to keep overall stiffness of the model tunnel similar to that of the prototype. The effective ratio of the transverse bending rigidity (η) is often adopted as a general index to evaluate the overall stiffness of segmental rings during the design process for segmental tunnel linings (Lee and Ge, 2001, Koyama, 2003). Based on the study of the segmental tunnel linings in the Shanghai metro, Huang et al. (2006) suggested that the value of η equals 0.67 for the straight-jointed assembly conditions. This value is adopted to determine the size of the wire for the tunnel model in this research. A finite element model for the tunnel model was developed by using FE software ABAQUS as shown in Fig. 6 (a), which is assembled using lining segments simulated by solid elements and embedded iron wires simulated by beam elements. The material properties were assumed to be elastic and given the properties listed in Table 3. By applying the same concentrated load at the tunnel crown in the numerical models, the vertical diameter changes of the continuous ring ($\Delta D_{v,CR}$) and segmental linings ($\Delta D_{v,SL}$) could be obtained as shown in Fig. 6 (b). The value of η was evaluated as $\eta = \frac{\Delta D_{v,CR}}{\Delta D_{v,SL}}$. Thus, the η values of model tunnels with different iron wire sizes could be calculated numerically, from which the wires with a $\Phi 1.6\text{mm}$ were adopted in this research.

The manufacture process use for the tunnel model is shown in Fig. 8. An assembled mould is designed and used for producing the tunnel models. Following these six steps, an appropriate model for the segmental tunnel linings was obtained as shown in the “Step 6” in Fig. 8.

There are four lining rings in one test. Ideally, all the segmental lining rings should behave identically

in the plane strain test condition. The adjacent lining rings were designed to be connected using screws and wire. As shown in Fig. 6 (a), the screws were installed every 45° around the lining external profile in the tunnel transverse section. Fig. 6 (b) presents a detailed drawing of the connection, with wire used to secure the adjacent screws on the adjacent lining rings. Thus, eight sets of such connection pairs were constructed along the tunnel section to secure one lining ring to another.

2.5. Modelling the steel plate strengthening for existing tunnels

Aluminum plates were employed to model the steel plates for strengthening the tunnel linings. The aluminum plate size was determined using the scaling law by following equation:

$$I_m = n_{EI} \cdot \frac{E_p}{E_m} I_p \quad (1)$$

Where n_{EI} is the scale ratio for the flexural rigidity listed in Table 1, E_p and E_m are the elastic modulus of the prototype and the model, $I = bt^3 / 12$ is the rotation inertia of the aluminum or steel plate sections, b and t are the width and thickness of the steel or aluminum plates. In this research, $E_p = E_s = 200GPa$, $E_m = E_a = 70GPa$, $b_p = 1000mm$, $t_p = 30mm$. Thus, the appropriate size of the aluminum plates section was adopted as $b_m = 60mm$, $t_m = 1.2mm$.

The process of steel plate strengthening in the model tests is illustrated in Fig. 9. First, the epoxy resin glue was uniformly smeared onto the inner surface of segmental tunnel linings. Subsequently, the aluminum plates with a length of the half inner tunnel circumference were installed at corresponding positions one after another, which were fixed to tunnel lining with screws (shown as Fig. 9 (a)). With all the aluminum plates installed, the whole strengthening was finally completed after 24 hours to allow the epoxy resin glue to set. The strengthening process was thus completed

and the strengthened segmental tunnel lining is shown in Fig. 9 (b). The purpose of using screws was to fix the steel plates position during the curing of the epoxy resin adhesive, although the screws themselves would have enhanced the interface property.

2.6. Tests procedure

During all the tests, the surcharge load was applied at intervals of 0.75kN to the soil surface in the test tank. Additional load was not applied until the movement of the loading plate stopped, thus, the whole loading process could be considered static. Tests for the strengthened tunnels were conducted in three steps as shown in Fig. 10. In Step 1, the applied load P was increased to p_1 , in which the tunnel without steel plates (noted: in the model test were aluminum plates) was stressed to a deformed status. In Step 2, the applied p_1 was unloaded to model an unloading process. The deformed tunnel was then strengthened with the steel plates. In Step 3, another surcharge load $P=p_3$ was applied onto the strengthened tunnel. This step was not stopped until failure occurred in the strengthened lining.

