Modelling the response of potassium vapour in resonance scattering spectroscopy


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Abstract

Resonance scattering techniques are often used to study the properties of atoms and molecules. The Birmingham Solar Oscillations Network (BiSON) makes use of Resonance Scattering Spectroscopy by applying the known properties of potassium vapour to achieve ultra-precise Doppler velocity observations of oscillations of the Sun. We present a model of the resonance scattering properties of potassium vapour which can be used to determine the ideal operating vapour temperature, and spectrophotometer detector parameters, which are essential when developing new instrumentation making use of off-the-shelf components [8].

1. Introduction

Resonance scattering techniques are often used to study the properties of atoms and molecules, such as energy levels and the fine and hyperfine structure [1]. When applied to absorption spectroscopy with techniques such as optical pumping (so-called Saturated Absorption Spectroscopy) it is possible to achieve a resolution that is Doppler-free and limited only by the uncertainty principle, producing a highly stable locking reference for tunable laser systems [2, 3]. Resonance scattering spectroscopy has wide reaching multi-disciplinary applications including biomedical diagnostics [4], and environmental sensing in terms of atmospheric pollution [4]. In astronomy, vapour reference cells are often used to enable the high-precision spectrograph wavelength calibration required for asteroseismology and detection of exoplanets [5, 6].

The Birmingham Solar Oscillations Network (BiSON) makes use of resonance scattering with a potassium vapour reference cell, enabling ultra-precise Doppler velocity measurements of oscillations of the Sun [7]. In this article we present a model of the resonance scattering properties of potassium vapour which can be used to determine the ideal operating vapour temperature, and spectrophotometer detector parameters, which are essential when developing new instrumentation making use of off-the-shelf components [8].

In section 2 we give a brief overview of BiSON instrumentation and the use of resonance scattering spectroscopy. In section 3 we review the theory of spectral line formation from first principles, beginning from a similar position to Boumier and Dame [9] for sodium vapour, and in section 4 develop the equations necessary to determine optical depth from vapour temperature. In sections 5 and 6 we use a tunable diode laser to validate the model against the absorption

Some figures may appear in colour only in the online journal.
profiles observed with a standard BiSON vapour cell at a range of temperatures. Finally in section 7 we use the model to determine the ideal vapour temperature and detector configuration to maximise the detected scattering intensity, and again validate against observed scattering profiles.

2. BiSON instrumentation

The original BiSON resonance scattering spectrophotometer (RSS) developed for Doppler velocity astronomical observations is described by Brookes et al [10]. Modern BiSON RSS follow the same principles but make use of slightly different designs, and a typical example is shown in figure 1. Light from the Sun is first passed through a 30 mm diameter aperture, and a pair of lenses in a Keplerian telescope arrangement are used to compress the beam reducing the diameter in preparation for subsequent smaller optics. A red long-pass filter, and an infra-red short-pass filter, form a pair to relieve the thermal load on the instrumentation. An interference filter with a bandwidth of 1.5 nm is used to isolate only the potassium D1 Fraunhofer line at 769.898 nm, excluding the D2 line. The potassium is contained within a small cubic glass cell with sides of length 17 mm, and a short stem. The stem is typically heated to around 90 °C to cause the formation of potassium vapour within the cell, with the cubic cell itself maintained at a temperature higher than this to ensure the glass remains clear of solid potassium. The cell is placed in a longitudinal magnetic field which causes the absorption line to be Zeeman split into two components, where their separation is dependent on the magnetic field strength. Splitting the lab reference-frame in this way allows measurements to be taken at two working points on the corresponding absorption line in the solar atmosphere. The polarisation component is selected using a linear polariser and an electro-optic Pockels-effect quarter-wave retarder. The polarisation is switched at approximately 100 Hz and a normalised ratio, $R$, formed,

