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Observation of Iron Ore Beneficiation within a Spiral Concentrator by Positron Emission Particle Tracking of Large (Ø≈1440 μm) and Small (Ø≈58 μm) Hematite and Quartz Tracers

D. Boucher*, Z. Deng², T. Leadbeater², R. Langlois³, K. Waters³

*Department of Mining and Materials Engineering, McGill University, 3610 University Street, Montreal, Quebec, H3A 0C5, Canada
²School of Physics and Astronomy, University of Birmingham, Edgbaston, Birmingham, B15 2TT, United Kingdom

*Author for Correspondence:
Email: darryel.boucher@mail.mcgill.ca
Tel: +1 514 398 4755 x09503

Abstract
This paper presents the results of using positron emission particle tracking to record the trajectories of large (Ø≈1440 μm) and small (Ø≈58 μm) particles of hematite (S.G.≈5.3) and quartz (S.G.≈2.7) in a slurry of iron ore (20 % solids w/w) flowing in a gravity spiral concentrator. The tracking was undertaken using modular positron emission particle tracking detectors (ECAT 951) assembled and calibrated for this purpose. The tracer particles used were generated by the direct activation of large particles in a cyclotron beam (^3He, 35 MeV), in the Positron Imaging Centre at the University of Birmingham. These larger particles were then broken and sized to isolate small active particles when required. The behaviour of the valuable and gangue particles in the first two turns of the spiral is presented. The formation and interaction of different bands of similar size/density particles is shown. For small particles, these bands are less defined and can be present at different radial positions on the trough for the same size and density material. Their formation and dispersion is influenced by the flow of the slurry. Part of the large dense hematite particles are shown concentrating toward the inside of the spiral...
trough while some others are shown remaining in the high flow-speed outer zone outside of a band of large quartz particles. The behaviour in the feed device and first 0.3 turn of the spiral is related to the later separation of some of the large particles and this highlights the effect of the feed radial distribution of the particles on the trough.

Keywords
Gravity separation; spiral concentrator; iron ore; positron emission particle tracking; modular positron detector; direct activation;

1. Introduction
Many industries process powders, often mixed with liquid to form a slurry, in their product manufacturing cycle. Mineral processing is one of the important sectors where large scale processing of such mixtures takes place. One such example is the iron ore sector, which involves separating large amounts of valuable iron minerals from gangue minerals. Plants processing those minerals treat many millions tons of ore every year, and most of the refinement and separation techniques used rely on bulk ore properties (density, size, magnetism) and wet processing.

Considering economies of scale, operators are interested in using simple yet cost effective devices. The spiral concentrator is one commonly used separator: it is gravity fed, with no moving parts, requires no power for the separation and produces throughput per floor space area of up to 40 t/h/m² when arranged in multiple start columns (Palmers and Vadeikis, 2010). Thus, improvements in recovery and grade by optimising of the design and operation of spirals is of interest, considering the volumes of ore processed.

Researchers have published work on recoveries, grades and partition curves for different spiral designs, feed characteristics and operation parameters, but only a few took an experimental look at particles and fluid flow dynamics (Atasoy and Spottiswood, 1995; Golab et al., 1996; Holland-Batt and Holtham, 1991; Holtham, 1990, 1992a, b; Loveday and Cilliers, 1994). These studies form the knowledge base of spiral separation theory. There is interest in improving the spiral design to improve the separation of particles that can be problematic, such as some fines particles (Ø<75 μm) not being separated or some large dense particles (Ø>1000 μm) reporting to tailings streams (Bazin et al., 2014; Hyma and Meech, 1989; Richards et al., 2000; Sadeghi et al., 2014; Tripathy and Rama Murthy, 2012).

Having measurement techniques that allow one to follow the path, display the velocity field or assess the residence time of particles is important in designing efficient process equipment. Particle tracking provides this information and can be used to build empirical models (Portillo et al., 2010) or simply to validate fundamental models as it shows the real motion of a particle or liquid inside a system. Applying particle tracking to mixtures of fluid and granular material can help validate computational fluid dynamics (CFD) and discrete element method (DEM) models (Jayasundara et al., 2011; Marigo et al., 2013). Furthermore, single particle tracking is an interesting way to provide knowledge about the separation mechanisms through direct visualisation.
Widely used particle tracking techniques include Laser Doppler Anemometry (LDA) (Darelius et al., 2007) and Particle Image Velocimetry (PIV) (Li and Hishida, 2009). These are optical techniques which rely on low particle concentrations and on transparent media and equipment. This is a limitation for investigating opaque media, mixtures with high particle concentrations or non-transparent systems. Computer-Automated Radioactive Particle Tracking (CARPT) (Rammohan et al., 2001), Magnetic Resonance Imaging (MRI) (Kawaguchi, 2010) and Positron Emission Particle Tracking (PEPT) (Parker et al., 1993) have made investigation of such systems possible.

Recent work (Boucher et al., 2014; Waters et al., 2012) has shown the potential of using PEPT to investigate spiral concentrators. These studies were limited by the configuration and location rate of the PEPT detector used (the University of Birmingham ADAC Forte Camera). This paper first aims to characterize the limits of the PEPT technique with the use of small, directly activated, tracers. Then, the paper presents the results obtained from tracking the motion of hematite and quartz particle over the first two turn of a spiral with a new modular PEPT detector configuration. The two particles size investigated were $\varnothing=1440$ μm and $\varnothing=58$ μm.

2. Theory
This section describes the basics of the spiral concentrator as well as the PEPT technique, which has been used to record the trajectories of tracer particles along the spiral trough.

