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Mode shape curvature squares method for crack detection in railway pre-stressed concrete sleepers

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This unprecedented study aims to demonstrate the potential to locate crack damage in full-scale railway pre-stressed concrete sleepers. The dynamic mode shape curvature squares method has been utilised. This approach adopts structural deflection shapes extracted from experimental modal analysis using an impact excitation. The railway concrete sleepers are exposed to the first crack and 1.5 times above the first-crack loads using experimental setup in accordance with the British Standard. It is found that the first cracking of the sleepers has caused non-significant stiffness reduction of the structural component evidenced from the fact that the natural frequency shifts are only few percent and no visible differences in deflection mode shapes are observed. In addition, the mode shape curvature alone cannot indicate the crack establishment in the railway sleepers. However, a relatively sparse wireframe for deflection shapes enable the plausible density of sensor grids that can be further analysed for damage detection. In this paper, the curvature square approach has been developed to quantify and locate the damage in the railway sleepers. The standardized damage index distributions and subsequent thresholding with different levels of confidence of damage localization have been firstly developed to enhance the accuracy of crack localization. It is found that accurate locations of cracks mostly in the mid span of the sleepers can be reasonably detected in accordance with the actual crack measurements from the experimental data. The insight into this approach can enhance the development of on-board technology for railway sleeper crack detection using operational modal signals.

Keywords: concrete sleeper; crack detection; deflection shape; curvature; damage index; modal analysis

Highlights

- Dynamic mode shapes of cracked railway concrete sleepers are extracted.
- Mode shape curvature square method is used to identify cracks in railway sleepers.
- Polynomial smoothing of mode shape curvature eliminates the need for baseline data.
- Initial and further cracks in railway concrete sleepers are accurately detected.

1. Introduction

Sleeper is a critical component of railway track. The main functions of the sleepers include transferring load from the rails to the ballast and the underlying substructure, securing track gauge during train traffics and preventing movement of the track in longitudinal and lateral directions ensuring a comfortable ride for the train passengers [1]. Such an important component of railway infrastructure as sleeper has to be maintained properly in order to avoid accidents, for example, train derailments, etc. Two main causes of failure of the concrete sleepers are the tensile cracking and compressive crushing of the concrete [2]. The flexural capacity of railway concrete sleepers can be assessed through the measurement of bending moment. For this purpose, in [3] authors equipped concrete sleepers with strain gauge sensors in order to measure the sleeper-to-sleeper bending moment variability. They found out that the value is between 0 kNm and 22.8 kNm. Authors in [4] used numerical simulations to assess crack propagation in pre-stressed concrete sleepers. They found that flexural performance of the sleepers is mostly influenced by the crack length rather than width. Moreover, the first cracks usually appear in the centre position of the sleepers.

Innovative solution to minimizing probability of railway sleeper failure was proposed in [5] consisting of embedding insulated rail joints into concrete sleepers themselves and further optimizing

the design. Long-term solution to this problem, however, would be adaptation of a structural health monitoring concept, widely applied to bridges, high rise buildings and other structures. Acoustic emission is a promising technique that is plausible for evaluation of crack location and severities by examining and post-processing acoustic emission signatures, as demonstrated in [6], while flexural capacity of pre-stressed concrete using electromechanical impedance spectroscopy was reliably assessed in [7].

One of the most well-established vibration-based structural health monitoring techniques is based on mode shape curvatures (MSC). Numerous studies exist where this methodology with slight modifications was adopted to successfully indicate the damage in various types of structures, ranging from composite plates, concrete beams to wind turbines and bridges. The success of MSC and related methods is mainly attributed to the fact that, first of all, it is easy to implement, since only modal analysis or operational modal analysis with natural excitation has to be performed and mode shapes extracted. Secondly, once extracted, mode shapes and their transformations provide a valuable spatial information about the structural condition as opposed to examination of resonance frequency shifts when only the fact of existence of damage can be either confirmed or declined.