A series of tests for tunnels strengthened at different degrees of deformation are listed in Table 5. Test No.1 is for the segmental tunnel lining without any strengthening treatment, while Tests No.2 to No.4 are for tunnels strengthened by steel plates. The surcharge load before strengthening (p_1) is varied to stress the tunnels to different degrees of deformation before strengthening.

3. Results and data analysis

In this section, the experimental data will be analysed with respect to the model scale. The analysis for tunnels without strengthening (Test No. 1) will be presented in Section 3.1. The analysis for

tunnels with steel plate strengthening (Test No. 2) will be presented later.

3.1. Tunnel without strengthening (Test No. 1)

The test No. 1 was conducted on a tunnel without strengthening. The tunnel profiles before and after loading are shown in Fig. 11 (a) and (b), where the overall shape of tunnel changed from a circle to an oval as the applied load increased. It was observed that the tunnel crown went downwards and the lining expanded horizontally at the spring-line. The relative deformation increased at larger rate as the surcharge increased. Joint opening was observed during the test, with the joints near the tunnel crown opening inwards, while the joints near the tunnel spring-line opening outwards. A creak broke through the lining segment near the tunnel invert at end of the test.

The changing values in the horizontal and vertical diameters of the tunnel lining are presented in terms of P - ΔD curves in Fig. 12. The tunnel deformation developed nonlinearly as the load being increased. When $P < 2\text{kN}$, both ΔD_h and ΔD_v increased slightly and equally, which means the tunnel linings were still deforming as a circular shape with good structural conditions. When $2\text{kN} < P < 5\text{kN}$, ΔD_h and ΔD_v increased by 4-6mm, which indicate that the tunnel gradually deformed from a circle to an oval shape. Changes in curve slopes implies a decrease in the overall lining stiffness. When $P > 5\text{kN}$, ΔD_h and ΔD_v developed rapidly, with a small increase in the applied load resulting in a significant change in the tunnel lining profile.

From the measured tunnel deformation, significant loss of tunnel lining stiffness was observed when the tunnel profile changed from a circle to an oval shape. This overall stiffness loss was a result of some of the partial defects within the lining segments. Some of the detailed features within

the damaged segmental tunnel linings are shown in Fig. 13. Inward openings of the joints near the tunnel crown were observed as shown in Fig. 13 (a), where relative rotation occurred between adjacent segments resulting in the segment outer edges being compressed. In contrast, outward openings were observed at the joints near the tunnel spring-line as shown in Fig. 13 (b), where relative rotation occurred resulting in the segment inner edges being compressed to crush due to stress concentration (Fig. 13 (c)). As illustrated in Fig. 13 (d), at positions near the tunnel invert, cracks arose and developed through the invert segment from the inner to the outer edges, which resulted in a significant reduction in bending rigidity of these segments. Therefore, it was a result of all these partial defects that led to a reduction in the overall stiffness degradation of the segmental tunnel linings.

The circumferential strain values were measured at the inner and outer tunnel surfaces by attached strain gauges. The strain development at locations of the tunnel crown, spring-line and invert are illustrated in Fig. 14, respectively.

The strains at the tunnel crown are shown in Fig. 14 (a), and demonstrate there was compression on the outer edge and tension on the inner edge, which indicates a bending moment leading to the inward joint opening near the tunnel crown (as seen in Fig. 13 (a)). The absolute values of both the tension and compression strains increased as the applied load increased, while the magnitudes in compression were higher than those in tension.

The lining conditions at the tunnel spring-line are shown in Fig. 14 (b), and demonstrate there was tension on the outer surface and compression on the inner surface, which indicates a bending moment leading to outward joints openings near the tunnel spring-line (as seen in Fig. 13 (b)). The magnitudes of the inner compressive strains were higher than those of outer surface tensile strains.

The strains at the tunnel invert are shown in Fig. 14 (c), and demonstrate there was compression on the outer surface and tension on the inner surface.