2.1 Spiral concentrator
Spiral concentrators are used in the processing of ores composed of minerals with different densities. A unit is composed of a profiled channel swept helically around a central post creating a spiralling trough. Commonly used spirals have between three and seven turns, with a diameter between 0.4 and 1 m (Palmers and Vadeikis, 2010). The feed mixture is composed of ground ore mixed with water, forming a slurry that is gravity feed at the top of the trough. On its way to the bottom of the spiral, the denser particles will generally report inward while the less dense ones normally flow towards the outer part of the trough.

The slurry flow on the trough can be deconstructed into two flows: a primary flow going downward; and a secondary radial flow (Figure 1). This flow description is central to spiral separation theory (Gleeson, 1945). As the slurry film flows down the trough, the dense particles will settle faster and will be carried inward by the lower layer of the secondary flow, while the less-dense particles will stay on top of the dense materials and will then be carried outward by the top layer of the secondary flow (Sivamohan and Forssberg, 1985). This mechanism has been reported to take place mainly in the first three turns of the spiral (Holland-Batt, 1995). After this early separation, most of the water will be found towards the outer edge and a band of dense material with a solids content up to 70% w/w (Holtham, 1992a) will be found close to the centre post, ready to be removed by an intermediate recovering device or a splitter at the end of the trough.

Flow speed is trough design and operation dependent with reported values being in the range of 0.1 to 0.3 m/s radially across most of the trough, with a more rapid stream found towards the outermost point
of the trough. Here, speeds can reach up to 2.0 m/s with little variation in these values from turn to turn for the same trough design (Holtham, 1990, 1992b). Speed values are based on slurry stream flowrate sampling and slurry film thickness measurements.

2.2 Positron emission particle tracking

Positron emission particle tracking (PEPT) is a technique based on the localisation of a single particle labelled with a positron emitting radionuclide. The technique was developed at the University of Birmingham, UK (Hawkesworth et al., 1986; Parker et al., 1993) and has been described in detail by Leadbeater et al. (Leadbeater, 2009; Leadbeater et al., 2012). The advantage of PEPT, over other techniques, is that it enables one to record the position of a tracer inside an opaque and dense system as a function of time, therefore the trajectory in a slurry with high solids content can be determined. Tracking a tracer over a long period of time or over many recirculations enables one to average the behaviour of particles similar to the tracer, and show their typical motion.

Tracers can be produced via different methods: ion exchange; direct activation (as used in this study); or surface modification (Fan et al., 2006a, b). During the direct activation process, the particle is placed in a cyclotron beam, and some oxygen atoms from the surface layer are converted to $^{18}$F (Fan et al., 2006b) via the competing capture reactions (Buffler et al., 2010). Further decay of these radioisotopes (half-life of 110 min) occurs mostly by positron emission ($\beta^+$ decay). Each positron will annihilate upon contact with a nearby electron. This annihilation event produces two back-to-back ($180^\circ \pm 0.5^\circ$) gamma rays (511 keV each). Coincident detection of the two gamma photons by scintillation crystals in detectors arranged around the experimental setup enables the reconstruction of a Line of Response (LoR) that passes very close to the activated particle (Leadbeater et al., 2012).

Figure 2 shows a schematic of the detection of eight gamma photons creating four LoRs in space originating from the tracer particle. In this schematic, two buckets of four detector blocks are used; each block contains 64 scintillation crystals.
LoRs detected are grouped over short intervals of time (of the order of milliseconds). Each group of a fixed number of lines \((N)\) is then used to triangulate an approximate point of emission using a location algorithm which removes most of the corrupt lines detected and keeps only a fraction \((f)\) of the initial LoRs (Parker et al., 1993). This point of emission is considered to be the tracer location for this group of LoRs, therefore at the centre of this short time interval. Recording the tracer positions over time allows a number of parameters to be determined, including: the trajectory; velocity; and occupancy (related to residence time).

The PEPT technique has been applied to track particles in mixing vessels (Chiti et al., 2011; Guida et al., 2009; Guida et al., 2010; Pianko-Oprych et al., 2009) and fluidised beds (Laverman et al., 2012) as well as to other granular or slurry systems including lab-scale mineral flotation cells (Waters et al., 2008), grinding mills (Govender et al., 2013), pharmaceutical and food industry mixers (Marigo et al., 2013; Portillo et al., 2010; Rafiee et al., 2011).

One of the limitations of PEPT being used to investigate many other industrial processes is the minimum size of the tracer that can be activated to a sufficient degree for tracking. In direct activation, the amount of activity required for precise tracking is proportional to the cross sectional area of the activated particle. In this study, particle size is greatly reduced and the amount of activity was expected to be very low.

At the University of Birmingham (UK) and under optimal conditions, recording rates of a 1 mm tracer moving at 10 m/s are up to 1000 localisations per second with a precision of 0.5 mm (Leadbeater et al., 2012). These values were recorded with the ADAC Forte camera (Parker et al., 2002). With lower localisation rates due to sub optimal conditions, Cole et al. (2012) showed in the high performance PEPT Cape Town facility (Buffler et al., 2010), that it is possible to use the PEPT technique (with ion exchange activated tracers) to follow trajectories of particles down to a diameter of 50 μm ± 5 μm, moving at a velocity up to 2 m/s with a location error of approximately 2.6 mm.

Accurately tracking a representative tracer of this small size is the next challenge. This is of particular importance in processes where surface chemistry plays an important role, such as the separation of minerals through flotation or when the density of the particle is involved in the process as in gravity
separation of fine ores. A technique for coating the small tracer with bulk representative material is under development (Cole et al., 2014). The direct activation technique is, however, interesting for this small size as it allows a particle of the same composition as the bulk to be used as tracer.