Vast number of studies exist on damage localization using MSC methods. In [8] MSC was applied to locate the damage in wind turbine blades. Modal analysis was carried out to extract natural frequencies, damping and mode shapes of healthy and damaged blades. The curvature of difference between mode shapes at healthy and damaged states was computed as a distribution over blade for 3 damage scenarios. This approach managed to locate the damage in all cases. A hybrid damage detection procedure for thick conical shells using both wavelet finite element and mode shape curvature is proposed in [9]. The algorithm involved the detection of damage by calculating the difference of curvature of mode shapes between healthy and damaged structures and estimation of damage severity by constructing a wavelet finite element and solving for natural frequencies for different damage severities (achieved by reducing the thickness of finite elements in numerical simulation model). The damage localization procedure introduced in [10] is based only on the information of damaged structure. Operational deflection shapes of beam and plate structures are obtained using an operational modal analysis with a passing vehicle. Global Filtering of operational shape curvature (calculated by central difference) yielded damage localization which is sensitive to small damage and is fast to perform. Authors in [11] examined the impact damage detection feasibility of 3 damage indices based on mode shapes, namely, differences in out of plane translations, differences in slopes of the translations and differences in translation curvatures by comparing structural signatures in healthy and damaged state of carbon epoxy laminated composite plates. Mode shapes were obtained using TV pulsed holography with loudspeaker excitation and pulsed ruby laser to read the structural displacements. Researchers in [12] proposed to base the choice of mode shapes for the damage identification on the highest shifts of natural frequency imposed by damage. In this work, damage localization procedure was carried out on numerically simulated cantilever and simply supported steel plates by comparing slope of mode shapes in their healthy and damaged condition. The location of damage in beam-like structures can be found by examining the natural frequency shifts caused by damage as shown in [13]. Authors argued that these frequency changes are sensitive to the location of damage for any particular vibration mode, therefore a larger number of mode shapes should be studied. These findings have also been demonstrated experimentally on 12 steel beams in different boundary conditions. Fibre Bragg grating optical fibre sensors were used to measure distributed macrostrain in simply supported steel beams [14, 15]. Based on this data, normalized modal macrostrain (MMS) was computed and compared between healthy and damaged beams. Essentially, it served as a damage index and authors claimed that the use of MMS data improves the performance of MSC methods due to vulnerability to noise and use of numerical differentiation. Dynamic parameters of reinforced concrete beams were extracted in healthy baseline and damaged states using experimental modal analysis and their changes compared using traditional natural frequency shifts and MAC in [16]. Researchers suggested to calculate CoMAC factors of modal curvatures for better damage localization. Low-velocity impact damage identification in carbon epoxy laminate plates using vibration characteristics was studied in [17]. Natural frequency shifts, mode shape changes and curvature of mode shape changes due to damage were examined. Researchers, however, commented that the earliest damage detection is possible if composite specimens' strength decreased by at least 27 %. Also, they concluded that the effect of number of degrees of freedom of

mode shapes and the number of mode shapes themselves on damage identification is unclear. The progression of damage severity in reinforced concrete single-span bridge using extracted natural frequencies and mode shapes from frequency response of harmonic excitation was reported in [18]. Modal curvatures calculated from lower order modes successfully pinpointed the location of damage. Studies in [19] demonstrated that damage localization results in beam type structures based on numerically computed modal curvatures by traditional means of central differences are improved by incorporating Savitzky-Golay filter and cubic smoothing spline method. In paper [20] fibre optical sensor system was adopted for performing modal analysis of beams under bending. Modal analysis results were compared to the ones obtained with strain gauges and accelerometers. Fibre optical sensor measurements were Cauchy wavelet-transformed to yield eigenfrequencies and damping ratios. Authors argued that use of optical sensors has an advantage over conventional sensors, e.g., accelerometers, in terms of calculation of modal curvatures, which, in turn, are used in damage localization. Authors in [21, 22] proposed to fuse wavelet transform and Teager energy operator and to use complex-wavelets [23] to enhance the damage detection capabilities of the common mode shape curvature. Authors claimed that this approach is able to tackle the problem of multiple damage localization and is also relatively immune to measurement noise.

In this study, four railway concrete sleepers are subjected to 3-point bending load configuration in order to artificially generate crack damages. Two out of four sleepers are loaded to failure, whereas the remaining sleepers are subjected to a two-stage loading scheme – at the first stage the sleepers are loaded until the first crack, while at the second stage the load reaches 1.5 times the load of the first stage. At each of these states of structural integrity, the experimental modal analysis with an impact excitation is conducted to extract and compare natural frequencies and deflection shapes. Afterwards, the deflection shapes become the input for damage localization algorithm based on mode shape curvature squares method. The standardization of damage indices and subsequent application of thresholds corresponding to incremental levels of confidence of damage localization ensures more accurate performance of the proposed algorithm. The results suggest that the algorithm has managed to localize the cracks mostly in mid span region of the sleepers where the actual cracks are clustered according to the crack measurements.

The presented paper is organized in the following manner: In Section 2, the proposed damage localization algorithm based on mode shape curvature squares is introduced. In Section 3, description of tested specimens and experimental equipment and techniques is provided. In Section 4, the results of crack localization in railway concrete sleepers are presented.

2. Damage localization algorithm

The proposed algorithm exploits the fact that the flexural stiffness EI is locally decreased in the zone of damage. As a response, the magnitude of mode shape curvature locally increases. Most methods based on mode shape curvature found in the literature compare healthy or baseline data of the structure with that of a damage structure. However, such an information often cannot be obtained a priori to an actual event of damage and is difficult to obtain during the real service conditions of the structure. In present paper, this shortcoming is avoided by using exclusively mode shape curvature data of a damaged structure.

The basic idea of the method is that the mode shape curvature of the healthy structure has a smooth surface, and it can be approximated by a polynomial. Using the mode shape curvature data of the damaged structure and a regression analysis with a polynomial approximation, smooth mode shape curvature surfaces of the healthy structure are estimated [24]. A locally weighted scatter plot smooth using linear least-squares fitting is employed to build the smoothed surface [25]. The local regression smoothing process follows these steps for each data point:

1. Compute the *regression weights* for each data point in the span. The weights are given by the tri-cube function:

$$w_i = \left(1 - \left|\frac{x - x_i}{d(x)}\right|^3\right)^3 \quad (1)$$

where x is the predictor value associated with the response value to be smoothed, x_i are the nearest neighbours of x as defined by the span, and $d(x)$ is the distance along the abscissa from x to the most distant predictor value within the span.