A sudden drop in tensile strains at the tunnel invert was observed at $P=5.2\text{kN}$ (Fig. 14 (c)), which is just at the moment that the crack within segment D occurred, seen in Fig. 13 (d). The appearance of the cracks at the tunnel invert resulted in a sudden reduction in bending rigidity of segment D, which led to stress relief at the invert and simultaneous stress intensity elsewhere (seen as a sudden change in the strain values in Fig. 14 (a) and (b) at $P=5.2\text{kN}$). This redistribution of stress was also accompanied with an increase in overall deformation and reduction in integral structural stiffness observed as an inflection in the $P-\Delta D$ curves in Fig. 12.

3.2. Tunnel strengthened by steel plates (Test No. 2)

Subsequent to the results of the tunnel without strengthening (Test No. 1), Test No. 2 involved the over-deformed tunnel being strengthened by steel plates (modelled by aluminum plates).

Photographs of the tunnel at moments just after strengthening and then just after strengthening failure are shown in Fig. 15 (a) and (b) respectively. In Fig. 15 (a), the tunnel profile had already deformed to an oval shape, with defects such as joint openings and cracks visible. This deformed tunnel was then strengthened using the aluminum plates as described in Section 2.5.

During the loading process after strengthening, no significant additional deformation in the strengthened tunnel lining was observed until a sudden failure occurred at the interface between the tunnel lining and the aluminum plates accompanied with a sound of breaking. A sudden movement of segment linings was observed with a downwards movement at the tunnel crown and outwards movement at the tunnel spring-line. The final profile after the strengthening failure is

298 shown in Fig. 15 (b), where severe damage of tunnel lining and a significant debonding at tunnel-
 299 steel interface can be observed. In contrast, the tunnel without steel plates deformed gradually
 300 without a sudden failure as the surcharge load increased (as seen in Fig. 11).

301 Some details of the strengthened tunnel after the occurrence of strengthening failure are shown in
 302 Fig. 16. Debonding failure occurred at the interface between the tunnel lining and the steel plate in
 303 the ranges $20^{\circ}\sim 50^{\circ}$ and $200^{\circ}\sim 230^{\circ}$ (clockwise from the tunnel crown), where a thin layer of gypsum
 304 attached to aluminum plates was detached from the segment surface. A significant shear crack
 305 throughout the segment was observed near tunnel crown where the debonding failure occurs, this
 306 is because the sudden interface failure resulted in a sharp increase in the shear force within the
 307 lining segment. It should be noted that, the interface conditions at the positions near the tunnel
 308 spring-line were still well-bonded.

309 The evolution of the tunnel deformation before and after the installation of the steel plate can be
 310 illustrated as $P-\Delta D_h$ and $P-\Delta D_v$ curves as shown in Fig. 17 (a) and (b). When $P < 6\text{kN}$, the trends of
 311 both the $P-\Delta D_h$ and $P-\Delta D_v$ curves coincide well with the curves for the tunnel without strengthening.
 312 Subsequently, as the tunnel was unloaded at $P=6\text{kN}$, the horizontal tunnel diameter recovered by
 313 0.7mm (as shown in Fig. 17 (a)), and the vertical tunnel diameter expanded by approximate 0.2mm
 314 (as shown in Fig. 17 (b)).

315 The damaged tunnel was strengthened at a deformation of $\Delta D_h = 9.3\text{mm}$ and $\Delta D_v = 11.8\text{mm}$. As
 316 observed in Fig. 17, the behaviour after strengthening demonstrates the structural stiffness of the
 317 strengthened lining was significantly improved by 1.9 times compared to that of the tunnel without
 318 strengthening. The deformation of the strengthened segmental lining didn't change much until the
 319 debonding failure occurred at $P=11.7\text{kN}$, and the bearing capacity is improved by 69%. As

mentioned previously, the brittle debonding failure at the interface resulted in an abrupt loss in structural stiffness of the strengthened tunnel lining, after which the tunnel lining behaved flexibly and the applied surcharge load could not be increased.

