Modelling the dispersion and transport of reactive pollutants in a deep urban street canyon: Using large-eddy simulation

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Abstract:

This study investigates the dispersion and transport of reactive pollutants in a deep urban street canyon with an aspect ratio of 2 under neutral meteorological conditions using large-eddy simulation. The spatial variation of pollutants is significant due to the existence of two unsteady vortices. The deviation of species abundance from chemical equilibrium for the upper vortex is greater than that for the lower vortex. The interplay of dynamics and chemistry is investigated using two metrics: the photostationary state defect, and the inferred ozone production rate. The latter is found to be negative at all locations within the canyon, pointing to a systematic negative offset to ozone production rates inferred by analogous approaches in environments with incomplete emission mixing. This study demonstrates an approach to quantify parameters for a simplified two-box model, which could support traffic management and urban planning strategy or personal exposure assessment.

Capsule:

Reactive pollutants in a deep street canyon exhibit significant spatial variation driven by two unsteady vortices. A method of quantifying parameters of a two-box model is developed.

Keywords:

Urban street canyon, Large-eddy simulation, Pollutant removal, Turbulence, Two-box model.
1 Introduction

The term “street canyon” describes a restricted space (poor air ventilation) with surrounding buildings along both sides of the urban street. Vehicle emissions are dominant among various anthropogenic pollutant sources in urbanized areas (Liu et al., 2005). A combination of vehicle emissions and reduced dispersion caused by surrounding buildings could result in poor air quality at the pedestrian level, thereby leading to associated public health effects for those exposed to such environments (Solazzo et al., 2011). Understanding the dispersion and transport of reactive pollutants in urban street canyons is important to effectively quantify – and develop policies to mitigate – such impacts.

Various approaches have been undertaken over recent years to tackle the issue of air pollution inside street canyons. The most fundamental approach is direct field measurement, which can provide the first-hand and useful information. Examples of such approach include the studies by Xie et al. (2003), Kumar et al. (2008) and Prajapati et al. (2009). However, there are several disadvantages of field measurements, e.g. challenges to data interpretation, uncontrollable meteorological conditions, low spatial coverage, and high expense. An alternative approach is physical modelling, such as wind tunnels, e.g. Sagrado et al. (2002), Kovar-Panskus et al. (2002), Park et al. (2004) and Michioka et al. (2011), and water channels, e.g. Caton et al. (2003), Jiang et al. (2007) and Li et al. (2008a). Physical modelling offers the advantages of fully controlling testing parameters and sampling points so as to provide useful data for the evaluation of numerical models. However, there is a challenge for such models to replicate fully the large-scale atmospheric turbulence of the real world due to the scale limitation. Another useful alternative approach is numerical simulation (e.g. computational fluid dynamics, CFD). With rapid development of advanced computer technology, CFD has become a useful tool to explore experimental flow and pollutant dispersion problems (Chang, 2006), providing a complete view of distribution of flow and pollutant fields at high-resolution in both time and space. The most comprehensive applications of CFD have been based on Reynolds-averaged Navier–Stokes (RANS) equations and large-eddy
RANS can only predict mean information about the flow and pollutant fields, while LES also provides the turbulent information about unsteadiness and intermittency (Cai et al., 2008).

The flow patterns in a street canyon under neutral meteorological conditions can be classified into three main regimes (Oke, 1987): isolated roughness, wake interference and skimming flow, depending on the aspect ratio (AR, the ratio of building height $H$ to street width $W$). Skimming flow, which has been the subject of several studies and will be further investigated here, normally occurs in the regular street canyons (0.7<AR<1.5) and deep street canyons (AR > 1.5) (Murena et al., 2009). A single primary vortex is formed within the regular street canyon (e.g. AR=1), which has been extensively studied. Most studies only considered passive pollutants (i.e. non-reactive scalars). However, vehicle emissions are chemically reactive, evolving on the timescale of typical canyon circulation and residence times. Such chemical processes are expected to play a role in determining abundance, alongside dispersion and transport, of reactive pollutants. Baker et al. (2004) introduced simple NO$_x$-O$_3$ chemistry into a LES model and examined reactive pollutant dispersion and transport inside a regular street canyon (AR=1). The concept of the photostationary state (PSS) defect was introduced and served as a sensitive indicator of reactive mixing. Baik et al. (2007) carried out a RANS model of a regular street canyon (AR=1) using the same chemistry as the study by Baker et al. (2004). Both these studies showed that the chemistry is close to equilibrium within the primary canyon vortex, but far from equilibrium at the canyon roof level where air exchange between the canyon and the overlying background takes place. Kikumoto and Ooka (2012) investigated the transport and dispersion of atmospheric pollutants within a regular street canyon (AR=1) by using LES coupled with a bimolecular chemical reaction (O$_3$ + NO $\rightarrow$ product). They found that NO$_x$ and O$_3$ have contrasted mechanism of transport and the correlation between the reactants’ concentration fluctuations strongly influences the reaction rates at the canyon roof level. Kwak and Baik (2012) and Kwak et al. (2013) employed a RANS model coupled with the carbon bond mechanism IV (CBM-IV) considering the chemistry of O$_3$, NO$_x$ and volatile organic
compounds (VOCs) in idealized street canyons (AR=1,2). They found that both O$_3$ and OH oxidation processes are of vital importance in the canyon-scale chemistry and that there are two counter-rotating vortices in the street canyon with AR=2. According to Li et al. (2009), there are multiple vortices within a deep street canyon, which may create very poor ventilation conditions for pollutants. Thus the dispersion of pollutants in a deep street canyon could be substantially different from the AR=1 case, very complex in terms of both dynamical and chemical processing, and deserves a thorough examination.