The weights have the following characteristics:

- The data point to be smoothed has the largest weight and the most influence on the fit;
 - Data points outside the span have zero weight and no influence on the fit.
2. A weighted linear least-squares regression is performed.
 3. The smoothed value is given by the weighted regression at the predictor value of interest.

The damage index is defined as the absolute difference between the measured curvature of the damaged structure and the smoothed polynomial representing the healthy structure. The maximum value indicates the location of damage. In this study, the mode shape curvatures and the corresponding polynomial smoothing are computed only in x direction, because in accordance with the developed wireframe model for deflection shapes of concrete sleepers, only 2 nodes are present in y direction and thus, it renders impossible to calculate mode shape curvatures in y using the difference relations from Eq. (3). Hence, the formulation of damage index in two dimensions found in [24] is adapted for a one-dimensional space. This damage index for the n^{th} mode at grid point i is expressed as:

$$DI_i^n = \left| \left(\frac{\partial^2 w^n}{\partial x^2} \right)_{(i)} - \kappa_x^{n^2}{}_{(i)} \right| \quad (2)$$

where w^n is the measured transverse displacement of the structure, κ_x^n is smoothed mode shape curvature surface in x direction, n is a mode number, and i is a number of grid points in x direction.

The mode shape curvature is calculated from the mode shapes by the central difference approximation at grid point i as:

$$\left(\frac{\partial^2 w^n}{\partial x^2} \right)_{(i)} = \frac{w_{i+1}^n - 2w_i^n + w_{i-1}^n}{h^2} \quad (3)$$

where h is the distance between two successive nodes or measured points.

To deal with the problem of other smaller peaks, the concept of the statistical hypothesis testing technique [26-29] is used. For this reason, the damage indices determined for each node are standardized and the concept of the statistical hypothesis testing is used to classify damaged and undamaged elements and to locate damage depending on the pre-defined damage threshold value. The standardized damage index at grid point i for every mode shape is obtained as follows:

$$SDI_i^n = \frac{DI_i^n - \mu_{DI}^n}{\sigma_{DI}^n} \quad (4)$$

where μ_{DI}^n and σ_{DI}^n are, respectively, mean value and standard deviation of damage indices from Eq. (2) for every mode shape. The decision on the localization of damage is established based on the level of significance used in the hypothesis test, which can be determined from a pre-assigned classification criterion. The typical damage threshold values for the standardized damage index widely used in literature include 1.28, 2, and 3 for 90 %, 95 %, and 99 % confidence levels for the presence of damage.

3. Experimental procedure

3.1 Concrete sleepers

The railway concrete sleepers are an essential component in railway track. According to [30-32] their function is to

- redistribute the dynamic loads from the rail foot to the underlying ballast bed;
- support and restrain the rail foot;
- maintain the rail gauge;
- withstand longitudinal, lateral and vertical rail movements;

- provide insulation between parallel rails;
- resist wear and endure extreme weather conditions.

The pre-stressed concrete sleepers are usually used in the standard gauge, heavy haul rail tracks [30].

Four railway pre-stressed concrete mono block sleepers of type G44 manufactured by CEMEX are considered in this study. The physical dimensions of sleepers are as follows: length = 2500 mm, depth at rail seat = 200 mm, nominal maximum weight = 309 kg + 3 kg for loose fastening components. A total of six tendons are embedded within every sleeper. The photo of the sleepers is shown in Fig. 1.

Fig. 1. G44 concrete sleepers.

3.2 Experimental modal analysis

In order to simulate a real ballast condition, a polymeric material can be placed between the rail seats of sleepers as an alternative test support specified in Australian Standard AS1085.19J [33–38]. It is found that 5 layers of rubber conveyor matting used in the mining industry is enough to avoid excessive vibrations from the floor. These free support conditions are shown in Fig. 2 (a). Experimental modal analysis with impact hammer excitation is performed on concrete sleepers in their healthy and damaged condition to extract the global dynamic parameters. Components of experimental modal testing equipment are shown in Fig. 2 (b).

The equipment contains PROSIG P8004 acquisition box with 4 channels. The modally tuned impact hammer (PCB Piezotronics, model 086D05, serial number 36223) is connected to the first channel, while accelerometer – to the second channel. The hammer size, length, material and velocity at impact determine the amplitude and frequency content of the force impulse. The impact cap material determines energy content. In general, stiffer tips are suggested for higher frequency responses. Plastic vinyl tip is used for the impact hammer (sensitivity $0.2509 \frac{\text{mV}}{\text{N}}$). PCB Piezotronics quartz shear accelerometer of model 352B, serial number 187846 (Fig. 2 (c)) is mounted on the surface of sleepers using thin layer of wax. The sensitivity of accelerometer at 100 Hz is $99.7 \frac{\text{mV}}{\text{m/s}^2}$, the bias level of 11.2 V DC and the frequency range of 2 to 10 kHz.

(a)

(b)

(c)

Fig. 2. Modal analysis setup: (a) concrete sleeper on a rubber mat; (b) testing equipment; (c) accelerometer.