The strains of the lining segments and the steel plates were measured at different positions as shown in Fig. 18. Due to the strengthening operation in the tunnel during the experiment, strain gauges could only be attached to the outer surface of the lining segments and the aluminum plate. The strains measured at the tunnel crown are illustrated in Fig. 18 (a). The outer surface of the lining segment was compressed, while the aluminum plates were in tension. It can be seen that the segment strain reduced to zero without any residual strain after the unloading at $P=6\text{kN}$. After strengthening, the tensile strain in the aluminum plates and the compression strain in the outer surface of the tunnel increased simultaneously as the surcharge load increased until the sudden strengthening failure occurred at $P=11.7\text{kN}$. The strain in aluminum plate instantaneously reduced at this point due to the interface debonding failure near tunnel crown, after which the aluminum plates near the tunnel crown were no longer stressed.

The strains measured at the tunnel spring-line are illustrated in Fig. 18 (b). The lining segment was subjected to tension on the outer surface, while the aluminum plate was subjected to compression. There was still some residual strain evident within the segments at this position after the unloading at $P=6\text{kN}$. After strengthening, the compressive strain in the aluminum plate and the tensile strain in the lining segment kept increasing until failure occurred.

The strains measured at the tunnel invert are illustrated in Fig. 18 (c). It is observed that there was only a small proportion of strain recovered after the unloading.

From strain measurements at all three positions when the strengthening failure happened at

$P=11.7\text{kN}$, it can be observed in Fig. 18 (a) and (c) that there was a sharp decline in tensile strains of the steel plate at the tunnel crown and invert. This is because of the sudden interface debonding failure near the tunnel crown and invert, as seen in Fig. 18. Thereafter, the strengthened aluminum plates no longer behaved as a component of the composite lining system. This explains the reason for the sudden drop in overall structural stiffness in the tunnel lining observed in Fig. 17.

To investigate how the steel plates behave when used to strengthen the existing segmental tunnel linings, the strain values measured at different loading stages ($P=2\text{kN}$, 6kN and 10kN) are presented in Fig. 19, where tensile strains are positive and compressive strains are negative. It is observed that the aluminum plate was subjected to compression at 90° and 270° , while it is in tension at other measurement positions. All the strains increased as the load P being increased. The maximum tensile strain appeared at the tunnel invert and the maximum compressive strain appeared at the tunnel spring-line, while the absolute value of the maximum tension strain is nearly twice as high compared to the maximum compressive strain.

4. Discussion

As introduced in Section 2.6, tunnels being strengthened at different degrees of damage were tested, i.e. Test No. 2 is the tunnel being strengthened at ($P_1=6\text{kN}$, $\Delta D_{h1}=9\text{mm}$, $\Delta D_{v1}=11\text{mm}$), Test No. 3 is the tunnel being strengthened at ($P_1=4\text{kN}$, $\Delta D_{h1}=3\text{mm}$, $\Delta D_{v1}=5\text{mm}$), and Test No. 4 is the tunnel being strengthened at ($P_1=0$, $\Delta D_{h1}=0$, $\Delta D_{v1}=0$). In this section, the performance of tunnels in all these tests are compared in terms of the load-deformation curves to show the influence of the existing deformation on post-strengthened tunnel performance.

For the comparison purpose, two dimensionless indicators, i.e. ovality and surcharge level, are

proposed as Equations (2) and (3) to evaluate the changes in tunnel transverse profiles and the degree of the applied surcharge load, respectively.

$$O = (\Delta D_h + \Delta D_v) / 2D_0 \quad (2)$$

$$SL = p / \gamma h \quad (3)$$

where ΔD_h and ΔD_v are absolute values of the changing in horizontal and vertical tunnel diameters, p is the equivalent surcharge calculated as applied load P divided by the square of the soil box cross section, γ and h are the unit weight of sand and cover depth of the tunnel shown in Table 2. The behaviour of the strengthened tunnels in the different tests are illustrated as the $SL-O$ curves as shown in Fig. 20. To emphasise the improvement in the lining performance due to the strengthening, only the parts of curves exceeding the curve for the tunnel without strengthening are kept in this figure.

In order to quantitatively compare the improvement of the tunnel stiffness due to strengthening, a linear regression for the data of the $SL-O$ curves from the starting point of the strengthening to the failure point of the strengthening are presented in Fig. 20. The regression coefficients have been used to define a stiffness improvement ratio (denoted by k_s), since this value indicates the composite tunnel stiffness of the segmental lining after strengthening.