This study investigates the dispersion and transport of reactive pollutants in a deep urban street canyon (AR=2). The LES methodology coupled with a simple chemical mechanism is employed as described in Section 2. In Section 3, the results of the LES dynamical model are evaluated against a water-channel experiment, and the characteristics of reactive pollutant dispersion from the LES coupled with the simple NO$_x$-O$_3$ chemistry are presented. A two-box model framework is developed. Finally, the conclusions are presented in Section 4.

2 Methodology

2.1 Numerical model

2.1.1 Flow equations

The LES model employed here is OpenFoam v2.1.1 (OpenFOAM, 2012), in which incompressible flow and neutral condition are assumed. The filtered momentum equations and continuity equations are

\[ \frac{\partial \tilde{u}_i}{\partial t} + \frac{\partial}{\partial x_j} \tilde{u}_i \tilde{u}_j = -\Delta P \delta_{ij} - \frac{\partial \tilde{P}}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} + \nu \frac{\partial^2 \tilde{u}_i}{\partial x_i \partial x_j} \]  
\[ \frac{\partial \tilde{u}_i}{\partial x_i} = 0 \]
where the overbar (\(\bar{}\)) represents the filtered quantity, \(\bar{u}_i\) \((i=1,2,3)\) are the filtered velocities, \(\Delta P\) is the large-scale kinematic pressure difference, \(\delta_{ij}\) is the Kronecker delta, \(\bar{p}\) is the filtered kinematic pressure, \(\nu\) is the kinematic molecular viscosity and \(\tau_{ij}\) represents the sub-grid scale (SGS) stresses, which are parameterised as follows:

\[
\tau_{ij} = -2\nu_{SGS} S_{ij}
\]  

(3)

\[
S_{ij} = \frac{1}{2} \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right)
\]  

(4)

\[
\nu_{SGS} = C_k \frac{k_{SGS}^{1/2}}{\Delta}
\]  

(5)

\[
\Delta = (\Delta_1 \Delta_2 \Delta_3)^{1/3}
\]  

(6)

\[
\frac{\partial k_{SGS}}{\partial t} + \frac{\partial}{\partial x_i} (k_{SGS} \bar{u}_i) = 2\nu_{SGS} S_{ij} S_{ij} + (\nu + \nu_{SGS}) \frac{\partial^2 k_{SGS}}{\partial x_i \partial x_i} - C_\varepsilon \frac{k_{SGS}^{3/2}}{\Delta}
\]  

(7)

where \(k_{SGS}\) is the SGS turbulent kinetic energy, \(\Delta_i\) \((i=1,2,3)\) are the local grid spacings and the modelling constants \(C_k = 0.094\), \(C_\varepsilon = 1.048\).

The study simulates the high Reynolds number \(\sim 10^6\) turbulent flow (see Section 2.2) in a deep street canyon with rough surfaces and the logarithmic law of the rough-wall (Schlichting and Gersten, 2000) is applied for the near-wall treatment:

\[
\bar{u}_1 = \frac{u_\tau}{\kappa} \ln \frac{z_\perp}{z_0}
\]  

(8)

where \(\bar{u}_1\) is the resolved scale velocity component parallel to the wall, \(u_\tau\) is the wall friction velocity, \(\kappa\) \((=0.42)\) is the von Kármán constant, \(z_\perp\) is the distance normal to the wall and \(z_0\) \((=0.015\) m representing a characteristic physical length of 0.15 m, e.g. window frames) is the aerodynamic surface roughness length. \(u_\tau\) is calculated by Equation (8) and used to derive \(\nu_{SGS}\) near the wall using
\[ \nu_{SGS} = \frac{u_i^2}{|\nabla u_1 \cdot \hat{n}|} \]  
\[(9)\]

where \( \hat{n} \) is the unit vector normal to the wall.

### 2.1.2 Equations for reactive pollutants

The reactive pollutants concerned here are nitric oxide (NO), nitrogen dioxide (NO\(_2\)) and ozone (O\(_3\)). The associated chemical reactions are (Carpenter et al., 1998):

\[ \text{NO}_2 + \text{hv} \rightarrow \text{NO} + \text{O} \]  
\[(10)\]

\[ \text{O} + \text{O}_2 + \text{M} \rightarrow \text{O}_3 + \text{M} \]  
\[(11)\]

\[ \text{O}_3 + \text{NO} \rightarrow \text{NO}_2 + \text{O}_2 \]  
\[(12)\]

where M denotes a third body molecule (usually O\(_2\) or N\(_2\)) which absorbs excess energy so that O and O\(_2\) may recombine to form an O\(_3\) molecule. The filtered equations for the concentrations of reactive pollutants are:

\[ \frac{\partial \bar{[\text{NO}]} }{\partial t} + \frac{\partial}{\partial x_i} (\bar{\pi}_i \bar{[\text{NO}]}) = \frac{\partial}{\partial x_i} \left( (\frac{\nu + \nu_{SGS}}{Sc}) \cdot \frac{\partial \bar{[\text{NO}]} }{\partial x_i} \right) + J_{NO_2} \bar{[\text{NO}_2]} - k_1 \bar{[O_3]} \bar{[\text{NO}]} + S_{NO} \]  
\[(13)\]

\[ \frac{\partial \bar{[\text{NO}_2]} }{\partial t} + \frac{\partial}{\partial x_i} (\bar{\pi}_i \bar{[\text{NO}_2]} ) = \frac{\partial}{\partial x_i} \left( (\frac{\nu + \nu_{SGS}}{Sc}) \cdot \frac{\partial \bar{[\text{NO}_2]} }{\partial x_i} \right) - J_{NO_2} \bar{[\text{NO}_2]} + k_1 \bar{[O_3]} \bar{[\text{NO}]} + S_{NO_2} \]  
\[(14)\]

\[ \frac{\partial \bar{[O_3]} }{\partial t} + \frac{\partial}{\partial x_i} (\bar{\pi}_i \bar{[O_3]} ) = \frac{\partial}{\partial x_i} \left( (\frac{\nu + \nu_{SGS}}{Sc}) \cdot \frac{\partial \bar{[O_3]} }{\partial x_i} \right) + k_2 \bar{[\text{O}]} \bar{[\text{O}_2]} - k_1 \bar{[O_3]} \bar{[\text{NO}]} \]  
\[(15)\]

where \( J_{NO_2} \) is the photolysis rate for NO\(_2\) in Reaction (10); \( k_1 \) and \( k_2 \) are the rate constants for Reactions (11) and (12), respectively; \( S_{NO} \) and \( S_{NO_2} \) are the emission rates for NO and NO\(_2\), respectively; \( Sc \) (=0.72) is the Schmidt number. Based on the pseudo-steady-state approximation for the highly reactive oxygen atom (O) (Seinfeld and Pandis, 1998), the formation rate of O by
Reaction (10) is the same as the depletion rate of O by Reaction (11). Thus, the following equation is derived:

$$k_2[\overline{O}][\overline{O}_2][\overline{M}] = J_{NO_2}[\overline{NO_2}].$$  \hspace{1cm} (16)

Therefore, substituting Equation (16) into Equation (15) yields:

$$\frac{\partial[\overline{O}_3]}{\partial t} + \frac{\partial}{\partial x_i}(\overline{u}_i[\overline{O}_3]) = \frac{\partial}{\partial x_i}(\frac{\partial}{\partial x_i}(\nu + \nu_{\text{SGS}})) \cdot \frac{\partial[\overline{O}_i]}{\partial x_i} + J_{NO_2}[\overline{NO_2}] - k_1[\overline{O}_3][\overline{NO}]$$  \hspace{1cm} (17)

For further analysis, the photostationary state (PSS) defect $d_{ps}$ (Baker et al., 2004) is defined:

$$d_{ps}(\%) = \left(\frac{k_1[\overline{O}_3][\overline{NO}]}{J_{NO_2}[\overline{NO_2}]} - 1\right) \times 100,$$  \hspace{1cm} (18)

where the values of $J_{NO_2}$ and $k_1$ are 0.0092 s$^{-1}$ and 0.0004 ppb$^{-1}$ s$^{-1}$, respectively (Bright et al., 2013).

$d_{ps}$ is a widely-used measure of the deviation from chemical equilibrium. The larger is the magnitude of $d_{ps}$, the higher is the deviation from the chemical equilibrium. $d_{ps} = 0$ means that the chemistry is at the equilibrium state.

We may also define $PO_3$ as the ozone production rate associated with the VOCs chemistry under the perfect mixing condition as follows. Atmospheric chemical reactions of hydro- and organic-peroxy radicals ($HO_2$ and $RO_2$) with NO generate NO$_2$ through:

$$NO + HO_2 \rightarrow NO_2 + OH$$  \hspace{1cm} (19)

$$NO + RO_2 \rightarrow NO_2 + RO$$  \hspace{1cm} (20)

Considering a chemical equilibrium system with perfect mixing comprising Reactions (10)-(12), (19) and (20), we obtain

$$J_{NO_2}[NO_2] - k_1[O_3][NO] = k_3[NO][HO_2] + \sum_i k_{4,i}[NO][RO_2],$$  \hspace{1cm} (21)
where \( k_3 \) and \( k_{4,i} \) are the rate constants for Reactions (19) and (20), respectively; \( i \) is the \( i^{th} \) organic-peroxy radical. The terms \( k_3[NO][HO_2] + \sum_i k_{4,i}[NO][RO_2] \) represent the rate of conversion of NO to NO\(_2\) (through the VOCs chemistry) which is subsequently photolysed leading to O\(_3\) production. Thus we define \( PO_3 = k_3[NO][HO_2] + \sum_i k_{4,i}[NO][RO_2] \). Due to the difficulties of evaluating \( HO_2 \) and \( RO_2 \) from measurement, we may use (21) to infer \( PO_3 \) from the \( NO_x \) and \( O_3 \) measurements:

\[
PO_3 = J_{NO_2}[\overline{NO_2}] - k_1[O_3][\overline{NO}],
\]

(22)

This is referred to as the \( NO_x-O_3 \)-steady-state-defect approach. In this approach, we assume that deviations from PSS arising from imperfect mixing are negligible (Volz-Thomas et al., 2003). We evaluate the accuracy of this assumption within the canyon environment in Section 3.2.1.