Roving impact excitation is performed over 26 points along the perimeter of the top surface of the sleepers. Locations of excitation points are chosen to lie where slope of the surface relief experiences changes. Dynamic response of the sleepers is measured near point No. 26 via uniaxial accelerometer

in Y direction (vertical direction). The wireframe model for experimental modal analysis of concrete sleepers is shown in Fig. 3. The x and y coordinates of all 26 measurement nodes are also given. The accelerometer is mounted at one of the corners of the sleepers and remains in a fixed position. Setup information is passed to DATS software (PROSIG) where the following parameters are edited – frequency bandwidth = 0:2048 Hz, resolution = 1 Hz, number of averaging for each impact: 10 times, window functions: exponential window for response and force window for excitation. Frequency response functions (FRFs) and coherence plots are recorded for every excitation point. Curve fitting of collected raw FRFs employing Half-Power method is performed in DATS Modal Analysis package in order to extract resonance frequencies, corresponding damping ratios and mode shapes. A total of five first deflection shapes are extracted.

Fig. 3. Wireframe model for deflection shapes of sleepers (top view), units in millimeters.

3.3. Three-point bending

BS EN 13230 specifies the support conditions required for the 3-point bending test, instructing point supports at the railheads for both positive and negative bending tests. This standard is commonly used for performance benchmarking in industry [39-43]. The support must be 100 mm wide and made from steel with a hardness Brinell: HBW > 240.

For this study, a static load is applied at the mid span of the sleepers for both positive and negative bending in order to create artificial cracks. It is important to note that the standard type testing setup is commonly used for performance benchmarking in manufacturing quality control. The setup for positive bending test is shown in Fig. 4 (a) and the loading controls in Fig. 4 (b).

Fig. 4. Experimental setup for three-point bending tests: (a) test configuration; (b) loading controls.

The procedure of experimental testing along with the damage localization is shown in Fig. 5. At first, experimental modal analysis is performed on all four sleepers at their healthy state using the boundary conditions shown in Fig. 2 (a). Afterwards, sleepers are subjected to 3-point bending where two sleepers are set for positive bending moment configuration and remaining two sleepers – for

negative. Two sleepers (one from each of two bending configurations) are loaded to failure and their deflection shapes are extracted. These sleepers (sleepers 1 and 3) are not considered for damage localization purposes, whilst for other two sleepers a two-stage procedure with the following steps is employed:

1. At first, experimental modal analysis is performed on both sleepers at their healthy state at free boundary conditions. FRF at each point of excitation is measured ten times and these FRFs are later averaged over all nodes of excitation to obtain the FRF of the whole sleeper. This FRF is post-processed (curve-fitting procedure) to extract natural frequencies, damping and deflection shapes.
2. Sleepers are placed on 100 mm wide steel supports and a static load is applied at mid-span in a 3-point bending configuration. Sleeper 4 is set for positive bending moment and sleeper 2 – for negative. Sleepers are loaded till first crack.
3. Sleepers are taken off the steel supports, put on the rubber matting and an experimental modal analysis is repeated.
4. Sleepers are set for bending test where the load is increased from 0 kN to load corresponding to 1.5 times the load of first crack.
5. Sleepers are put on the rubber matting once more for the final stage of experimental modal analysis.
6. Resonance frequencies are extracted from FRF of a structure for healthy, cracked and 1.5 cracked states of the sleepers.
7. A total of 5 deflection shapes (1st bending, 2nd bending, 1st torsion, 3rd bending and 4th bending) are extracted for all health states of the sleepers. Torsional shape is dismissed, since, in our case, mode shape curvature calculations are not possible in y direction.
8. By inputting each of the extracted deflection shapes into damage localization algorithm separately, a curvature (Eq. (3)) of the particular deflection shape in x direction is calculated.
9. Polynomial fitting of curvature surfaces is computed to generate smooth surfaces κ_x representing the healthy structure and thus eliminating the need for baseline data.
10. Damage index distribution according to Eq. (2) is calculated for both sleepers at their cracked and 1.5 cracked state.
11. Damage index is then standardized (refer to Eq. (4)) with the application of statistical hypothesis testing.
12. Threshold levels of 1.28, 2 and 3 are applied to standardized damage indices to ascertain for crack localization with confidence of 90 %, 95 % and 99 %, respectively.
13. The locations of peaks in thresholded standardized damage index profiles are then compared with actual crack location measurements and the final decision on crack localization is made.

Fig. 5. Experimental testing and damage localization flowchart.

4. Results

4.1. Crack progression

The crack observations were marked on the sleepers as the experiment was ongoing. Cracking patterns corresponding to 1.5 times the first crack load for sleepers 2 and 4 are shown in Fig. 6 for one side of each sleeper. In the same figure, one can see the failed sleepers 1 (negative bending moment configuration) and 3 (positive bending moment configuration). These sleepers had reached the ultimate load of 102 kN with a significant loss of tendon prestressed force and concrete disintegration for sleeper 1 and 113 kN with a pronounced shear failure mode for sleeper 3.

(a)

(b)

(c)

(d)

Fig. 6. Cracking pattern of concrete sleepers after loading: (a) sleeper 2 at the first crack (53 kN) and 1.5 load of the first crack load; (b) sleeper 4 at 1.5 load of the first crack load; (c) failed sleeper 1; (d) failed sleeper 3.