As seen in Fig. 20, the stiffness improvement ratio k_{s-4} for test No.4 equals 1.37 ($k_{s-3}=1.12$ for test No.3, $k_{s-2}=0.74$ for test No.2). The stiffness improvement ratio (k_s) decreases due to the increase in pre-strengthening tunnel deformation. This means that the postponement of strengthening will cause a decrease in the tunnel stiffness after strengthening. This is because as the tunnel deformation before strengthening increases, the original tunnel stiffness decreases. The structural stiffness of the retrofitted lining depends on both the original segmental lining and the steel plates.

Thus, a reduction in segmental lining stiffness due to the delay of strengthening will certainly result in a decrease in the strengthened tunnel stiffness, which appears as a drop of k_s .

In order to compare the improvement in total capacity of the tunnel lining due to strengthening at different points, the surcharge level values at the strengthening failure point in each test have been extracted and denoted as SL_f . As seen in Fig.20, the total capacity of the tunnel lining in test No.4 is $SL_{f-4}=0.44$ ($SL_{f-3}=0.78$ in test No.3, $SL_{f-2}=0.91$ in test No.2). The total surcharge that can be applied rises, since the strengthening point is postponed. This means that some allowance of tunnel deformation before strengthening can achieve a higher total capacity of the tunnel support after strengthening. Therefore, a sufficient use of the original lining capacity before strengthening benefits the tunnel from the perspective of the total capacity. In practice, it is inappropriate to apply the steel plate strengthening too early to the segmental lining with relatively small deformation.

In addition, the increased capacity due to strengthening (denoted as Δ_{SL}) is calculated by the following equation:

$$\Delta_{SL} = SL_f - SL_s \quad (4)$$

Where SL_s and SL_f are the surcharge levels at the strengthening point and at the strengthening failure point respectively.

As illustrated in Fig.20, the increased capacity of the tunnel after strengthening in test No.4 is $\Delta_{SL-4}=0.421$ ($\Delta_{SL-3}=0.442$ in test No.3, $\Delta_{SL-2}=0.439$ in test No.2). It can be seen that there is only a small variance in the increased capacity values, despite the difference in the strengthening point. This means that the improvement in the tunnel bearing capacity after strengthening is not much affected by the variance in the tunnel deformation before strengthening.

After strengthening, the retrofitted tunnel behaves as a composite lining composed of the external

original segmental linings and the internal steel plates. The interface between the two components plays a key role. In this experiment, the strengthening failure occurred in the form of interface debonding. The increased capacity of the tunnel after strengthening is related to the interface property, which was kept unchanged in the series of tests in this study. Thus, further research could be conducted to investigate the influence of different interface properties on the segmental tunnel linings strengthened by steel plates.

5. Conclusions

In this paper, a 1-g physical model test was designed and performed to investigate the effectiveness of using steel plates to strengthen the over-deformed segmental tunnel linings. A series of tests were performed for the tunnel without strengthening and for the tunnels being strengthened at different degrees of deformation. The performance was analysed based on data for both the tunnels with and without steel plates strengthening. Some conclusions can be drawn from these tests as follows:

(1) Segmental tunnel linings affected by ground surface surcharge deform nonlinearly. As the applied surcharge increases, the joints open and eventually the concrete crushes and lining cracks at the tunnel invert, which leads to a gradual degradation of tunnel lining performance.

(2) Compared with the tunnel without strengthening, the structural performance of the damaged segmental tunnel linings are significantly enhanced with steel plates strengthening. For example, comparing between the results from Test No. 1 (no strengthening) and No. 2 (strengthened tunnel), the stiffness and capacity of the tunnel was improved by 190% and 69%, respectively, due to the steel plate strengthening.

(3) An increase in the tunnel deformation before strengthening (i.e., postponement of strengthening) will result in a decrease in the stiffness and an increase in the total capacity of the tunnel after strengthening, while the increased capacity will be less affected.