$$ R = \frac{I_b - I_r}{I_b + I_r}, $$

where $I_b$ and $I_r$ are the measured intensities in the blue and red wings respectively. Normalising the ratio in this way reduces the effect of atmospheric scintillation allowing low-noise photometry through Earth’s atmosphere [11], and also means it is unnecessary to know the precise value of the magnetic field strength or the precise frequency of the potassium line on the Sun. Light is focused into the centre of the potassium cell, where it is resonantly scattered by the vapour. Light that interacts with the vapour is scattered isotropically, and it is this isotropic nature that is leveraged by the BiSON RSSs to move a photon away from the instrumental optical axis and into a detector. Two photodiode detectors on either side of the beam return a precise measurement of the changing solar radial velocity. A third detector monitors unscattered light that passes directly through the instrument.

There are several natural broadening processes which affect the properties of an absorption line, and it is necessary to understand the environmental factors (temperature and pressure) that affect these processes when building a model of expected instrumentation performance and informing new designs [8].

3. Resonance radiation

3.1. Natural line width

In a gas that forms an absorption line, the absorption coefficient $\kappa_\nu$ of the gas is defined in terms of,

$$ I_\nu = I_0 e^{-\kappa_\nu x}, $$

where $I_0$ is the intensity of incident light, $I_\nu$ is the intensity of the transmitted light, and $x$ is the thickness of the absorbing material. The units of the absorption coefficient are always...
expressed in terms of the reciprocal of the units of $x$ such that the exponent becomes a unitless ratio.

It can be shown [12, p 95] that the integral of $\kappa_\nu$ over all frequencies is equal to,

$$\int \kappa_\nu d\nu = \frac{\lambda_0^2 g_2 N}{8\pi g_1 \tau} \left(1 - \frac{g_1 N'}{g_2 N}\right),$$

(3)

where $\lambda_0$ is the wavelength at the centre of the absorption line, $\tau$ the lifetime of the excited state, and $g_1$ and $g_2$ are the statistical weights of the normal and excited states respectively. $N$ is the number density of atoms of which $[N - N']$ are capable of absorbing in the frequency range $\nu$ to $\nu + d\nu$, and similarly $N'$ is the number of excited atoms that are capable of emitting in this range. In the case where the ratio of excited atoms to normal atoms is very small ($\ll 10^{-3}$) then $N'$ can be neglected and equation (3) reduces to,

$$\int \kappa_\nu d\nu = \frac{\lambda_0^2 g_2 N}{8\pi g_1 \tau},$$

(4)

and this result shows that the integral of the absorption coefficient is constant if $N$ remains constant. This assumption can normally be made when the formation of excited atoms is due to absorption of a beam of light. Where a gas is electrically excited at high current densities, for example in a gas discharge lamp, the number of excited atoms may become a high fraction of the total number and so the simplification in equation (4) cannot be made. In the case where all atoms capable of absorbing at a certain frequency are already excited, the gas is said to be saturated and no further absorption can take place at that frequency.

Although the energy of an atomic transition is fixed, and therefore similarly the frequency of light with which it can interact, the absorption profile has a natural line width which arises from the uncertainty principle. When considered in the form,

$$\Delta E \Delta \tau \geq \frac{h}{2},$$

(5)

where $\Delta E$ is the energy, $\Delta \tau$ the lifetime, and $h$ the reduced Planck constant, the result suggests that for extremely short excited state lifetimes there will be a significant uncertainty in the energy of the photon emitted. If the energy of many photons are measured the distribution formed is Lorentzian in shape, where $\Gamma$ is the width parameter for a Lorentzian profile. If we assume the lifetime in the excited state is the uncertainty in time (i.e. $\tau = \Delta \tau$) then,

$$\Delta E = \frac{\Gamma}{2} = \frac{h}{2\tau},$$

(6)

and so,

$$\Gamma = \frac{h}{\tau},$$

(7)