2.2 Model configuration and initialisation

Fig. 1 illustrates schematically the computational domain of an idealised deep street canyon (AR=2, i.e. \( H=36 \) m and \( W=18 \) m). The building width \( B \) is 18 m. The domain width sizes \((L_x \times L_y \times L_z)\) are \( 36 \times 40 \times 112 \) m. The grid resolutions \((\Delta x \times \Delta y \times \Delta z)\) are \( 0.3 \times 1 \times 0.3 \) m, with \( \Delta z \) gradually increasing from 0.3 m at the canyon roof level to a maximum value of 5.54 m at the top. The number of grid cells in the \( x \)-, \( y \)- and \( z \)-directions is \( 60 \times 40 \times 120 \) within the canyon and \( 120 \times 40 \times 40 \) above the canyon, respectively.

A constant pressure gradient \((\Delta P)\) across the free surface layer (above the canyon) is imposed in the \( x \)-direction to drive the atmospheric flow (perpendicular to the street axis), representing the worst-case scenario for the dispersion of reactive pollutants within a street canyon (Li et al., 2008b).

The prevailing wind speed \( U_f \) is about \( 2.2 \) m s\(^{-1}\) and the Reynolds number \( \text{Re} \) \((=U_f H / \nu)\) is the order of \( 10^6 \). For velocity components, the symmetry boundary condition is employed at the domain top. Cyclic boundary conditions are specified in both the \( x \)- and \( y \)-directions. Therefore, the model
configuration represents an infinite number of idealised street canyons along the $x$-direction and each canyon is infinitely long in the $y$-direction, which is a good approximation of real street canyons relevant to traffic management or urban planning.

Emissions sources are assumed to be two continuous line sources representing two lanes of traffic located at 2.5 m from both sides of the canyon centre at $z=1$ m with a Gaussian distribution (i.e. $\delta_x = 3$ m and $\delta_z = 1$ m) so that the near-vehicle dispersion is approximated. Drawing upon the UK Road Vehicle Emission Factors (Boulter et al., 2009b), the emission rate of NO$_x$ is determined as 620 g km$^{-1}$ h$^{-1}$, which represents an urban continuous road traffic of 1500 vehicles h$^{-1}$ with an average speed of 30 mph for a fleet composition representing the year of 2010 (Zhong et al., 2014). The total emission for NO$_x$ applied here is equivalent to 1000 ppb s$^{-1}$ released into a typical LES model grid (0.3 m$x$1 m$x$0.3 m) but this total emitted NO$_x$ is re-distributed based on the Gaussian distribution mentioned above. The ratio of NO to NO$_2$ emission rate is 9:1 by volume. The background concentrations of NO, NO$_2$ and O$_3$ used are 3.07, 6.02 and 43.62 ppb (Bright et al., 2013), respectively, which are uniformly distributed among the whole domain initially and also employed as the inlet boundary conditions, i.e. signifying no emissions from upwind canyons. For the outlet, the advective boundary condition (i.e. $\frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = 0$) is applied, representing no reflection of pollutants back into the computational domain. For the solid boundaries, zero-gradient boundaries are applied without considering the effect of pollutant deposition. The symmetry boundary is set on the top boundary and a cyclic boundary condition is adopted in the $y$-direction for the pollutants.

Initially, the LES model is run with dynamics only for 5 hours in order to generate a statistically steady turbulent flow. We take the dynamical-equilibrium flow field as the initial condition (i.e. $t = 0$ min) for the model in this study and further run the LES model without chemistry for the first 30 min before considering chemistry. At $t = 30$ min, the chemistry scheme
and emissions modules are turned on for the next 210 min \((t = 30 \text{ to } 240 \text{ min})\) with a time step of 0.03 s in order to reach chemical quasi-equilibrium. For the analysis, the simulation 3-D outputs over the last 60 min period \((t = 180 \text{ to } 240 \text{ min})\) at a time interval of 3 s are stored and post-processed to derive the resolved-scale turbulent statistics based on the averages over the period and along the \(y\)-direction. This temporal average over \(t \in [t_1, t_2]\) and spatial average over \(y \in [0, L_y]\) of any quantity \(\bar{\varphi} = \langle \bar{\varphi} \rangle + \phi\) gives \(\langle \bar{\varphi} \rangle\), which is a 2D function of \((x, z)\):

\[
\langle \bar{\varphi} \rangle(x, z) = \frac{1}{L_y (t_2 - t_1)} \int_{t_1}^{t_2} \int_{0}^{L_y} \bar{\varphi}(x, y, z, t) dy dt
\]

(23)

and the fluctuation component \(\phi\) is described as follows:

\[
\phi (x, z) = \frac{1}{L_y (t_2 - t_1)} \int_{t_1}^{t_2} \int_{0}^{L_y} [\bar{\varphi}(x, y, z, t) - \langle \bar{\varphi} \rangle(x, z)] dy dt
\]

(24)

### 3 Results and discussion

#### 3.1 Flow field

A water-channel experiment (Li et al., 2008a) is employed to evaluate the performance of the current LES simulation with respect to the flow field. This water-channel experiment was conducted in a laboratory flume, which was 10 m in length, 0.3 m in width and 0.5 m in height.