Measurements of crack locations for both sides of sleepers 2 and 4 are provided in Fig. 7. These measurements are necessary for validation of damage localization. As expected, cracks are clustered around mid-span corresponding to the largest bending moment.

Fig. 7. Measurements of crack locations after loading with force equal to 1.5 times the first crack load.

4.2. Modal analysis

DATS software has been used for recording and post-processing of experimental modal analysis data. The following steps have been made on this matter. Frequency response functions (FRFs) and coherence functions have been recorded for every node of excitation after an impact with a modal hammer. Afterwards, a curve-fitting of FRFs using Half-Power method has been performed and modal parameters (natural frequencies and damping ratios) extracted. Fitted FRFs and calculated displacements have been superimposed on the wireframe model (Fig. 3). This fitted FRF along with the corresponding coherence at healthy and cracked states of sleeper 2 are shown in Fig. 8. Relatively small fluctuations of the coherence function around unity suggest satisfactory modal measurements over the desired frequency range (excluding higher frequencies which are not of interest in this study).

The first and even further cracking has insignificant influence on stiffness of sleepers as indicated by barely visible natural frequency shifts with the presence of crack. The extracted modal parameters, averaged over all excitation nodes of the wireframe are shown in Table 1. The most marked difference is in the first mode, decreasing by 5.4 %, with the other four modes having reductions of less than 0.7 %. Visibly, there is no discernible difference but the frequency reduction indicates that damage has occurred.

Fig. 8. Experimental modal analysis results for sleeper 2: (a) FRF; (b) coherence.

Table 1

Extracted modal parameters of sleeper 2

Mode	Healthy	1 st Crack	1.5 × 1 st Crack
1 st bending	$\bar{f} = 128.4 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (2.13 \pm 0.08) \%$	$\bar{f} = 121.4 \pm 0.1 \text{ Hz}$ $\bar{\xi} = (1.81 \pm 0.03) \%$	$\bar{f} = 127.1 \pm 0.3 \text{ Hz}$ $\bar{\xi} = (2.07 \pm 0.13) \%$
2 nd bending	$\bar{f} = 348.5 \pm 0.1 \text{ Hz}$ $\bar{\xi} = (0.94 \pm 0.03) \%$	$\bar{f} = 346.2 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (1.04 \pm 0.07) \%$	$\bar{f} = 346.3 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (1.02 \pm 0.16) \%$
3 rd bending	$\bar{f} = 673.3 \pm 0.7 \text{ Hz}$ $\bar{\xi} = (0.69 \pm 0.17) \%$	$\bar{f} = 670.2 \pm 0.9 \text{ Hz}$ $\bar{\xi} = (1.22 \pm 0.21) \%$	$\bar{f} = 668.0 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (0.81 \pm 0.03) \%$
4 th bending	$\bar{f} = 1054.0 \pm 0.6 \text{ Hz}$ $\bar{\xi} = (0.86 \pm 0.18) \%$	$\bar{f} = 1052.1 \pm 0.6 \text{ Hz}$ $\bar{\xi} = (0.73 \pm 0.22) \%$	$\bar{f} = 1048.8 \pm 0.6 \text{ Hz}$ $\bar{\xi} = (0.89 \pm 0.27) \%$

The corresponding experimental modal analysis results for sleeper 4 are shown in Fig. 9 and Table 2. As with sleeper 2, coherence functions remain relatively flat around unity, except for the highest frequencies not considered in this study. The largest decrease of natural frequency value is for the first deflection shape (3.1 %), pointing towards a slight overall reduction in global stiffness. The acquired modal parameters for the positive and negative crack progressions suggests that the minor cracking has negligible influence on the stiffness. As the cracks progressed and the load reached between 80 and 90 kN their influence on the dynamic properties start to become apparent. By just observing the deflection shapes, it is difficult to discern any noticeable difference between healthy and damaged state of the structure with development of cracks. On the other hand, frequency values show a trend suggesting that it is possible to identify sleeper damage through modal analysis, however, the magnitude of damage must reach a yet to be determined threshold.

Fig. 9. Experimental modal analysis results for sleeper 4: (a) FRF; (b) coherence.

Table 2

Extracted modal parameters of sleeper 4

Mode	Healthy	1 st Crack	1.5 × 1 st Crack
1 st bending	$\bar{f} = 123.9 \pm 0.1 \text{ Hz}$ $\bar{\xi} = (1.83 \pm 0.07) \%$	$\bar{f} = 120.1 \pm 0.1 \text{ Hz}$ $\bar{\xi} = (1.90 \pm 0.07) \%$	$\bar{f} = 125.0 \pm 0.1 \text{ Hz}$ $\bar{\xi} = (2.15 \pm 0.12) \%$
2 nd bending	$\bar{f} = 344.9 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (0.98 \pm 0.20) \%$	$\bar{f} = 343.6 \pm 0.4 \text{ Hz}$ $\bar{\xi} = (1.03 \pm 0.21) \%$	$\bar{f} = 344.7 \pm 1.2 \text{ Hz}$ $\bar{\xi} = (0.90 \pm 0.19) \%$
3 rd bending	$\bar{f} = 665.5 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (0.88 \pm 0.03) \%$	$\bar{f} = 666.2 \pm 0.5 \text{ Hz}$ $\bar{\xi} = (1.26 \pm 0.15) \%$	$\bar{f} = 665.0 \pm 0.2 \text{ Hz}$ $\bar{\xi} = (0.76 \pm 0.02) \%$
4 th bending	$\bar{f} = 1044.8 \pm 0.7 \text{ Hz}$ $\bar{\xi} = (0.81 \pm 0.31) \%$	$\bar{f} = 1046.1 \pm 0.4 \text{ Hz}$ $\bar{\xi} = (0.77 \pm 0.36) \%$	$\bar{f} = 1045.0 \pm 0.4 \text{ Hz}$ $\bar{\xi} = (0.74 \pm 0.32) \%$

The extracted deflection shapes for various health states of concrete sleepers are given in Table 3. No visible differences between deflection shapes at healthy and cracked states can be observed. On the other hand, failure of sleepers causes a sever distortion of deflection shapes along with significant natural frequency reduction.

Table 3

Extracted mode shapes of sleepers at various health conditions

Mode	Healthy	1st Crack	1.5 × 1st Crack	Failed
1 st bending				
2 nd bending				
3 rd bending

4.3. Damage localization

Standardized damage index profile along with an application of threshold of 3, curvature in x direction and polynomial smoothing of this curvature κ_x for the first deflection shape of sleeper 4 are shown in Fig. 10.

Fig. 10. Standardized Damage Index distribution for sleeper 4 (1st bending mode), cracked: (a) no threshold; (b) with a threshold of 3, (c) curvature in x direction, (d) polynomial fit of curvature in x direction.

Curvatures of all extracted bending deflection shapes for all health states of sleepers 2 and 4 are depicted in Table 4. The curvatures are not computed in y direction as deflection shapes comprise of only two data points in this direction. According to Eq. (3), two neighbouring points are required to calculate central difference approximation between these points. Therefore, instead of 2×13 data points the signal size of deflection shapes is 2×11 . The difference of curvature values (in %) with each progression of damage with respect to healthy state is given below the curvature plots. These values are organised to match the excitation nodes in the wireframe model (Fig. 3). The largest differences are highlighted in dark green. According to the results for the first bending mode, the most notable differences are at node No. 22 for sleeper 2 and No. 21 for sleeper 4 (ignoring the end of the sleeper), for the second bending mode – at node No. 20 for sleeper 4, while there is no consensus regarding sleeper 2 – cracking may be initiated at node No. 7 but further cracking is more pronounced at node No. 23. For the third bending mode – again node No. 21 and for the fourth bending mode – at node No. 20 for sleeper 4. These findings suggest that most likely the structural integrity has been disrupted at nodes No. 20 and/or 21 for sleeper 4. On the other hand, the respective results do not show a clear trend for sleeper 2 as for different deflection shapes the calculated curvature changes are not of the same level of magnitude for initial and further cracking.

Table 4

Curvature of bending modes of sleepers 2 and 4 under various states of health and relative difference of curvature (in %) with respect to healthy state for every node

healthy	cracked	cracked 1.5
---------	---------	-------------

1st bending mode

sleeper 2

sleeper 4

sleeper 2

healthy → cracked

423.2	22.8	8.2	53.7	3.3	5.5	-50.5	114.3	-48.1	97.8	-3.4
455.9	170.0	0.5	180.0	-22.0	33.8	-44.8	27.1	-2.2	35.0	60.1

healthy → cracked 1.5

111.1	-529.5	214.8	907.7	-3.5	16.2	19.7	-414.6	223.6	-180.5	83.2
84.7	-379.3	64.1	-1441.0	-136.8	-25.2	-338.5	1066.7	23.3	-191.8	45.6

sleeper 4

healthy → cracked

68.2	9.6	23.6	175.1	46.6	-20.8	71.6	562.7	32.6	-647.6	17.7
-1245.5	-47.2	27.8	105.1	387.1	59.0	-61.7	198.4	18.3	6.1	-103.7

healthy → cracked 1.5

2.4	11.2	23.5	73.2	-11.0	10.1	42.9	568.1	17.9	-794.5	26.1
-1522.5	160.6	-6.4	90.1	389.3	54.1	-69.5	191.6	16.7	-46.8	121.0

2nd bending mode

sleeper 2

sleeper 4

healthy → cracked

-188.6	-1.5	-3.9	0.3	-15.4	94.6	4.1	-3.2	-14.4	13.9	27.7
-303.6	30.8	-17.5	-6.1	4.8	21.2	-11.1	3.4	-14.6	15.5	31.8

healthy → cracked 1.5

99.5	-39.6	-7.5	243.0	14.8	-29.0	68.3	-42.5	51.6	99.5	-39.6
187.9	137.6	-267.9	50.5	-199.8	220.0	183.4	-179.7	23.8	187.9	137.6

sleepers 4											
healthy → cracked											
-14.7	-4.7	10.4	-6.7	15.3	167.5	-27.3	2.9	15.2	-53.0	31.4	
-97.7	14.1	-19.6	-6.7	22.3	378.6	-39.0	19.6	3.5	-19.7	25.3	
healthy → cracked 1.5											
-16.3	-4.8	8.0	-13.3	26.7	128.0	-1.7	-4.6	6.1	-36.5	25.7	
-228.7	26.7	-10.2	-8.2	9.1	327.8	-27.2	6.5	5.4	-19.2	23.8

sleepers 2											
healthy → cracked											
-58.7	5.5	1.9	-15.0	-0.5	-7.9	11.5	-22.7	0.7	0.5	18.1	
-81.0	16.0	-15.5	-15.4	-7.7	-13.6	33.4	-6.9	-12.5	2.2	22.5	
healthy → cracked 1.5											
-26.4	16.5	-69.0	83.3	27.1	11.3	-15.6	143.2	-104.1	7.6	35.2	
-31.1	-52.4	205.3	-29.9	62.1	-13.0	48.0	-127.2	238.8	-82.5	19.1	

sleepers 4											
healthy → cracked											
-5.4	6.2	-8.4	-46.2	-38.2	-7.6	14.8	11.4	-3.6	-15.5	7.6	
-28.9	8.3	-24.8	-10.6	-93.1	11.6	19.6	14.1	-2.8	-4.1	6.2	
healthy → cracked 1.5											
-1.8	1.6	-8.5	-36.5	-39.6	0.3	16.6	18.3	8.0	-14.3	4.6	
-66.6	10.5	-28.6	-23.4	-121.7	14.8	22.1	22.7	-10.7	-6.8	12.7

sleeper 2											
healthy → cracked											
-30.4	-1.8	-1.5	9.3	-2.3	-386.9	-11.0	0.2	1.6	-12.0	9.4	
-35.3	2.2	138.5	-3.4	-5.6	-88.2	-7.3	-4.0	511.9	-3.2	9.9	
healthy → cracked 1.5											
-38.0	39.7	1511.3	-106.5	-5.2	-34.8	1.1	-155.6	2161.2	32.4	14.1	
-10.6	-2.5	-435.2	142.8	-55.9	-67.0	-56.1	200.0	-2596.9	-8.3	0.5	
sleeper 4											
healthy → cracked											
-0.4	4.2	61.0	-4.7	-3.7	-30.3	-1.1	-5.0	-74.2	-2.6	-4.1	
-3.9	4.6	106.2	-25.4	2.2	124.3	-10.1	-9.7	120.8	0.4	0.6	
healthy → cracked 1.5											
-2.0	5.6	71.9	-7.6	-4.8	29.6	3.1	-8.0	387.8	-6.6	-3.0	
-28.2	2.4	68.4	-17.9	2.5	143.5	-13.0	-0.3	111.7	-0.6	5.0	

Standardized damage index (with thresholds) profiles are computed for both sleepers using all five deflection shapes as an input according to procedure from subsection 3.3. The thresholded standardized damage index distributions are further analysed with respect to location of peaks. If these peaks are in the same position as the measured locations of cracks, the algorithm has successfully managed to localize the cracking damage. The thresholded standardized damage index distributions for every deflection shape along with the excitation node with nonzero amplitude are given in Table 5.

Table 5

Thresholded standardized damage index distributions for both concrete sleepers calculated for different deflection shapes

Sleeper 2		Sleeper 4	
cracked	cracked 1.5	cracked	cracked 1.5
1 st bending shape			
Node 18: 2.70 Node 19: 2.17	Node 10: 3.19	Node 7: 3.85	Node 23: 3.11
2 nd bending shape			
Node 19: 2.64	Node 19: 2.66	Node 8: 2.09 Node 19: 2.89	Node 19: 2.79
3 rd bending shape

All nodes with nonzero amplitude of thresholded standardized damage indices are summed up over all 5 deflection shapes and the fraction of occurrence is provided in Table 6.

Table 6

Node counts over all 5 deflection shapes for both sleepers

Sleeper 2, cracked	Node 19: 3/5	Node 18: 1/5	Node 23: 1/5	Node 17: 1/5	Node 16: 1/5	Node 24: 1/5	Node 21: 1/5	
Sleeper 2, cracked 1.5	Node 10: 1/5	Node 19: 1/5	Node 25: 1/5	Node 7: 1/5	Node 20: 1/5	Node 3: 1/5	Node 8: 1/5	Node 11: 1/5
Sleeper 4, cracked	Node 7: 2/5	Node 8: 2/5	Node 19: 1/5	Node 5: 1/5	Node 18: 1/5	Node 20: 1/5	Node 3: 1/5	Node 11: 1/5
Sleeper 4, cracked 1.5	Node 23: 1/5	Node 19: 2/5	Node 12: 1/5	Node 20: 1/5	Node 11: 1/5			

Measured crack locations in conjunction with the developed sleeper wireframe model are used to establish a correspondence between particular excitation nodes and crack coordinates. These results for both sleepers are shown in Tables 7 and 8. As expected, all crack location nodes lie between two successive nodes. Therefore, nodes that are closer to the cracks are underlined. At the bottom of the table, the highlighted nodes are summed up over all cracks for both sides of sleepers and the likelihood of the node to be the closest to any of these cracks is computed.