which shows that the natural line width is inversely proportional to the lifetime of the atom in the excited state. Mishra [13] observed the natural lifetime of the potassium $4P_2 - 4S_2$ transition to be 27 ns. Using equation (7) this corresponds to a Lorentzian width of $2.44 \times 10^{-8}$ eV. We can convert this to frequency using the relation $E = h\nu$, and so equation (6) becomes,

$$\Delta \nu = \frac{1}{4\pi \tau},$$

(8)

producing a width of 5.9 MHz. For the line centre of the $4P_2 - 4S_2$ atomic transition at 769.898 nm this is a full width at half maximum (FWHM) of just $1.166 \times 10^{-3}$ nm, which is equivalent to a Doppler velocity of 4.54 m s$^{-1}$.

3.2. Pressure broadening

Pressure acts to modify the natural line width. When an excited atom collides with another particle, it can be stimulated to decay earlier than would be the case for its natural lifetime. Continuing the argument from the uncertainty principle as before, if the lifetime is reduced then the uncertainty on the energy emitted must increase and hence broaden the line width. As the pressure increases, the likelihood of collisions increases.

Experimental conditions are usually selected to ensure that pressure broadening is minimised to a level of insignificance, and this is the case for our vapour reference cells which are placed under vacuum before being filled with their reference element. We will neglect this effect.

3.3. Doppler broadening

Since the atoms in a gas are moving, the wavelength of light absorbed or emitted by the gas will be shifted according to the standard non-relativistic Doppler formula,

$$\frac{\Delta \lambda}{\lambda_0} = -\frac{\Delta \nu}{\nu_0} \approx \frac{\nu}{c},$$

(9)

where $\Delta \lambda$ is the shifted wavelength, $\lambda_0$ is the rest wavelength, $\nu$ the speed, and $c$ the speed of light. Similarly, $\Delta \nu$ is the shift in frequency, and $\nu_0$ is the frequency at rest. The atoms in a gas are moving at speeds defined by the Maxwell–Boltzmann distribution, and so a spectral line will be broadened into a range of possible wavelengths with a Gaussian distribution. The FWHM due to Doppler broadening is given by,

$$\Delta \nu = \frac{8k_B T \ln 2}{mc^2} \nu_0$$

(10)

which can be used to calculate the expected Doppler width of the absorption line. Potassium has a standard atomic weight of 39.0983 u. For a reference vapour at 100 °C the broadening is 0.0017 nm. This is equivalent to a Doppler velocity of 663 m s$^{-1}$, almost 150 times larger than the width produced by natural broadening. On the Sun at a temperature of 7777 K, the D1 line width due to Doppler broadening is 0.0067 nm.

It may be shown [12, p 99] that when considering only Doppler broadening, the absorption coefficient of a gas is given by,

$$\kappa_\nu = \kappa_0 e^{-\left(\frac{\Delta \nu}{\Delta \nu_n}\right)^2},$$

(11)
where \( \kappa_0 \) is the ideal maximum absorption for Doppler broadening alone, and \( \Delta \nu \) is the Doppler breadth defined in equation (10). The integral of \( \kappa_\nu \) over all frequencies is equal to,

\[
\int \kappa_\nu d\nu = \frac{1}{2} \sqrt{\frac{\pi}{\ln 2}} \kappa_0 \Delta \nu, \tag{12}
\]

and this depends only on the temperature and the atomic mass of the atoms forming the vapour, which for a given material means temperature is the only variable.