On the detection system side, PEPT has developed to the point where modular detectors blocks can be used in different configurations (Leadbeater and Parker, 2011; Parker et al., 2009). This enables the study of systems of different shapes and size operated in a specific environment. These specifically designed modular assemblies give more flexibility in the tracking, but the characterisation of such setup is of great importance. One of the objectives of this work is to assess the performance of a specific modular detector assembly made of ECAT 951 detectors for tracking tracers between 53 and 63 μm in diameter.

3. Experimental

The modular tracking system was used to investigate the path of large (=1440 μm) and small (=58 μm) tracer particles inside an iron ore slurry processed in a spiral concentrators. As part of this investigation targeted very small particles, for which no assessment of the tracking system performance was available, the system was initially tested by tracking the path of small tracers under different conditions:

- Moving at a known trajectory (circular) and velocity in air.
- At rest in water.
- Freely moving in a water-filled, baffled container, stirred by a Rushton turbine.

These conditions were intended to provide a comparison between expected and recorded trajectory as well as the effect of tracer velocity and media attenuation (air or water) on the localisation rate and precision. Comparisons were made with the ADAC Forte camera performance. This section describes the detector setup, the experimental systems, the ore samples and tracers used.

3.1 Circular constrained motion setup

A planar circular motion was created by fixing a tracer particle to the edge of one of the six paddles of a standard Rushton impeller using carbon tape (shown in Figure 3). Rotation of the impeller was set at the desired speed using a digital mixer (Caframo, BDC 1850, Canada).

![Figure 3 - Schematic of the Rushton impeller holding the tracer with dimension in mm.](image-url)
With this setup, the tracer follows a circular trajectory in the \(zx\) plane and the expected location over time can be assumed to be a sinusoid in the \(x\) axis and another sinusoid in the \(z\) axis. In the \(y\) axis, the expected location should be constant over time, provided that the plane of rotation is perpendicular to the axis.

### 3.2 Determination of the location error

The different cases investigated can be characterised by a location error when the trajectory of the tracer is constrained (Volkwyn et al., 2011). For a set of data, this error is calculated using the root mean square error (RMSE) technique shown in Equation 1 for the \(x\) axis. The error \((\Delta x_i, \Delta y_i, \Delta z_i)\) on each location is the difference between the PEPT located position and the expected position with \(n\) being the number of locations used. The expected position is determined by fitting the best sinusoid to the located position, starting with an approximate knowledge of the parameters based on rotational speed and impeller dimensions. The RMSE was determined by using the MATLAB® Curve Fitting Toolbox™ (The MathWorks Inc.).

\[
RMSE_x = \sqrt{\frac{\sum_i^n (\Delta x_i)^2}{n}}
\]  

(1)

### 3.3 Determination of tracer velocity

The velocity of the tracer at a location was calculated by using the five previous, the actual, and the five next locations of the tracer with regards to the time for each of these locations and weighting factors (Stewart et al., 2001). This method has the effect of smoothing the velocity and reducing the effect of the tracer localisation error (Leadbeater et al., 2012). This method must be used carefully when tracking a tracer moving in and out of the field of view of the camera, or at a very low location rates (low tracer activity) as the previous and next locations can be non representative of the tracer motion over a short timeframe.

### 3.4 Mixing vessel setup

A two litre cylindrical glass beaker (Kimble Chase, Model 14000-2000) was used as the container. Four baffles made from sheet metal were held inside the beaker by two sheet metal rings. Mixing was provided by the impeller and mixer described in Section 3.1. The volume of water used was 1200 ml. The schematic and dimensions of the container and impeller are shown in Figure 4. The tracer was added directly into the water of the vessel without mixing for tracking at rest and then the mixer speed was set at 400 rpm.
3.6 Modular detector assembly setup

Before assembling a modular detector geometry, simulations of the detection area (Figure 5) were created to assess the sensitivity and uniformity of the field of view (Leadbeater and Parker, 2013). These simulations were used for analysing different detector block configurations. Finally, twelve modular buckets of four ECAT951 detector blocks were arranged in a two layer circular pattern (Figure 6a). For each ring, six buckets were placed every 60° with a clearance diameter of 400 mm (required based on the spiral trough diameter) with a field of view thickness of 100 mm. This modular assembly was also used to track a small tracer inside the mixing vessel as shown in Figure 6b.

Figure 5 - Simulation showing a) xz and b) xy view of the modular assembly field of view sensitivity (Leadbeater and Parker, 2013).
3.7 Spiral setup and detectors arrangement
The spiral used was a Walkabout assembly (Wallaby trough) from Mineral Technologies with four turns, a pitch of 200 mm and a trough diameter of 360 mm. Figure 7 shows the circuit used. The slurry was mixed in a tank and pumped through a diaphragm pump to a funnel (for pulse damping) connected to the feed device at the top of the spiral trough. At the end of the trough, concentrate and tailings discharged into the tank for remixing and recirculation.

The modular detector assembly was positioned at different heights around the spiral to track different 100 mm thick slices of the trough. The four trough slices tracked can be seen in Figure 8 (Slice A was tracked only for the small tracers). Tracking runs were carried out for each size and mineral at the
specific position before moving the assembly vertically downward to the next slice. The 100 mm thick field of view was set to an angle of 10.5 degrees (same as the trough edge descent angle) to provide more tracking than just half a turn (pitch of 200 mm). The results of this arrangement is a tracking of about 0.3 of a turn for Slice A and C and about 0.7 of a turn for Slice B and D. The spiral with the modular assembly around is shown in Figure 9.