Table 7

Correspondence between crack locations in sleeper 2 and nodes of a sleeper wireframe

Sleeper 2 side 1: $y = 0$ mm	Sleeper 2 side 2: $y = 200$ mm
1066 mm → nodes <u>6</u> /7	1054 mm → nodes 20/ <u>21</u>
1073 mm → nodes <u>6</u> /7	1135 mm → nodes 20/ <u>21</u>
1173 mm → nodes <u>6</u> / <u>7</u>	1261 mm → nodes 19/ <u>20</u>
1263 mm → nodes <u>7</u> /8	1309 mm → nodes 19/ <u>20</u>
1346 mm → nodes <u>7</u> /8	1403 mm → nodes <u>19</u> / <u>20</u>
1442 mm → nodes <u>7</u> / <u>8</u>	1491 mm → nodes 18/ <u>19</u>
Node 6: 2/6	Node 19: 2/6
Node 7: 3/6	Node 20: 2/6
Node 8: 1/6	Node 21: 2/6

Table 8

Correspondence between crack locations in sleeper 4 and nodes of a sleeper wireframe

Sleeper 4 side 1: $y = 0$ mm	Sleeper 4 side 2: $y = 200$ mm
1065 mm → nodes <u>6</u> /7	1020 mm → nodes <u>21</u> / <u>22</u>

1125 mm → nodes <u>6</u> /7	1160 mm → nodes <u>20</u> /21
1230 mm → nodes 6/ <u>7</u>	1196 mm → nodes <u>20</u> /21
1311 mm → nodes <u>7</u> /8	1315 mm → nodes 19/ <u>20</u>
1448 mm → nodes 7/ <u>8</u>	1503 mm → nodes 18/ <u>19</u>
Node 6: 2/5	Node 19: 1/5
Node 7: 2/5	Node 20: 3/5
Node 8: 1/5	Node 21: 1/5

The results from Tables 7 and 8 are to be compared with the results of proposed experimental damage localization approach (Table 6). It is found that cracks are mostly localized around node No. 19 for sleeper 2 considering both damage states of the sleeper. In Table 6, the likelihood for crack to be near node No. 19 is 2/6 or 1/3 with the same likelihood for crack to lie near nodes No. 19 and 21. Unfortunately, no reliable localization results are obtained for row of nodes at $y = 0$ mm. Crack should have been localized near node No. 7 as there is a 50 % likelihood for crack tie lie near that node according to measurements. It can be concluded that for sleeper 2 the algorithm has managed to locate crack at coordinates (1403:1491,200) mm with a relatively high level of confidence. As for sleeper 4, crack localization results from Table 5 match the measured crack positions for nodes No. 19 and 20 (Table 7). Crack measurements indicate that for node No. 19 there is only 20 % likelihood for crack to lie near this node, but for node No. 20 – 60 %. By combining all crack localization results for sleeper 4, it is found that node No. 19 has the largest likelihood to contain a crack in it's vicinity, while nodes No. 11 and 20 have the same likelihood. However, node No. 11 is not identified in crack measurements. The proposed algorithm has located cracks near nodes No. 7 and 8 for initially cracked state, however these results are not consistent with results for further cracking where these particular nodes do not appear in localization results. Therefore, it can be concluded that the proposed damage localization algorithm has located two cracks for sleeper 4 at coordinates (1160:1315,200) mm and ($\cong$ 1503,200) mm.

The proposed damage localization techniques has successfully detected the most prominent cracks in the prestressed railway concrete sleepers despite the following factors that limit the accuracy of damage localization:

- non-significant reduction of stiffness caused by concrete cracking;
- the effect of measurement noise;
- sparsity of deflection shape signals.

Nevertheless, it was chosen to do so in order to test the proposed damage localization algorithm in real life service conditions of the structure in an early stage of structural deterioration and when dense sensor grid for extraction of highly detailed deflection shapes is not available or plausible.

5. Conclusions

In this study, the well-known mode shape curvature square method is applied to cracking localization in pre-stressed railway concrete sleepers. Cracks are introduced through application of load at mid-span in two different sleeper configurations – positive and negative bending moments. Experimental modal analysis with impact excitation of upper surface of the sleepers is conducted to extract the first five natural frequencies and deflection shapes at various integrity states – healthy, the first crack and at load corresponding to 1.5 times the first crack load. Visually, no noticeable differences can be observed by examining the deflection shapes, although the natural frequency shifts, especially for the first bending mode suggest indicate the presence of damage. The mode shape curvature square method with the application of standardization of damage indices with various confidence levels of damage localization has revealed that the highest likelihood of crack location is at mid-span in accordance with the actual crack measurements for both configurations of sleepers. Unfortunately, the limitation of this method is that no damage can be localized at edges of the structure as mode shape curvature computation requires 2 neighbouring data points and thus the outermost data points of mode shapes are eliminated. However, this was not the case in the current study as cracking occurred at mid span of the sleepers. The challenges of accurate localization of cracks lie particularly in the existence of measurement noise, non-significant reduction of structural stiffness imposed by damage and sparsity of mode shape wireframe data points so that the actual damage lies between 2 successive nodes and may even be relatively far from each of them. The

insight derived from this study will lead to the development of on-board monitoring technology for sleeper crack detection using displacement sensors. Throughout the service life of the sleepers, the displacement distribution would be measured and deflection shapes extracted. These shapes would be post-processed using the proposed methodology to locate the damage.

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