4. Vapour optical depth

To be able to interpret the results of any experiments involving a gas reference cell, we need a mathematical expression for the absorption of the gas under the combined broadening conditions. We know that no matter what physical processes are responsible for the formation of a spectral line, the integral of the absorption coefficient over all frequencies must remain constant if the number of atoms remains constant. This can be explained more simply by considering that any given atom can have the appropriate physical properties (i.e., speed, direction) to interact with only one particular frequency. If a spectral line is broadened, then the absorption depth must simultaneously reduce due to there being fewer atoms available to interact at the line centre. From this we can equate equations (4) and (12) thus,

\[
\frac{\lambda_0^2 g_2 N}{8\pi g_1 \tau} = \frac{1}{2} \sqrt{\frac{\pi}{\ln 2}} \kappa_0 \Delta \nu, \tag{13}
\]

and solving for \( \kappa_0 \) produces [12, p 100],

\[
\kappa_0 = \frac{2}{\Delta \nu} \sqrt{\frac{\ln 2}{\pi}} \frac{\lambda_0^2 g_2 N}{8\pi g_1 \tau}, \tag{14}
\]

which is the maximum absorption possible. This can be combined with the expected line profile to produce the final value for \( \kappa_\nu \). We have already seen such an example in equation (11) where for a line profile dominated by Doppler broadening \( \kappa \), has a Gaussian profile.

The absorption coefficient and thickness in equation (2) can be combined into one term \( \tau_{\nu} \), known as the optical depth,

\[
\tau_\nu = \int I_0 e^{-\kappa_\nu d\nu}, \tag{15}
\]

where, as before, \( I_0 \) is the intensity of incident light, and \( I_\nu \) is the intensity of the transmitted light. Unit optical depth is therefore defined as the optical thickness that reduces the photon flux by a factor of \( 1/e \). It should be noted that \( \tau_\nu \) is specifically a different quantity from \( \tau \) the lifetime of the excited state.

We know that the 769.898 nm line profile formed by potassium vapour is dominated by Doppler broadening, and so equation (11) is valid to describe the distribution. In order to evaluate \( \kappa_\nu \), we need to know the value of all the terms in equation (14)—temperature \( T \), the atomic mass \( m \), the frequency and wavelength of the line centre \( \nu_0 \) and \( \lambda_0 \), the number density of absorbing atoms \( N \), the lifetime of the excited state \( \tau \), and the degeneracy of the \( 4^2P_2 - 4^2S_2 \) energy levels \( g_1 \) and \( g_2 \), respectively.

We already know the lifetime \( \tau \) to be 27 ns, the atomic mass to be 39.0983 u, the central wavelength to be 769.898 nm, and it may be shown [12, p 97] that the ratio \( g_2/g_1 \) is unity. The temperature of the reference cell is controlled, and so the only remaining term is the number density. We can determine the number density based on the vapour pressure, since as we saw earlier it depends only on the temperature and not on the amount of physical material.

The vapour in a gas reference cell can be treated as an ideal gas since the pressure is by design very low. The cells are evacuated and baked out before being filled with a small amount of potassium. Since the pressure is low, there will be few interactions between particles. The ideal gas law is defined as,

\[
pV = \frac{Nk_BT}{p}, \tag{16}
\]

where \( p \) is the pressure, \( V \) the volume, \( N \) the number of atoms or molecules, \( k_B \) the Boltzmann constant, and \( T \) the temperature. If we combine the number of atoms and the volume into one parameter to form the number density \( n(T) \), and define the pressure in terms of temperature then equation (16) simplifies to,

\[
n(T) = \frac{p(T)}{k_BT}, \tag{17}
\]

which depends only on the vapour pressure and the temperature.

Previous independent measurements have been made [14, 15] of the vapour pressure of potassium at various temperatures. These data have been used to fit a polynomial in log space,

\[
p_{\text{vapour}} = e^a T^{b+c} T^{d}, \tag{18}
\]

where \( p_{\text{vapour}} \) is the vapour pressure and \( T \) is the temperature in Kelvin. The values of the four fit coefficients are shown in table 1. A plot of results from this model against the original data are shown in figure 2. The model residuals are all within \( \pm 5\% \) of the original value, with an upper limit to the fit of 449 K (175°). For a typical vapour temperature of 100°C the number density required is \( 4.9 \times 10^{17} \) m\(^{-3}\). This is equivalent to \( 3.2 \times 10^{-8} \) kg of potassium—if you can see solid potassium in the cell then there is enough to form the required vapour.

We now have everything in place to be able to calculate the optical depth of a potassium vapour from equation (15). We know all of the parameters required to calculate the absorption coefficient \( \kappa_0 \) in equation (14) by determining the

<p>| Table 1: Potassium vapour pressure model coefficients. |
|-----------------|-----------------|-----------------|</p>
<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Value</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>( a )</td>
<td>( 6.005 \times 10^{-7} )</td>
<td>( 8.747 \times 10^{-8} )</td>
</tr>
<tr>
<td>( b )</td>
<td>( -8.912 \times 10^{-4} )</td>
<td>( 1.007 \times 10^{-4} )</td>
</tr>
<tr>
<td>( c )</td>
<td>( 4.890 \times 10^{-1} )</td>
<td>( 3.840 \times 10^{-2} )</td>
</tr>
<tr>
<td>( d )</td>
<td>( -9.555 \times 10^{-5} )</td>
<td>( 4.844 )</td>
</tr>
</tbody>
</table>
We used a Tunable Diode Laser (TDL) manufactured by Toptica, which is a tunable diode laser. The model was verified by probing a potassium vapour cell using a tunable diode laser.

5. Laser calibration

We used a Toptica DLC pro tunable diode laser, which is a Littrow-style external cavity diode laser (EDCL) [16]. The installed laser diode has an emission spectrum and tuning range of 765–805 nm. The primary tuning mechanism is by altering the angle of incidence of the grating forming the external cavity, which for coarse adjustment is done using a micrometer screw, and for fine adjustment by varying the applied voltage to a piezo actuator. Tuning can also be achieved by changing the diode drive current and temperature. The diode suffers mode-hopping as the tuning parameters are adjusted, but this can be mitigated by varying all parameters simultaneously. The typical mode-hop-free tuning-range (MHFTR) is quoted at 20–50 GHz, which at a wavelength of 770 nm is equivalent to 40–98 pm. Achieving this range can be tricky due to the interaction of all the various tuning methods. The typical line width achieved by a Littrow-style ECDL over a duration of 5 μs is 10–300 kHz, which again at a wavelength of 770 nm is less than 0.6 fm. The main contributions to the line width are electronic noise, acoustic noise, and other vibrations that affect the cavity length.

The output of the ECDL has no intrinsic wavelength calibration, except that the wavelength must be somewhere within the broadband output of the model of installed laser diode. In order to coarse-tune the laser to approximately 769.9 nm the output wavelength was measured using an Agilent 86142B optical spectrum analyser [17], shown in figure 3. The 86142B has a resolution bandwidth (RBW) of 0.06 nm and so the measured laser line width is considerably broadened. This resolution is sufficient to allow use of the coarse manual micrometer screw adjustment to ensure the required wavelength is positioned within the narrow scan range of the piezo actuator.

The resolution is insufficient to tune the wavelength precisely to the desired absorption line, but once coarse calibration is achieved simply scanning between the piezo limits allows the absorption line to be found. In order to calibrate the width and depth of the absorption line at varying temperature, it is necessary to calibrate the piezo voltage in terms of wavelength and to normalise the beam intensity. This calibration is non-trivial and we will now go on to discuss the steps required to achieve the final overall calibration.

Since BiSON spectrophotometers use a magnetic field to Zeeman split the reference absorption line and produce two separate instrumental passbands, this technique can be used to produce a known wavelength separation and so calibrate the piezo. Figure 4 shows the two components of the Zeeman split absorption line with the cell heated to 90 °C in a 0.3 T longitudinal magnetic field. The beam intensity is not uniform across the piezo scan due to a drive-current feed-forward mechanism employed to increase the MHFTR of the diode laser. It is imperative that the diode does not mode-hop during the scan since this would result in different wavelength calibrations either side of the mode-hop, destroying the overall calibration. The feed-forward adjusts the drive-current.
proportionally with the piezo position-voltage by a factor of $-0.32 \text{ mA V}^{-1}$, which helps prevent mode-hopping but has the undesired side-effect of changing the beam intensity. If a mode-hop continues to appear at an inconvenient wavelength, then the temperature of the diode can be adjusted to move the mode-hop elsewhere. The mean drive-current and detector-gain has to be selected carefully to ensure that the current always stays above the lasing threshold of $10^9 \text{ mA}$, but also that the beam intensity does not exceed the dynamic range of the detector throughout the whole piezo scan range. Once a mode-hop-free scan has been achieved with a beam intensity that is comfortably within the dynamic range of the detector, a flat-field can be captured and used to normalise the intensity of the scan, shown in figure 5.

We can complete the calibration by making use of the known position of the two Zeeman components, and applying the splitting to the piezo voltages at the measured line centres. The calibrated absorption profiles for eight different cell temperatures are shown in figure 6. There is some evidence of slight misalignment of the polarising filters indicated by differences in absorption depth between the two polarisation states. There is also some nonlinearity in the wavelength scan indicated by a slight difference in width between the two polarisation states. These errors are small and will be mitigated against by fitting the model to both absorption components simultaneously, allowing all equal-and-opposite errors to cancel.

6. Model validation

The laser calibration is dependent on the accuracy and uniformity of the vapour cell longitudinal magnetic field. The field strength at several points inside the cell oven was measured using a Hirst GM04 Gaussmeter, which is factory calibrated using nuclear magnetic resonance to correct for irregularities in the supplied semi-flexible transverse Hall probe. It was found that the target field strength of 0.3 T is achieved only at the cell centre and drops to approximately 0.26 T at the front and rear of the cell oven, as shown in figure 7. The mean field strength is 0.283 T. Due to the variation in field strength, it is not necessary to measure the field strength to high precision, however this does mean that the absorption profile will have an additional broadening factor caused by the non-uniform magnetic field, and the FWHM determined from equation (10) has to be modified to allow an additional degree of freedom.

The resulting final model has been fitted against absorption profiles for all eight vapour temperatures in figure 6. Both absorption components are fitted simultaneously allowing systematic equal-and-opposite errors to cancel. The results are shown in figure 8, where the dotted lines show the measured absorption profile and the solid lines show the results of the fit to the data. The fitted parameters and uncertainties listed in table 2.

All fitted temperatures indicate that the vapour pressure is controlled by the temperature of the solid potassium in the stem of the cell. The temperature of the upper cube of the cell simply has to be higher than the stem and high enough to ensure that deposition of solid potassium onto the windows does not occur. The increasing difference between the model temperature and the stem temperature at higher values is an indication of the difficulties of coupling heat efficiently into the cell. Heating of the stem is achieved by a foil heating element wrapped around the glass, and heat does of course leak into the surrounding chassis as well as heating the cell.
At higher temperatures the losses become more significant and it becomes progressively more difficult to effectively heat the cell, and this is indicated by the real temperature of the vapour as determined from the model being a few degrees below the measured temperature of the stem heating element.

7. Instrumentation parameters

The model can be used to estimate the scattering performance of the cell and the effect of different detector aperture sizes and positions. Figure 9 shows the expected intensity change.
as light passes through the cell determined from equation (2). The absorption coefficient is modelled as monochromatic but with the initial intensity scaled by the expected FWHM to compensate for the differences in spectral bandwidth. The white circle in the centre indicates the typical 6 mm aperture of a scattering detector.

<table>
<thead>
<tr>
<th>Oven temp</th>
<th>Model temp</th>
<th>Broadening factor</th>
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</thead>
<tbody>
<tr>
<td>Stem</td>
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<td>Stem</td>
</tr>
<tr>
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<td>70</td>
<td>50</td>
</tr>
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<td>130</td>
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</tr>
</tbody>
</table>

Figure 9. Absorption through a typical 15 mm BiSON vapour cell at various temperatures. The absorption coefficient is modelled as monochromatic but with the initial intensity scaled by the expected FWHM to compensate for the differences in spectral bandwidth. The white circle in the centre indicates the typical 6 mm aperture of a scattering detector.

centre of the figure indicates the typical 6 mm aperture of a scattering detector, with scattered light perpendicular to the page coming out towards the reader as the beam passes through from left to right. It is clear that at low temperatures there is very little scattered light due to the small absorption coefficient. At high temperatures almost all the light is scattered at the front of the cell and so not captured by the detector. This implies that there will be some optimum temperature at which the measured scattering intensity is greatest. By considering the change in intensity within the area of the white circle, we can estimate the intensity of light scattered away from the beam optical axis. Figure 10 shows the estimated scattering intensity for several aperture sizes and vapour temperatures. If the aperture is equal to the size of the vapour cell then all the light scattered towards the detector is captured, and the intensity continually increases with temperature. As the aperture size is reduced a temperature plateau forms. One might expect that the ideal aperture is as large as possible in order to maximise the intensity of scattered light and so maximise the signal-to-noise ratio. However, there are several reasons why this is not the case. Applying a smaller aperture and causing the temperature plateau to form minimises the effect of fluctuations in vapour temperature, and the temperature-width of the plateau is greatest at smaller apertures. Also, it is imperative to eliminate non-resonantly scattered light from reaching the detector, such as specular reflections from the cell glass especially at the edges and corners of the cell, and again this is best achieved via small apertures effectively acting as a baffle.
vapour cells and commercially available alternatives. Previously the optical depth of the cell, and the location within the cell where most of the scattering occurs, has not been known precisely. This information is essential when designing new instrumentation, such as the prototype next generation of BiSON spectrophotometers (BiSON:NG [8]), where the aim is to make use of off-the-shelf components to simplify and miniaturise the instrumentation as much as practical.

9. Open data

All code and data are freely available for download from the University of Birmingham eData archive [18], and also from the source GitLab repository [19].

Acknowledgments

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References


Figure 11. Vapour cell scattering intensity profiles at a range of temperatures. The profile asymmetry seen at temperatures above the ideal temperature is a result of the inhomogeneity of the magnetic field.

The scattering detectors used in most BiSON instrumentation employ 6–10 mm circular apertures which suggests that the maximum intensity will be found at a stem temperature of approximately 80 °C–90 °C. Many BiSON instruments run at a stem temperature of 90 °C and a cube temperature of 110 °C and so these results agree with expectation based on experience. At this temperature the optical depth is approximately one if measured from the front of the cell to the centre, or approximately two from the front of the cell to the rear.

Figure 11 shows the scattering profiles taken simultaneously with the absorption profiles shown in figure 6 over a range of vapour cell temperatures, and the intensity peaks at approximately 80 °C–90 °C as expected. The profile asymmetry seen at high temperatures is a result of the inhomogeneity of the magnetic field. At lower temperatures, light is detected from across the whole aperture, and the peaks are centred at the wavelengths corresponding to the splitting produced by the mean field strength. At higher temperatures, the scattering is dominated towards the front of the cell within the weaker part of the field, and not seen by the detector. The detector captures only the remaining small fraction of light at the wavelength corresponding to the higher field strength at the centre of the cell, leading to the observed offset weighted towards higher field strength.

8. Conclusion

We have developed a model of a BiSON potassium vapour cell and validated the output of the model using a tunable diode laser, where the model was found to effectively reproduce the properties of the cell. Previously the ideal temperature working point was determined empirically, and the result found here now puts the choice on a firm footing.

The model can be used to assess vapour cells of different size and shape, and determine the ideal operating vapour temperature and configuration of detectors, allowing comparison of expected performance between existing BiSON...