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507 **Table 1.** Scale Factors adopted in 1-g model test

Quantity	Symbol	General	Scaling ratio
Length	l	n_l	1:15
Unit weight	γ	n_γ	1:1
Elastic modulus	E	$n_E=n_l \times n_\gamma$	1:15
Pressure	q	$n_q=n_l \times n_\gamma$	1:15
Strain	σ	$n_\sigma=n_L \times n_\gamma$	1:15
Displacement	δ	$n_\delta=n_l$	1:15
Strain	ε	n_ε	1:1
Force	F	$n_F=n_l^3 \times n_\gamma$	1:15 ³
Moment	M	$n_M=n_l^4 \times n_\gamma$	1:15 ⁴
Flexural rigidity	EI	$n_{EI}=n_E \times n_l^4$	1:15 ⁵

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510 **Table 2.** Properties of the model soil materials

Parameters	Unit	Symbol	Rubber particles	Dry sand
Unit weight	kN/m ³	γ	8.6	15.6
Water content	%	w	0	0
Medium grain size	mm	d_{50}	3	0.32
Uniformity coefficient	-	C_u	1.9	3.3
Compression modulus	MPa	E_s	0.51	18.18
Friction angle	°	φ	31.5	33.1

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513 **Table 3.** tunnel model dimensions

Quantity	Symbol	Unit	Model	Prototype	Scaled ratio
Outer diameter	D	mm	410	6150	1:15
Lining thickness	t	mm	25	375	1:15
Embedded wire diameter	ϕ	mm	1.6	-	-

514 **Table 4.** Properties of the gypsum used for tunnel model manufacture

Quantity	Symbol	Unit	Model	Prototype	Actual scaled ratio
Compressive strength	σ_g	MPa	2.23	32.4	1:14.5
Elastic modulus	E_g	GPa	1.89	34.5	1:18.2

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517 **Table 3.** A series of tests for tunnels strengthened at different degrees of damage

Test No.	p1 (kN)	Steel plate strengthening
1	-	No
2	6	Yes
3	4	Yes
4	0	Yes

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Figure 1 Photographs of the experiment apparatus, (a) an overview, (b) a view of the tunnel

Figure 2 A diagram showing the experimental apparatus (unit: mm)

Figure 3 Rubber particles and a sand sample

Figure 4 Test results for the model soil materials, (a) compressibility test results, (b) direct shear test results

Figure 5 A diagram showing the arrangement using to model the segmental tunnel lining

Figure 6 Detailed drawings of the segmental tunnel lining model (unit: mm), (a) An overall drawing

of the segmental lining ring and screws arrangement, (b) A detailed drawing of the segmental joint, (c) The connection between adjacent lining rings, (d) The interface between the lining and the steel plate.

Figure 7 Numerical simulation for tunnel model design (a) the finite element model (b) the numerical test for evaluating the effective ratio of the transverse bending rigidity.

Figure 8 Manufacturing process for the model segmental tunnel linings

Figure 9 modelling the steel plate strengthening for existing segmental tunnel linings using aluminum steel plates (a) Installing the aluminum plates (b) The final strengthened tunnel

Figure 10 Test procedure for the steel plates strengthened segmental tunnel linings

Figure 11 Photographs of the tunnel without strengthening (a) the initial tunnel profile; (b) the damaged tunnel profile

Figure 12 Tunnel cross-section deformation in terms of changes in horizontal and vertical diameters

Figure 13 Details of the defects in the damaged segmental tunnel linings

Figure 14 Strain measurements of lining segments at different locations, (a) crown (b) spring-line

(c) invert

Figure 15 Photographs of tunnels strengthened with aluminum plates, (a) after strengthening (b) after the occurrence of strengthening failure

Figure 16 Detailed features of the debonding failure of the strengthened segmental linings, (a) the interface near the tunnel invert, (b) the interface near the tunnel crown

(a)

(b)

Figure 17 P - ΔD curves for the tunnel strengthened by steel plates, (a) horizontal deformation P -

ΔD_h (b) vertical deformation P - ΔD_v

Figure 18 Strain values at the outer edge of the tunnel lining and the steel plate at different positions, (a) crown, (b) spring-line, (c) invert

Figure 19 Strain distribution in the strengthening steel plate at different loading stages

Figure 20 The relationship between the surcharge level and the ovality of the tunnels being strengthened at different degrees of damage