Several identical building blocks \((0.1 \text{ m} \times 0.3 \text{ m} \times 0.1 \text{ m}\) in the \(x\)-, \(y\)- and \(z\)- directions) were placed perpendicular to the flow with the street width of 0.05 m (i.e. AR=2). The laser Doppler anemometer technique was applied for the data acquisition of the velocities and turbulent statistics.

Fig. 2 shows the comparison of vertical profiles of the normalized averaged streamwise and vertical velocities and their fluctuation intensities at the upstream, centre and downstream locations for the deep street canon (AR=2) between the current LES simulation and the water-channel experiment.
All of the quantities in Fig. 2 are normalized by $u_{norm}$ (the averaged value of $\langle \bar{u} \rangle$ at the height $1.0 \leq z / H \leq 1.1$). Fig 2a presents the mean streamwise velocity and there is clear evidence of a shear layer across the canyon roof level, at which strong wind shear strength is observed. Fig. 2b shows the vertical mean velocities and there is clear evidence of the complicated flow pattern: the clockwise vortex in the upper part of the canyon and the weak anti-clockwise vortex in the lower part of the canyon. The upper recirculation is created by the strong wind shear at the roof level and the lower recirculation is generated by a relatively weaker wind shear induced by the upper recirculation. Figs. 2c and 2d illustrate the intensity of resolved-scale fluctuations of the two velocity components, which display local maxima at the canyon roof level. These maxima may be caused by the instability of the wind shear-layer at the canyon roof level. As shown in Fig. 2, there are some small discrepancies between the current LES simulation and the water-channel experiment. The current LES simulation generally slightly underestimates all the quantities. There are several possible reasons for this. Firstly, due to the computational cost, a limited computational domain is employed in the current LES simulation, only representing eddies with sizes smaller than half of the domain width. However, eddies in the experiment are created by the vortex generators and there may be larger eddies which are not modelled in the LES simulation. Secondly, the grid mesh might not be fine enough across the shear-layer, and so some small eddies within the shear-layer and the momentum exchange caused by these small eddies might not be resolved. Finally, these discrepancies may be attributed to different averaging approaches. In the LES simulation, the temporal and spatial averaging approach is adopted to derive the flow quantities. In the experiment, these quantities were only measured on a middle vertical plane in the $y$-direction (Li et al., 2008a).

Fig. 3 illustrates the vortex structure in the current LES simulation compared with a wind tunnel experiment carried out by Kovar-Panskus et al. (2002). Both the model and experiment shows that there are two counter-rotating vortices formed within the deep street canyon (AR=2). This is a major difference from the single-vortex flow for a street canyon with AR=1 (e.g. Bright et al., 2013). The two-vortex mean flow was also found by other studies for AR=2 using RANS, e.g.
Kwak et al. (2013), but their RANS model generated a larger lower vortex than the one found in the water tank experiment and in the LES result here. It is also noted that the upper vortex is centred lower within the canyon compared with the experiment. Also, the centre of the lower vortex is shifted downstream closer to the windward wall compared with that of the upper vortex both in the model and experiment.

Overall, the current LES simulation agrees well with the experiments in terms of the velocities, turbulent intensities and vortex structure, which provides confidence that the simulated dynamics within the canyon is reasonable. However, there are currently no suitable water-channel or wind-tunnel experiments to evaluate the dispersion of reactive species, especially in deep street canyons.

### 3.2 Pollutant dispersion and transport

#### 3.2.1 Spatial variation of reactive pollutants

Figs. 4a-f depict contour plots of the spatially and temporally averaged mixing ratios of (a) $\langle NO \rangle$, (b) $\langle NO_2 \rangle$, (c) $\langle O_3 \rangle$, (d) $\langle NO_x \rangle$, (e) $\langle O_3 \rangle$, and (f) $\langle NO \rangle/\langle NO_2 \rangle$. The plots show the influence of two primary vortices, which span the deep street canyon: the upper clockwise vortex, and the lower anti-clockwise vortex. This influence was also found by Kwak et al. (2013) for the street canyon with AR=2. In general, the spatial patterns of the quantities for the upper vortex resemble those for the single vortex in a street canyon with AR=1, e.g. Baker et al. (2004), Baik et al. (2007), Bright et al., 2013, Garmory et al. (2009), Tong and Leung (2012), and Kwak and Baik (2012). There also exist two shear layers. The first one is at the canyon roof level with increasing turbulence from the leeward (upwind) building to the windward (downwind), which traps NO$_x$ emissions near the leeward building, allows more exchange near the windward building and entrains O$_3$ into the canyon toward the windward building. The other one is at the level of around z/W=0.5, which allows the NO$_x$ emissions generated at the ground level inside the lower vortex to intrude into the upper vortex and the ambient O$_3$ inside the upper vortex to be entrained into the lower vortex. NO$_x$
and O\(_3\) are allowed to mix and react with each other inside the two vortices in the presence of the two shear layers where exchanges take place. It is also noted that there is an accumulation of traffic emissions with a maximum value of about 1100 ppb for NO\(_x\) and a low level of O\(_3\) with a minimum value of about 4 ppb in the lower vortex. This is attributed to a high level of NO\(_x\) emitted into the very weak lower vortex to react with the limited O\(_3\) entrained along the windward wall from above. This is very different from what Kwak et al. (2013) showed in their Fig. 2(d) which gives a local maximum of about 30 ppb near the centre of the lower vortex. One explanation is that their emission rate of NO\(_x\) is much lower than ours (20 vs. 90 ppb s\(^{-1}\) released into 1 m\(^3\)). Considering the NO\(_x\)-O\(_3\) photochemistry, \(NO_x = (NO + NO_2)\) and the total oxidant \(O_3 = (O_3 + NO_2)\) are effectively passive, exhibiting a similar spatial distribution to each other. The ratio of NO/NO\(_2\) also shows a similar pattern across the two vortices ranging from about 6 at the right corner to about 3 at the canyon roof level, which indicates the conversion of NO to NO\(_2\) by the within-canyon chemistry.