![Spiral concentrator inside the modular assembly](image)

**Figure 9 - Spiral concentrator inside the modular assembly**

3.8 Ore and spiral operation parameters

A bulk sample of iron ore from the Mount-Wright Mine in the Labrador Trough (Canada) was used to prepare representative samples for the different spiral tests. The ore was sieved to remove the fraction larger than 850 μm (initially 7% of the total) to ease recovery of the large tracer at the end of each test run, and to reduce blockage of the pump. The size distribution of the samples is given in Table 1 while the solids composition and spiral operating parameters are presented in Table 2.
Table 1 - Ore size distribution

<table>
<thead>
<tr>
<th>Size fraction (μm)</th>
<th>Content (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>850 - 1180</td>
<td>0.1</td>
</tr>
<tr>
<td>600 - 850</td>
<td>7.1</td>
</tr>
<tr>
<td>425 - 600</td>
<td>9.8</td>
</tr>
<tr>
<td>300 - 425</td>
<td>13.9</td>
</tr>
<tr>
<td>212 - 300</td>
<td>15.0</td>
</tr>
<tr>
<td>150 - 212</td>
<td>13.8</td>
</tr>
<tr>
<td>106 - 150</td>
<td>10.7</td>
</tr>
<tr>
<td>75 - 106</td>
<td>8.0</td>
</tr>
<tr>
<td>53 - 75</td>
<td>5.1</td>
</tr>
<tr>
<td>38 - 53</td>
<td>5.7</td>
</tr>
<tr>
<td>0 - 38</td>
<td>11.0</td>
</tr>
</tbody>
</table>

Table 2 - Solids composition and slurry feed parameters

<table>
<thead>
<tr>
<th>Solids</th>
<th>56.6 %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quartz</td>
<td></td>
</tr>
<tr>
<td>Hematite</td>
<td>43.2 %</td>
</tr>
<tr>
<td>Other minerals</td>
<td>0.2 %</td>
</tr>
<tr>
<td>Slurry solids content</td>
<td>20 % w/w</td>
</tr>
<tr>
<td>Slurry feed rate</td>
<td>0.9 tph</td>
</tr>
</tbody>
</table>

3.9 Tracer preparation

For the modular detector assembly characterisation and comparison with the ADAC Forte, quartz particles with a specific gravity (S.G.) of 2.65 from Unimin (USA) were used as the irradiated tracers. This mineral (SiO₂) is prone to direct activation by the ³He cyclotron beam and is of interest as it is found in many mineral formations, including iron ore deposits. For the spiral experimentation, the tracers were created by the direct activation of hematite (Fe₂O₃, S.G.=5.26) and quartz particles selected from a raw ore sample (the test ore), hence directly mimicking real particles.

The activation of 3-4 large particles (Ø=1440 μm) of the same material was performed at the same time in the 35 MeV ³He cyclotron beam at the University of Birmingham, UK. Activity levels attained by the large particles were measured with an ionisation chamber (Capintec CRC-25PET) and are reported in Table 3 for the modular assembly characterisation and Table 4 for the spiral investigation.

In the case where a submillimetre sized tracer (Ø=58 μm) was required, the large particle with the highest activity was broken into smaller pieces. A rubbing action breakage (attrition by gyratory action) of the large particle was conducted using a brass hammer (100 g) and anvil (500 g). This method provided smaller particles originating from the surface of the initial particle. This surface material has a minimal radioactivity level for tracking as it is a particle’s surface which is bombarded by the cyclotron beam (Fan et al., 2006b). The other large activated particles were stored for later use or as a backup.

The products of the breakage were sieved and the particles of the desired size (53<Ø<63 μm) were isolated. An artist's brush with a single remaining hair was then used to pick-up the small tracers under
the field of view of an optical microscope. Measurement of the activity of the small particles was carried out to select one with the larger activity for use in the small particle investigation.

For these smaller particles, the activation levels shown in Table 3 and Table 4 were very low and were measured in counts per second (cps) using a contamination monitor (Tracerco T401). The probe of this device is flat (pancake style), the value measured is thus only based on the gamma rays hitting the probe and not on the whole particle activity and disintegration rate, hence providing a relative comparison of the activity for the small particle selection. Activity values for the small particles shall then be taken relatively as no efficient way of measuring it was available.

Once isolated, the tracers were either individually stuck to double sided carbon tape piece for the fixed motion experiment; directly inserted into the water of the vessel; or added to the slurry in the spiral setup.

The remaining particles which were too small, too large or with too low an activity were disposed of accordingly.

This method of creating small tracers has some advantages as it provides a particle similar (surface properties, density) to the particles forming the bulk material to be investigated. However, a large number of small particles are created by the breakage, but only few of them are used, considering that tracking is conducted on one tracer at the time and that the $^{18}$F short half-life limits the number of consecutive experiments possible for each initial activation.

### Table 3 - Initial activity of the quartz particles used as tracers for setup characterisation

<table>
<thead>
<tr>
<th>Particles details</th>
<th>Size (μm)</th>
<th>Initial activity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>ADAC Forte experiment</td>
</tr>
<tr>
<td>Before breakage</td>
<td>1180 to 1700*</td>
<td>30 to 52 MBq</td>
</tr>
<tr>
<td>Tracer for constrained motion experiment in air</td>
<td>53 to 63**</td>
<td>2600 cps</td>
</tr>
<tr>
<td>Tracer for still and free motion experiment in water</td>
<td>53 to 63**</td>
<td>3700 cps</td>
</tr>
</tbody>
</table>

*Activity measured with a Capintec CRC-25PET
**Activity measured with a Tracerco T401

### Table 4 - Tracers material, size and initial activity for spiral investigation

<table>
<thead>
<tr>
<th>Size (μm)</th>
<th>Activity</th>
<th>Slice</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Quartz</td>
<td>Hematite</td>
</tr>
<tr>
<td>1180 to 1700*</td>
<td>Not tracked</td>
<td>Not tracked</td>
</tr>
<tr>
<td>16.1 MBq</td>
<td>18.3 MBq</td>
<td>B</td>
</tr>
<tr>
<td>12.7 MBq</td>
<td>22.5 MBq</td>
<td>C</td>
</tr>
<tr>
<td>1500 cps</td>
<td>200 cps</td>
<td>A</td>
</tr>
<tr>
<td>2000 cps</td>
<td>1000 cps</td>
<td>B</td>
</tr>
<tr>
<td>1700 cps</td>
<td>1200 cps</td>
<td>C</td>
</tr>
<tr>
<td>1800 cps</td>
<td>2500 cps</td>
<td>D</td>
</tr>
</tbody>
</table>

*Activity measured with a Capintec CRC-25PET
**Activity measured with a Tracerco T401
For the spiral setup, a data recording run starts with the tracking of the small tracer inside the slurry. After approximately one hour of slurry recirculation on the trough, the decay of this small tracer reduced the activity to the point where tracking was no longer possible. At this moment, one of the remaining large activated particles was added to the slurry. This large tracer still had a high activity and was thus able to be tracked. After about 30 min of data recording with this tracer, the pump was stopped, the large tracer recovered for disposal and the system cleaned. A new slurry was prepared for each tracer activation run to prevent contamination of the ore.

4. Results and discussion
The expected and true position of the tracer were analysed for the tracer on the impeller and the tracer at rest in water. Details about the mixing vessel free motion and the tracking inside the spiral concentrator are then given.

4.1 Algorithm parameter optimisation and location precision with constrained trajectory
The selection of the parameters \((N \text{ and } f, \text{ see Section 2.2})\) used in the tracking algorithm can be optimised to reduce the root mean square error (RMSE). To do so, the RMSE values of 30 s samples of recording the small tracer attached to the impeller rotating in air (constrained circular trajectory) were calculated with different parameters. Different velocities were tracked for both setups. The rotational speed of the impeller carrying a \(\varnothing \approx 58 \mu\text{m}\) tracer was initially set at 150 rpm then decreased to 75 rpm and finally 15 rpm. Each speed was run for approximately 15 minutes.

Figure 10 presents the different RMSE based on different \(N\) and \(f\) values for 150 rpm. Figure 11 shows the mean location frequency associated with Figure 10. This type of graph was used to determine the best parameters. In this case (150 rpm), the tracer velocity was 27.6 cm/s for the ADAC setup and 37.7 cm/s for the modular assembly. This difference is caused by the tracer being further out on the impeller in the case of the modular setup. For any case when the location frequency was below three points per rotation (e.g. below 7.5 Hz for 150 rpm), the RMSE was not further analysed. Therefore the errors obtained are of interest for trajectories of a radius of curvature equal to or larger than that of the impeller (\(\geq 25 \text{ mm}\)). Smaller curvatures will be missed by the low location frequency.
Figure 10 - RMSE of the locations for the a) x axis b) y axis and c) z axis.
Table 5 provides the $N$ and $f$ values minimising the RMSE for the different cases investigated. For both tracking systems, the final parameters selected were also influenced by the higher location rate provided by a lower value of $N$, considering the low raw data rate experienced (especially with the ADAC Forte which is 5 to 10 time smaller than the modular assembly). Table 6 provides speeds and RMSE for the two setups for the different rotational speeds.

Table 5 - Optimal $N$ and $f$ parameters for the constrained rotational motion of the $\varnothing=58$ µm quartz tracer.

<table>
<thead>
<tr>
<th>Tracking system</th>
<th>Rotational speed (rpm)</th>
<th>Speed (cm/s)</th>
<th>Activity (cps)</th>
<th>Raw data rate (kHz)</th>
<th>$N$</th>
<th>$f$ (%)</th>
<th>Mean Location Frequency (Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADAC Forte</td>
<td>150</td>
<td>27.6</td>
<td>2600</td>
<td>2</td>
<td>25</td>
<td>50</td>
<td>12.4</td>
</tr>
<tr>
<td></td>
<td>75</td>
<td>13.8</td>
<td>2300</td>
<td>2</td>
<td>50</td>
<td>40</td>
<td>5.6</td>
</tr>
<tr>
<td></td>
<td>15</td>
<td>2.8</td>
<td>2100</td>
<td>1</td>
<td>150</td>
<td>30</td>
<td>1.5</td>
</tr>
<tr>
<td>Modular assembly</td>
<td>150</td>
<td>37.7</td>
<td>850</td>
<td>10</td>
<td>150</td>
<td>40</td>
<td>10.0</td>
</tr>
<tr>
<td></td>
<td>75</td>
<td>18.9</td>
<td>710</td>
<td>10</td>
<td>150</td>
<td>60</td>
<td>8.6</td>
</tr>
<tr>
<td></td>
<td>15</td>
<td>3.8</td>
<td>620</td>
<td>9</td>
<td>150</td>
<td>60</td>
<td>7.3</td>
</tr>
</tbody>
</table>

Table 6 - Precision of the localisation for the directly activated quartz tracers of size $\varnothing=58$ µm in a constrained circular trajectory

<table>
<thead>
<tr>
<th>Setup</th>
<th>Rotational speed (rpm)</th>
<th>Speed (cm/s)</th>
<th>RMSE x axis (mm)</th>
<th>RMSE y axis (mm)</th>
<th>RMSE z axis (mm)</th>
<th>RMSE 3D (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADAC Forte</td>
<td>150</td>
<td>27.6</td>
<td>2.0</td>
<td>1.7</td>
<td>2.8</td>
<td>3.8</td>
</tr>
<tr>
<td></td>
<td>75</td>
<td>13.8</td>
<td>1.6</td>
<td>1.2</td>
<td>2.1</td>
<td>2.9</td>
</tr>
<tr>
<td></td>
<td>15</td>
<td>2.8</td>
<td>1.2</td>
<td>0.5</td>
<td>1.2</td>
<td>1.8</td>
</tr>
<tr>
<td>Modular detector assembly</td>
<td>150</td>
<td>37.7</td>
<td>2.2</td>
<td>0.5</td>
<td>2.5</td>
<td>3.4</td>
</tr>
<tr>
<td></td>
<td>75</td>
<td>18.9</td>
<td>1.3</td>
<td>0.4</td>
<td>1.3</td>
<td>1.9</td>
</tr>
<tr>
<td></td>
<td>15</td>
<td>3.8</td>
<td>1.2</td>
<td>0.3</td>
<td>1.0</td>
<td>1.6</td>
</tr>
</tbody>
</table>

For each tracking system, the faster that the tracer was moving, the greater the location error (Table 6). This is explained by the lower number of LoRs recorded for a specific travelled distance.

Even at higher speeds, the tracking with the modular assembly is of a better quality and with a higher location frequency. This is mostly due to a greater raw data collection rate (more LoRs detected)
achievable with the ECAT951 detector blocks, which have a higher intrinsic efficiency for detecting 511 keV gamma photons compared to the ADAC Forte detectors. Another point of interest shown in Figure 10, is that the RMSE, is always larger than RMSE, and RMSE, for the ADAC Forte. This is caused by the lack of angular sampling in the z direction due to the detectors' configuration (parallel to the xy plane) in the ADAC camera (Parker et al., 1993).

Figure 12 shows the locations of the tracer and the sinusoid representing the expected trajectory for samples of five seconds while the impeller rotates at 75 and 150 rpm. It can be seen that even if the location rate is small (Table 5) the locations are sufficient to display a trajectory with a radius similar to that of the impeller.

![Figure 12](image)

**Figure 12** - x position of the Ø=58 µm quartz tracer affixed to the impeller and the sinusoid representing the expected trajectory for the ADAC Forte and the modular detector assembly.

### 4.2 Tracking of a small tracer at rest in water

To assess the resolution and the error of the localisation in water for both setups, a free tracer was tracked while lying on the bottom of the vessel filled with water before the impeller rotation was started. Table 7 provides the location rate and RMSE for the tracers lying in the water filled vessel. Figure 13 shows an example of the tracers position in time with the expected (least RMSE) position.
Table 7 - Precision of the localisation achieved for a directly activated quartz tracer of size $\Phi \approx 58$ µm at rest in a water filled vessel

<table>
<thead>
<tr>
<th>Setup</th>
<th>Activity (cps)</th>
<th>Raw data rate (kHz)</th>
<th>Location rate (Hz)</th>
<th>RMSE$_x$ (mm)</th>
<th>RMSE$_y$ (mm)</th>
<th>RMSE$_z$ (mm)</th>
<th>RMSE 3D (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADAC Forte</td>
<td>3200</td>
<td>1</td>
<td>6.0</td>
<td>1.5</td>
<td>1.6</td>
<td>3.1</td>
<td>3.8</td>
</tr>
<tr>
<td>Modular assembly</td>
<td>2400</td>
<td>9</td>
<td>2.0</td>
<td>1.9</td>
<td>1.5</td>
<td>2.4</td>
<td>3.4</td>
</tr>
</tbody>
</table>

Figure 13 - Tracer location while at rest on the bottom of the Rushton turbine with the expected location and RMSE for a) the ADAC Forte and b) the modular assembly.

For this case, the tracking provided by the modular assembly is slightly more accurate than the ADAC Forte with a smaller RMSE, except for the x axis. The location rate was lower for the modular assembly and a better tracking was expected based on the information in Table 6. It is worthwhile to mention that the activity of the small tracer for the ADAC Forte had a higher initial activity than the one for the modular setup as seen in Table 3. But more importantly, the tracer was lying on the bottom of the vessel.
hence very close to the lower limit of the detection field of view of the modular setup where sensitivity is lower (shown in Figure 5), this is a potential explanation for this low rate.

4.3 Tracking of a free moving tracer in a vessel stirred by a Rushton turbine
The vessel was then stirred by rotation of the Rushton turbine at 400 rpm (1.02 m/s impeller tip speed). Figure 14 shows a 2.7 s sample of the trajectory recorded with the modular assembly where the tracer makes two loops in the current under the impeller. It can be seen that the distance between locations is greater when the tracer travels through the impeller rotation zone where the tracer speed is higher. The location rate (with \(N=30, f=30\)) was between 20 and 30 Hz over the duration of the experiment. Figure 15 shows the speed of the \(\varnothing=58\) µm tracer for the trajectory sample of Figure 14, with values in the same range as the motion characterised in Section 4.1. In the case of the ADAC Forte, the location rate was not sufficient to determine a trajectory.

![Figure 14 - Trajectory of the tracer (\(\varnothing=58\)) doing two loops in the current under the Rushton turbine.](image)

![Figure 15 - Speed of the tracer for the trajectory of Figure 14.](image)

4.4 Tracking of a particle in a spiral concentrator
As the slurry containing a single tracer was pumped inside the spiral recirculating circuit of Figure 7, the tracer passed through the ring of detectors on numerous occasions. Each pass then represents a particle of the size and density of the tracer being processed in the spiral. By observing the top view (plan xz in Figure 16 and following) of the tracer trajectory, it can be seen where it entered the detector field of
view and where it exited with the location of the particle at different points along the trajectory observed.