Figs. 4g-h show contour plots of the spatially and temporally averaged \(d_{ps}\) and \(PO_3\). The magnitudes of \(d_{ps}\) and \(PO_3\) are smaller in the lower vortex than that in the upper vortex indicating that there is greater mixing for the chemistry system to reach the chemical equilibrium in the lower vortex compared to that in the upper vortex. This can be explained by the weaker vortex in the lower part of the canyon, where time scale is adequate to approach chemical equilibrium. A local maxima in \(d_{ps}\) (about 150\%) and \(PO_3\) (about -0.68 ppb s\(^{-1}\)) are observed across the canyon roof level in the presence of the strong turbulence. It is also observed that there are significantly larger values of \(d_{ps}\) and \(PO_3\) along the upper part of the windward building, indicating larger deviation from photochemical equilibrium in the region where two air parcels with very different chemical compositions interact.

Fig. 5 illustrates vertical profiles of (a) \(\langle NO \rangle\), (b) \(\langle NO_2 \rangle\), (c) \(\langle O_3 \rangle\), (d) \(\langle NO_x \rangle\), (e) \(\langle O_3 \rangle\), (f) \(\langle NO \rangle/\langle NO_2 \rangle\), (g) \(d_{ps}\), and (h) \(PO_3\) along the leeward and windward walls. These quantities are
averaged within the nearest three cells adjacent to the walls. The concentrations of NO, NO₂, NO₃, O₃, and NO/NO₂ on the leeward wall are higher (around 1.5 to 2 times) than those on the windward wall within the upper part of the canyon, but lower (around 50% to 70%) within the lower part. This indicates that traffic emissions are mainly trapped within the anti-clockwise lower vortex. For O₃, the situation is reversed with much lower values on the leeward wall (around 6 ppb) compared to those on the windward wall (ranging from about 6 ppb to 20 ppb) within the upper part of the canyon, but with slightly higher values (about 2 ppb difference) within the lower part. This is attributed to ambient O₃ being brought into the upper part of the canyon along the windward wall. It is also noted that the concentration reduces with height by a factor of about 0.8 on the leeward wall and by a factor of about 0.1 on the leeward wall for NO, NO₂, NO₃, O₃ and NO/NO₂, but increases by a factor of about 1.3 on the leeward wall and by a factor of about 5.5 on the leeward wall for O₃.

For the leeward wall, there is a sharp transition at the canyon roof level where each species rapidly approaches its background level, and a small gradient in concentration within the canyon. For the windward wall, there are two gradual transitions at the roof level and at the middle level of the canyon, respectively. These results for the upper part of the canyon match those of the field measurements by Xie et al. (2003), in which there was only one primary vortex inside the street canyon. The magnitudes of $d_p$ and PO₃ are very small (around 3% and 0.03 ppb s⁻¹, respectively) along the leeward wall inside the canyon, but increase rapidly within the shear layer at the roof level (around 80% and 0.40 ppb s⁻¹, respectively), where two air parcels with different compositions interact. Along the windward wall, the magnitudes of $d_p$ and PO₃ increase with height with much higher values in the upper part of the canyon, ranging from about 10% to 140% and from -0.08 ppb s⁻¹ to -0.53 ppb s⁻¹, respectively. This indicates that the deviation from chemical equilibrium is much larger in the upper vortex than that in the lower vortex.

Fig. 6 illustrates vertical profiles of the spatially and temporally averaged total, turbulent and advective fluxes, defined as $F_{total} = F_{adv} + F_{turb} = \langle \dot{w} \phi \rangle(x, z) + \langle \bar{w} \rangle(x, z) \langle \Phi \rangle(x, z)$, for NO, NO₂, O₃,
NOx, O3, and NO/NO2 averaged across the canyon. It is interesting to note that the advective fluxes are dominant for both the upper and lower vortices while turbulent fluxes are dominant for the shear layers. It is observed that there is a positive (upward) total flux for NO and NO2 from the canyon roof level into the background atmosphere aloft, and a negative (downward) total flux for O3 indicating that O3 is brought into the canyon from the overlying background atmosphere. A rapid increase in the total flux of NO and NO2 is observed from the ground to the level at z/W=0.1. This is due to the elevation of traffic emissions from the ground level. The total flux generally decreases with height for NO, but increases for NO2 indicating the conversion of NO to NO2 within the canyon chemical processing before they escape to the wider background environment. This conversion is also indicated as the ratios of total fluxes of NO to NO2 decrease with height from 9 near the emission source to about 4 at the canyon roof level. For the effective passive scalars NOx and O3, the total fluxes generally remain almost constant with height (around 5 ppb m s⁻¹ for NOx and 0.5 ppb m s⁻¹ for O3) except a rapid increase near the ground level.