Quartz tracers (Ø≈58 µm) were tracked flowing on the trough with the ADAC Forte (Boucher et al., 2014) and the modular setup. Figure 16 shows a comparison of the results from the two systems for a 100 mm horizontal slice of the spiral. Compared to the ADAC Forte, a clear improvement in location frequency can be seen with the modular assembly, thus providing a more detailed trajectory (especially closer to the centre post).

![Figure 16 - Comparison of the performance for tracking a quartz tracer (Ø≈58 µm) with the a) ADAC Forte and b) modular assembly for a 100 mm horizontal slice of a spiral concentrator processing a slurry with 20% solids by mass.](image)

Further tests were conducted with the modular setup and focussed on the tracers' behaviour for two different particle sizes (Ø=1440 µm and Ø≈58 µm) and two densities (hematite S.G.=5.26 and quartz S.G.=2.65). Larger tracers with higher activity will produce more location points, and small tracers provide just enough locations to follow their general path.

4.4.1 Hematite particle of diameter of 1440 µm

Figure 17 shows the three slices (B, C and D) tracked independently for the large hematite tracer where it is possible to see the combination of the many location points forming trajectories. Five passes out of 34 were within the middle zone when entering Slice B, the remaining being very close to or in the outer zone. An interesting behaviour to note is that the different passes of the large dense tracer rapidly split in two bands. One band is toward the inside of the trough, as expected. The second is formed of passes that do not show any concentrating behaviour from entrance of Slice B through the exit of Slice D. The loss of large dense particles to the outer zone of the trough has been reported to be influenced by the use of wash water (Sadeghi et al., 2014), but here no wash water was used such that another mechanism must be involved.
Another interesting behaviour is the fast inward migration of some passes starting on the outer zone limits of Slice B. This fast migration take place where there is a wave inflation (visual observation) in the slurry created by the flow climbing along the edge of the trough profile and coming back towards the inside. This might initiate the secondary circulation (upper flow layer moving outwards and lower flow layer moving inwards) in this small section of the trough which can explain why the large settling particle is carried inward. This phenomenon is caused by the initial direction of the flow at the exit of the feeding device. At the exit of Slice B, some trajectories show migration toward the outer zone, but this is caused by the whole flow direction that has not yet stabilised radially and this material is seen coming back toward the centre in Slice C, while Slice D show more circular trajectories with constant radius (no concentration). For all of the passes, migration of the large hematite seems to be stabilized by the end of Slice C (approximately 1.3 turns).
Figure 17 - Combination of the passes of the hematite tracer ($\varnothing \approx 1440 \, \mu\text{m}$) for Slice B, C, and D tracked independently.
4.4.2 Quartz particle of diameter of 1440 μm

Figure 18 shows the same slices (B, C, D) as Figure 17, but for the large quartz tracer runs. Looking at the quartz entrance in Slice B, there is already a difference compared to the hematite tracer behaviour: 40 out of the 41 passes entered Slice B in the outer zone or very close to this region. This indicates that there was already a slight selectivity in the first 0.3 turn of the trough (Slice A, not tracked for this size). The same wave inflation effect on the slurry as with the hematite is seen with quartz in Slice B where some passes suddenly migrate inwards. The trajectories then stay dispersed on the middle and outer zone up to the end of slice C where they form a more concentrated band in the middle zone.

Later down the trough, the trajectories of the large quartz tracer in Slice D was found to be located between the two bands of the hematite tracer of Figure 17. This shows that the large quartz and hematite is differentiated by the spiral even after 1.3 turn (entrance Slice D). But it appears that some of the large hematite is trapped outside of a material band carrying the large quartz tracer. Another explanation is that some large particles are trapped in the high flow rate dilute water at the outside as some passes of the large quartz and hematite tracers are in the outer zone for the three slices tracked with no indication of radial movement (toward inside or outside).
Figure 18 - Combination of the passes of the quartz tracer ($\phi = 1440 \, \mu m$) for Slice B, C and D tracked independently.
4.4.3 Effect of initial radial position of the feed on large particles trajectories

Another way of analyzing particles separation is by looking at the initial and final positions across the trough for each independent trajectory. Figure 19 and Figure 20 shows, for Slice B and D respectively, the radial position of every large tracer trajectories entry coupled with the radial position of their exit location.

![Figure 19](image1.png)

**Figure 19** - Influence of entry radial position on exit radial position for hematite and quartz tracers (Ø = 1440 μm) in Slice B.

![Figure 20](image2.png)

**Figure 20** - Influence of entry radial position on exit radial position for hematite and quartz tracers (Ø = 1440 μm) in Slice D.

For this trough design and operating parameters, the selectivity seem to take place at a very early point on the trough, in the first 0.3 turn of the spiral. Trajectories of the large tracers entering in Slice B outside of ≈125 mm in radius all exit the slice in the outside and if they enter inside of ≈125 mm radius, they all exit inside. Based on Figure 17 and Figure 18 it is possible to say that this early selection is unlikely to reverse further down the spiral (Slice C and D), especially for the large hematite tracers. This
behaviour shows the high importance of the feeding device design and the particles radial distribution at the exit of such device (the inner zone being the target to prevent the loss of the large dense particle). In the case of the large quartz tracer, many trajectories are seen to come closer to the inner band of the hematite tracer at the exit of Slice D (Figure 20). This is related to the non circular flow pattern seen at the exit of Slice C (Figure 18) where trajectories tend toward the inside.

4.4.4 Hematite particle of diameter of 58 μm
The tracking of small particles (Ø=58 μm) is more difficult due to their lower activity resulting in fewer positron emissions and annihilations. Trajectories are thus less accurate than the large tracers considering the lower number of LoRs detected and resultant location points. Even so, the high recording rate of the modular detectors' assembly generated enough data to show the small tracers' general trajectories (with N=30 and f=30). For the small hematite particles, the slices tracked (A, B, C and D) are shown in Figure 21.
As the location rate is in part related to the speed of the tracer, the outer zone trajectories have a lower quality for this particle size. The trajectories should be looked at as the combination of points for a pass rather than taking every point as the exact location of the tracer.

Slice A and B show fewer trajectories, 10 and 6 respectively and the lower activity of the tracer might be the cause of this, highlighting one difficulty of the direct activation and breaking technique: finding small particles and effectively measuring their activity to select one with high activity.

Slice A does not show any particular behaviour other than that the tracer became very slow for a few moments at the inside limit of the slurry film at the exit of the feeding device, probably sticking to the
trough rubber surface. In Slice B, the tracer reports solely to the middle zone, but considering the low number of passes for this slice, this is somewhat inconclusive. Slice C shows that the tracer is carried in two principal bands with few passes in the high speed outer zone. Those bands seem to merge at the exit of Slice C. In Slice D, the tracers’ trajectories initially dispersed split into different bands with most of the passes in the middle zone, but close to the inner zone limits. This show a slight concentration of this fine sized dense hematite at the end of the second turn.

4.4.5 Quartz particle of diameter of 58 μm
Spiral concentrators are generally less efficient for separating particles smaller than 75 μm and as expected Figure 22 show only a small difference in behaviour for the small quartz tracer compared to that of the hematite tracer (Figure 21).

Figure 22 - Combination of the passes of the quartz tracer (Ø ≈ 58 μm) for Slice A, B, C and D.
Slice A shows that the tracer was mostly fed into the outer zone where the flow climbs up the edge part of the trough profile shortly after entering. Slice B shows the same inward motion as the large tracers for trajectories entering the slice at the outer limit of the middle zone. This may be due to the small tracer just being carried in by the flow of water before the flow attains radial stabilisation. Surprisingly, many trajectories are found in the inner part of the trough at the end of Slice B, but they are dispersed in Slice C. This dispersion may be related to the temporary outward flow motion shown by the large tracer (end of Slice B of Figure 17 and Figure 18). In this case, this natural dispersion of the inner trajectories of Slice B would be beneficial for the hematite concentration as the small quartz is now more outward in Slice D.

In Slice D, the slightly lower density of the trajectories in the middle zone shows that the passes are more located inside or outside of the hematite trajectories of Slice D in Figure 21. This behaviour indicate that bands of similar size and density particle form on the trough. These bands can split and recombine under the effect of the overall flow behaviour.

5. Conclusions

A specially assembled modular positron emission particle tracking setup made of 12 ECAT951 detectors has been used to track large (Ø≈1440 µm) and small (Ø≈58 µm) particles of quartz and hematite. The small tracers were created by breakage and sizing of a directly activated large particle. RMSE performance in the order of 2.2 mm in x, 0.5 mm in y and 2.5 mm in z for velocities up to 37.7 cm/s with a resolution of 10 Hz was achieved for the tracking of the small particle with the modular assembly. This is an interesting improvement in location rate and slightly better in spatial resolution (even for higher velocity) compared to the ADAC Forte positron camera RMSE performance of 2.0 mm in x, 1.7 mm in y and 2.8 mm in z for a tracer particle moving at velocities up to 27.6 cm/s with a location rate of 12.4 Hz for a similar tracer. These results provide information about the capabilities of the modular detector assembly for tracking tracer particles of small size moving at low speed in granular and slurry processing systems. The low activity of the small tracer can results in very low location rate and poor trajectory quality which is also dependent on the tracer speed. Improvements in activation to a certain extend or detection of lower activity levels as well as improvement in measurement of the small particle activity are of interest to improve the applicability of the direct activation and breakage technique central to investigation of surface or density related process.

With the modular detectors system, iron ore representative tracers trajectories inside the first two turns of a spiral concentrator have been shown for the first time. The separation of the particles in different radial bands has been shown and some effects present are related to the primary and secondary flow separation theory, while others are related to the feeding process and trough design.

In the case of the large dense particle reporting to the outer zone of the trough, it appears that the radial feed position and the first 0.3 turn into the trough is important. Based on the combination of slices presented, it is highly improbable that large dense particles having an early outward radial position (outer 30% of the trough radius) will ever come to the inside of the trough. This will lead them to being discarded via the outer tailings port at the bottom of the spiral.
For the small tracer trajectories recorded, it has been shown that concentration is present in the first two turns, but to a much smaller extent. The important observation for this size is the creation and dispersion of less defined material bands. These bands seem to be affected by the flow of water and other size class as some fine quartz bands have been seen in the inner zone, event thought the quartz density is low.

Finally, it is possible to say that the concentration on the spiral is not a constant process taking place all the way down the spiral, but rather something occurring in specific sections with flow effects that are different depending on the particle's size and density. Tracking other intermediate size fractions could provide more information about the interaction between the different bands of material and how the primary and secondary flows affect the separation; as well as the magnitude that each of them are present along the trough.

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References


**Highlights:**

- Activation and further breakage of 1440 μm mineral particles provides tracers of 58 μm.
- A new PEPT detector assembly is presented and compared to a reference system.
- 3D root mean square location errors are in the order of 3.4 mm for 58 μm tracer.
- 58 and 1440 μm quartz and hematite particles are tracked in a spiral concentrator.
- Initial radial position of large particle influence concentration.