In the model scheme used here, no peroxy radical reactions [Reactions (19) and (20)] are considered, i.e. net chemical ozone production cannot occur. Non-zero values for $d_{ps}$, therefore reflect the impact of imperfect mixing (heterogeneity) within the canyon, rather than ozone production chemistry. The values of $PO_3$ obtained here may therefore be regarded as measures of a systematic error in the NOx-O3-steady-state-defect approach to assess ozone production rates (via NOx/O3 measurements in the real atmosphere), i.e. indicating the magnitude of the imperfect-mixing-generated deviation from steady-state. The canyon averaged $PO_3 = -0.074$ ppb s⁻¹ (i.e. -266 ppb h⁻¹) (see Fig. 4h) indicates a negative bias results at all locations, which is large compared with measured free boundary layer / free troposphere ozone production rates [typically a few ppb h⁻¹, up to 50 ppb h⁻¹ in the most polluted regions, e.g. Mexico City (Wood et al., 2009)]. This reflects the fact that the $PO_3$ term effectively represents a small difference between two large quantities, such that the impact of mixing may be very substantial. In fact, this effect (imperfect mixing in the vicinity of NOx emission sources) is general, and so a systematic negative contribution to NOx-O3-
steady-state derived ozone production rates will recur throughout the urban atmosphere, to an extent dependent upon the local heterogeneity.

### 3.2.2 Development of a two-box model

The preliminary results from the LES model show the formation of two primary counter-rotating vortices in the deep street canyon (AR=2), providing the potential to develop an alternative simplified two-box model. By using a plane at the level of $z/W=0.5$ (or $z/H=0.25$), the deep street canyon is divided into two boxes with the corresponding vortex inside each box (Figs. 3 and 7). It is assumed that each vortex has sufficient intensity for the chemical species to be well-mixed within the corresponding box (Murena et al., 2011). The mass transfer between two adjacent boxes is expressed by the introduction of an ‘exchange velocity’. A one-box chemistry model has been previously adopted by Liu and Leung (2008) to study reactive pollutant dispersion in street canyons (AR=0.5, 1, 2), using the values of exchange velocity derived from LESs for different ARs. Because they treated the whole canyon as one well-mixed box for all ARs, the model is unable to reproduce the significant contrasts of pollutant concentration between the lower and upper canyon as shown in Fig. 4. In this study, a more complex box model (i.e. a two-box model) is adopted:

\[
\frac{dc_{i,L}}{dt} = -\frac{w_{i,L}}{H_L} (c_{i,L} - c_{i,U}) + \frac{w_{i,U}}{H_U} (c_{i,U} - c_{i,b}) + \Delta S_{i,L} \tag{25}
\]

\[
\frac{dc_{i,U}}{dt} = \frac{w_{i,L}}{H_U} (c_{i,L} - c_{i,U}) - \frac{w_{i,U}}{H_U} (c_{i,U} - c_{i,b}) + \Delta S_{i,U} \tag{26}
\]

where $c_{i,L}$, $c_{i,U}$, and $c_{i,b}$ are concentrations of $i^{th}$ species ($i=$NO, NO$_2$ and O$_3$) in the lower box, upper box and overlying background atmosphere, respectively; $H_L$ and $H_U$ are the heights of the lower and upper boxes, respectively; $w_{i,L}$ is the exchange velocity between the lower and upper boxes, and $w_{i,U}$ is the exchange velocity between the upper box and the overlying background.
atmosphere; \( \Delta S_{i,L} \) and \( \Delta S_{i,U} \) are chemical sources of \( i^{th} \) species in the lower and upper boxes, respectively; and \( E_{i,L} \) is emission rates of \( i^{th} \) species.

Exchange velocities implemented into the two-box model are determined from the current LES model by calculating the ventilation of a passive scalar, i.e. \( w_{i,L} = \frac{F_L}{c_{ps,L} - c_{ps,U}} \) and \( w_{i,U} = \frac{F_U}{c_{ps,U} - c_{ps,b}} \), where \( F_L \) is the flux between the lower and upper boxes, \( F_U \) is the flux between the upper box and the overlying background atmosphere and ‘ps’ denotes the passive scalar. The resulting values applied into the two-box model are 0.018 m s\(^{-1}\) for \( w_{i,L} \) and 0.014 m s\(^{-1}\) for \( w_{i,U} \). The two-box model is then compared with the LES model in terms of the time evolution of the volume averaged mixing ratios of NO, NO\(_2\), O\(_3\), NO\(_x\) and O\(_x\) (see Fig. 8). There are apparent fluctuations in the mixing ratios of chemical species inherent in the LES approach due to dynamically-driven variability of large scale eddies and unsteady ventilation caused by the two primary vortices in the canyon. The two-box model generally matches the LES approach with respect to the mixing ratios for the lower box, but slightly underestimates for the upper box compared with the LES results. This may attributed to the greater mixing for the lower vortex than that for the upper vortex in the LES, indicated by the very small values for the PSS defects (Fig. 4g and Fig. 5g).

### 4 Conclusions

The dispersion and transport of reactive pollutants in a deep urban street canyon (AR=2) has been examined using an LES model coupled with simple NO\(_x\)-O\(_3\) photochemistry. It is observed that there exist two vertically aligned vortices, agreeing reasonably well with a previous water channel experiment. Reactive pollutants exhibit significant spatial variation caused by the two unsteady vortices. Ground level sourced pollutants (NO\(_x\)) are found to be largely trapped within the lower
vortex with a maximum value of about 1100 ppb. The deviation from chemical equilibrium in the upper vortex is much greater than that in the lower vortex. Imperfect mixing (reflected in non-zero values for the PSS defect) results in negative apparent chemical ozone production, representing a systematic error if such an approach is applied to obtain ozone production rates within a poorly-mixed environment close to NO\textsubscript{x} emissions sources. The substantial magnitude of the apparent ozone loss rate, relative to those encountered in the wider boundary layer / free troposphere, further suggests that even at some distance from fresh emissions, mixing-derived PSS defects may limit this approach in inferring chemical ozone production. This study demonstrates an approach to quantify parameters for a simplified two-box model, which could support traffic management and urban planning strategy or personal exposure assessment. A challenging research task for future study is to incorporate complex chemical mechanisms and consider various aspect ratios and wind speeds.

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Fig. 1 Schematic diagram of the computational domain where $L_x = 36 \text{ m}$, $L_y = 40 \text{ m}$ and $L_z = 112 \text{ m}$. $H (=36 \text{ m})$ is the building height, $W (=18 \text{ m})$ is the street width and $B (=18 \text{ m})$ is the building width.
Fig 2. Comparison of the vertical profiles of the normalized averaged streamwise and vertical velocities and their fluctuations at the upstream ($x/W=-0.25$), centre ($x/W=0$) and downstream position ($x/W=0.25$) for the deep street canon with an aspect ratio of 2: (a) $\langle u \rangle / u_{\text{norm}}$, (b) $\langle w \rangle / u_{\text{norm}}$, (c) $u' / u_{\text{norm}}$ and (d) $w' / u_{\text{norm}}$. Solid lines represent the current LES simulation; Dark squares denote the water-channel experiment carried out by Li et al. (2008a).
Fig 3. Vortex structure in the (a) current LES simulation (b) wind tunnel experiment carried out by (Kovar-Panskus et al., 2002).
Fig. 4 Contour plots of the spatially and temporally averaged [see Equation (23)] (a) $\langle NO \rangle$, (b) $\langle NO_2 \rangle$, (c) $\langle O_3 \rangle$, (d) $\langle NO_x \rangle$, (e) $\langle O_x \rangle$, (f) $\langle NO \rangle/\langle NO_2 \rangle$, (g) $d_{ps}$ and (h) $PO_3$. 
Fig. 5 Vertical profiles of the spatially and temporally averaged [see Equation (23)] (a) $\langle NO \rangle$, (b) $\langle NO_2 \rangle$, (c) $\langle O_3 \rangle$, (d) $\langle NO_x \rangle$, (e) $\langle O_x \rangle$ and (f) $\langle NO \rangle/\langle NO_x \rangle$, (g) $\delta_p$, and (h) $PO_3$ along the leeward wall represented by the dash lines, and along the windward wall represented by the solid lines.
Fig. 6 Vertical profiles of the spatially and temporally averaged total, turbulent and advective fluxes for (a) NO, (b) NO$_2$, (c) O$_3$, (d) NO$_x$, (e) O$_x$, and (f) NO/NO$_2$ averaged across the canyon. The total, turbulent and advective fluxes for each quantity are represented by the solid, dash and dotted lines, respectively.
Fig. 7 Sketch of the two-box model framework. \( c_{i,L} \) (ppb), \( c_{i,U} \) (ppb) and \( c_{i,b} \) (ppb) are the concentrations of \( i^{th} \) species (i.e. NO, NO\(_2\) and O\(_3\)) in the lower box, upper box, and overlying background atmosphere, respectively; \( H_L \) (m) and \( H_U \) (m) are the height of the lower and upper boxes, respectively; \( W_{i,L} \) (m s\(^{-1}\)) is the exchange velocity between the lower and upper boxes, and \( W_{i,U} \) (m s\(^{-1}\)) is the exchange velocity between the upper box and the overlying background atmosphere; and \( E_{i,L} \) (ppb s\(^{-1}\)) is the emission rates of \( i^{th} \) species.
Fig. 8 Time evolution of the volume averaged mixing ratios of (a) NO, (b) NO$_2$, (c) O$_3$ and (d) NO$_x$ and O$_x$ calculated using the LES simulation (LES) and the two-box model (BOX), respectively. ‘L’ represents the lower box while ‘U’ represents the upper box.
References:


