Test of CP-invariance of the Higgs boson in vector-boson fusion production and its decay into four leptons
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Test of CP-invariance of the Higgs boson in vector-boson fusion production and in its decay into four leptons

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ABSTRACT: A search for CP violation in the decay kinematics and vector-boson fusion production of the Higgs boson is performed in the $H \to ZZ^* \to 4\ell$ ($\ell = e, \mu$) decay channel. The results are based on proton-proton collision data produced at the LHC at a centre-of-mass energy of 13 TeV and recorded by the ATLAS detector from 2015 to 2018, corresponding to an integrated luminosity of 139 fb$^{-1}$. Matrix element-based optimal observables are used to constrain CP-odd couplings beyond the Standard Model in the framework of Standard Model effective field theory expressed in the Warsaw and Higgs bases. Differential fiducial cross-section measurements of the optimal observables are also performed, and a new fiducial cross-section measurement for vector-boson-fusion production is provided. All measurements are in agreement with the Standard Model prediction of a CP-even Higgs boson.

KEYWORDS: Hadron-Hadron Scattering, Higgs Physics

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The observed baryon asymmetry of the universe is one of the important open questions of physics today. To explain this, the Sakharov criteria [1] require sufficient violation of
combined charge conjugation and parity (CP) invariance. The only known source of CP violation in the Standard Model (SM) is a complex phase in the Cabibbo-Kobayashi-Maskawa (CKM) matrix \[2, 3\] for quark mixing. Other sources of CP violation may exist in the neutrino sector or the strong interaction. The CKM complex phase does not lead to a sufficient amount of CP violation to explain the baryon asymmetry. This motivates the exploration of potential new sources of CP violation, as performed in the present analysis of the production and decay of the Higgs boson \[4, 5\].

The spin-parity \((J^P)\) of the Higgs boson is predicted to be \(0^+\) with even C-parity by the Standard Model. Any sign of CP-violation in the production or decay of the Higgs boson at the current level of sensitivity would therefore be an unambiguous indication of beyond the Standard Model phenomena (BSM). With \(25 \text{fb}^{-1}\) of proton-proton collision data collected from the LHC with a centre-of-mass energy, \(\sqrt{s}\), of 7 and 8 TeV, the ATLAS and CMS experiments excluded the pure spin-parity states \(0^-, 1^+, 1^-, 2^+\) and \(2^-\) at more than 99\% confidence level (C.L.) based on the observed Higgs boson decays (\(\gamma\gamma, ZZ, WW\)) \[6–9\].

These results also provided the first limits on a possible CP-odd contribution to Higgs boson vector-boson couplings (\(HVV\)) in Higgs boson decays. With the same data set there was a first search for CP-odd \(HVV\) couplings in vector-boson fusion (VBF) production in the \(H \rightarrow \tau\tau\) decay channel \[10\] and associated \(VH\) production in the \(bb\) decay channel \[11\]. With an increased integrated luminosity of \(139 \text{fb}^{-1}\) of LHC collisions at \(\sqrt{s} = 13\) TeV, an order of magnitude more Higgs boson candidates were collected. Constraints on CP-invariance were tightened for the \(HVV\) couplings and extended to Higgs Yukawa couplings to fermions, for example in \(H \rightarrow \tau\tau\) decays and associated Higgs boson top pair (\(ttH\)) production in both the diphoton and \(bb\) decay channels, and other channels \[12–26\].

For the \(H \rightarrow ZZ^* \rightarrow 4\ell\) channel \((\ell = e, \mu)\), constraints on CP-even and CP-odd BSM couplings have been set with \(139 \text{fb}^{-1}\) at \(\sqrt{s} = 13\) TeV for Higgs boson production cross-section measurements, by comparing observations with SM expectations \[18, 27\]. However, potential deviations of the Higgs boson production cross-sections could be explained by either a CP-even or CP-odd BSM coupling, and would not distinguish between them. The present analysis searches for a visible CP-odd effect in VBF production and the \(H \rightarrow ZZ^* \rightarrow 4\ell\) decay by employing optimal observables \[9, 28–31\], which are CP-odd by construction, with \(139 \text{fb}^{-1}\) of data collected at \(\sqrt{s} = 13\) TeV by the ATLAS detector \[32\]. About 200 Higgs bosons decaying into four leptons are expected to be reconstructed in the detector for this sample, including about 10 events in a VBF production phase space.

The optimal observables are constructed from matrix elements of the Standard Model effective field theory (SMEFT) \[33–35\], a specific formalism of an effective field theory (EFT). An optimal-observable distribution is symmetric for the CP-even Higgs boson and becomes asymmetric when contributions from CP-odd BSM couplings are present. There are three dimension-six operators with BSM CP-odd couplings in the SMEFT Lagrangian that can contribute to VBF production or the \(H \rightarrow ZZ^* \rightarrow 4\ell\) decay, each associated with a Wilson coefficient. In this analysis, these three operators are considered in the Warsaw basis, and each operator has a different sensitivity to VBF production and the \(H \rightarrow ZZ^* \rightarrow 4\ell\) decay. The optimal-observable distributions are used in two ways: the observed distributions are used directly to constrain CP-odd couplings, and they are unfolded to a fiducial phase space, complementing the \(H \rightarrow ZZ^* \rightarrow 4\ell\) differential cross-section measurements in ref. \[36\].
to allow reinterpretations in different models. Since the present search is looking for a distinct CP-odd signature, the extraction of the CP-odd coupling constraints is based only on the shape of the optimal-observable distributions, ignoring the expected change in cross-section. Including cross-sections has only a small effect on the constraints, as shown in section 8.1. The fiducial phase space for the unfolded optimal-observable distributions is the same as for the $H \to ZZ^* \to 4\ell$ fiducial measurement [36], and is dominated by gluon-gluon fusion (ggF) production that allows constraints on CP-odd operators which are sensitive to the $H \to ZZ^* \to 4\ell$ decay. Extracting the differential distributions for the VBF optimal observables in a VBF-enriched fiducial phase space would improve the sensitivity to the CP-odd operator that is more sensitive to VBF production, however this is not yet within statistical reach. Instead this paper presents an inclusive cross-section measurement in a VBF fiducial phase space. This measurement can be used to constrain BSM models affecting the Higgs boson to $ZZ^*$ vertex through their expected impact on event rates.

2 Theoretical framework and analysis methodology

While the analysis is designed to be sensitive to signatures of CP violation independently of a particular BSM physics model, the SMEFT framework is used to guide the analysis strategy and interpret the results. This framework also provides the coupling scenarios used to define the optimal observables at the centre of the analysis strategy. Both the SMEFT framework and the optimal-observable formalism are described in more detail in the following. In addition, the known dependence of cross-sections on the BSM couplings in the framework of SMEFT is exploited to parameterize the signal prediction in the direct BSM coupling measurement as described in section 2.3.

2.1 EFT framework

In SMEFT, a complete set of higher-order-in-mass operators invariant under the SM gauge group $SU(3)_C \times SU(2)_L \times U(1)_Y$ is built from the SM fields [35]. If the dimension-five operator is ignored because it violates lepton number [37], the leading contributions to physical observables are expected to be from dimension-six operators. In this case the SMEFT Lagrangian becomes:

$$L_{\text{SMEFT}} = L_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} O_i^{(6)},$$

where $O_i^{(6)}$ are the operators of mass-dimension six, which are invariant under the SM gauge group, the $c_i$ are the corresponding dimensionless real coupling constants, the Wilson coefficients, and $\Lambda$ is the energy cutoff scale of the effective field theory.

There are several complete sets of these dimension-six operators. One such set, used in many existing LHC EFT interpretations [18, 38–41], is the Warsaw basis [34, 42]. Only three CP-odd operators contributing to the $HVV$ vertex for both VBF production and vector-boson decays are considered, and are listed in the first three rows of table 1.

This analysis is sensitive to each CP-odd coupling normalised by $(1 - c_{\text{even}})$ where $c_{\text{even}}$ is a linear combination of CP-even couplings that leave the shapes of the analysis observables invariant. Since these CP-even couplings are assumed to be zero, the measurements in the rest of this paper are simply denoted by the CP-odd coupling.
Table 1. SMEFT CP-odd dimension-six operators in the Warsaw and Higgs bases relevant for the measurement of CP-invariance in the $H \rightarrow ZZ* \rightarrow 4\ell$ decay channel. The gauge field strength tensors are denoted $W_{\mu\nu}^I$ and $B_{\mu\nu}$, while $\Phi$ is the scalar doublet Higgs boson field. The photon and Z-boson field strength tensors after electroweak symmetry breaking are denoted as $A_{\mu\nu}$ and $Z_{\mu\nu}$, respectively, and $h$ denotes the massive Higgs field after electroweak symmetry breaking. Combinations of couplings in one basis can be translated into equivalent combinations of couplings from the other basis that describe the same phenomena [43, 44]. The same phenomena are described by an alternative complete set of operators, based on the mass eigenstates after the spontaneous symmetry breaking instead of the fields of the unbroken gauge symmetry. This formulation is expressed in terms of the physical states of SM gauge bosons $W^+, W^-, Z,$ and $\gamma$. With these operators it is possible to build another basis [43, 44] that can probe the effects of the Higgs boson couplings to other particles, and is more closely linked to experimental physical observables than the Warsaw basis. It is called the Higgs basis in which three independent CP-odd couplings, listed in table 1 together with their operators, mediate the same phenomena as the Warsaw-basis couplings. Each coupling of one basis can be expressed as a linear combination of the three couplings in the other basis (see appendix A).

Finally, a common parameterization used in existing experimental searches for CP-violation at the $HVV$ vertex [10, 38] assumes a single BSM CP-odd Higgs boson coupling denoted by $\tilde{d}$. In [10], it was considered that the different contributions from the various electroweak gauge-boson fusion processes could not be distinguished experimentally, and assumed that the BSM CP-odd Higgs boson couplings $c_{H\tilde{W}}$ and $c_{H\tilde{B}}$ in the Warsaw basis are equal, leading to the remaining coupling $c_{H\tilde{W}\tilde{B}}$ being zero. The CP-odd parameter $\tilde{d}$ is related to the Warsaw-basis couplings by the parameterization $c_{H\tilde{W}} = c_{H\tilde{B}} = \frac{\Lambda^2}{v} \tilde{d}$, where $v$ is the Higgs boson vacuum expectation value. In the Higgs basis, it is equivalent to the direction $\tilde{c}_{z\gamma} = 0$, $\tilde{c}_{\gamma\gamma} = \sin^2 \theta_W \cos^2 \theta_W \tilde{c}_{zz}$, where $\theta_W$ is the Weinberg angle.

It should be noted that, in this framework, the coupling strength associated to the SM-like coupling itself is not modified.

In the following, the focus is on interpretations with the three couplings in the Warsaw-basis framework, but results are also provided for the Higgs basis and $\tilde{d}$ to facilitate comparisons. Constraints are set on a set of benchmark scenarios where one or two of the...
The aforementioned CP-odd coupling is none-zero at a given time, assuming that all other EFT couplings are zero.

2.2 Optimal observables

The cross-section for the combination of a set of CP-odd couplings, \( c_i \), within the SM is proportional to the square of the matrix element composed of the sum of the individual matrix elements:

\[
|\mathcal{M}|^2 = \left| \mathcal{M}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{M}_{\text{BSM},i} \right|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2 \sum_i \frac{c_i}{\Lambda^2} \Re(\mathcal{M}_{\text{SM},i}^* \mathcal{M}_{\text{BSM},i}) + \sum_i \sum_j \frac{c_i c_j}{\Lambda^4} \Re(\mathcal{M}_{\text{BSM},i}^* \mathcal{M}_{\text{BSM},j}).
\]

The expanded sum has a first term that is the squared SM matrix element, and a last term that represents the quadratic BSM contributions and the interference between BSM terms. These first and last terms are CP-even. The middle term is composed of the cross terms between the SM and BSM couplings (\( \Re \) is the real part) and represents the interference between the SM and BSM processes. This term is CP-odd and therefore suitable as a probe for CP violation.

Normalising the interference term by the SM term forms an ‘optimal observable’ for each coupling, which can be used to detect a CP asymmetry:

\[
\mathcal{O}_i = \frac{2 \Re(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{BSM}})}{|\mathcal{M}_{\text{SM}}|^2}.
\]

These observables are CP-odd by construction, implying a symmetric distribution with a vanishing mean in the absence of CP violation. Any asymmetry observed in the distribution of the optimal observables would be direct evidence for CP-violation in the HVV coupling. This property is not shared by other CP-even optimal observables constructed from squared matrix elements, and motivates the choice of the interference-based observable definition in this search. The LO matrix elements entering the optimal observable are calculated using MadGraph5_AMC@NLO [45] with the NNPDF2.3LO [46] parton distribution function (PDF) set. Two types of optimal observables are considered. Production-level optimal observables reflect the VBF production vertex, not considering the Higgs boson decay. They are constructed using VBF production matrix elements calculated from the reconstructed four-momentum of the Higgs boson candidate and the two leading jets assumed to form the VBF topology. The VBF production matrix element calculation is a PDF-weighted sum of matrix elements for several partonic processes. In addition, decay-level optimal observables are constructed using the matrix element describing the Higgs boson decay from the reconstructed four-momentum of the four decay leptons. These decay-level optimal observables are agnostic to the production vertex, and only a single matrix element is needed for an optimal-observable evaluation. The matrix element for decay-level optimal observables is evaluated separately for same flavour (4\( \mu \), 4e) and different flavour (2e2\( \mu \)) decays to account for the differences of the CP-asymmetry from final state interference. For each type of optimal observable, there

\[2 \Re(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{BSM}}) = \mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{BSM}} + \mathcal{M}_{\text{SM}} \mathcal{M}_{\text{BSM}}^*.\]
is a choice of which BSM coupling to assume when calculating the interference term. A dedicated observable is constructed for each of the seven EFT coupling parameters, three for each basis and one for $\tilde{d}$. While each observable is sufficiently general to be sensitive to CP-violating effects from different couplings to those assumed in its construction, the sensitivity to a CP-odd effect of a particular coupling is maximized using an observable made with the same coupling.

### 2.3 Morphing method

The distribution of the optimal observable for a signal process with an arbitrary combination of active EFT couplings is predicted as the weighted sum of a limited number of simulated predictions, described in section 4. The weights entering the sum are polynomial functions of the assumed EFT couplings, calculated using the morphing method [9, 18, 47]. This relies on the fact that, as shown in eq. (2.2), the cross-section in each phase space bin, $\sigma$, is a polynomial function of the EFT coupling when excluding effects on the Higgs boson total width,

$$
\sigma = \sum_{k=0}^{4} c^k A_k = \vec{c} \cdot \vec{A}, \quad \text{with} \quad \vec{c} = (1, c, c^2, c^3, c^4) \quad \text{and} \quad \vec{A} = (A_0, A_1, A_2, A_3, A_4)
$$

where $c$ is the EFT coupling under study and $A_k$ denotes the component of the cross-section proportional to the $k$th power of the BSM coupling. If up to two $HVV$ vertices are present, one for production and one for the decay, the maximum power in the BSM coupling is 4 as assumed above. The same method applies to combinations of multiple active couplings and to different numbers of $HVV$ vertices. In this case, $\vec{c}$ contains all combinations of powers of the BSM couplings appearing in the amplitude, and $\vec{A}$ the corresponding cross-section contributions. The dimensionality of $\vec{A}$ and $\vec{c}$ then corresponds to the number of such unique coupling power combinations, including the case without any BSM couplings (SM-only amplitude). For example, for one vertex and three BSM couplings denoted $c_1$, $c_2$, and $c_3$, there would be ten elements $(1, c_1, c_2, c_3, c_1^2, c_2^2, c_3^2, c_1c_2, c_1c_3, c_2c_3)$, and for two vertices and three BSM couplings, the dimensionality would increase to 35.

A set of simulated samples for different combinations of coupling values $\vec{c}_{\text{Sample}_i}$ can be interpreted as a vector of cross-sections, which depends on the coupling values via a matrix $C$,

$$
\vec{\sigma}_{\text{simulated}} = C \times \vec{A}, \quad \text{with} \quad C = [\vec{c}_{\text{Sample}_1}, \vec{c}_{\text{Sample}_2}, \ldots] .
$$

Inverting this relation, which is only possible if the number of simulated samples is equivalent to the dimensionality of $\vec{A}$, and inserting into eq. (2.3) allows the cross-section for an arbitrary coupling set to be expressed as a linear combination of the existing, simulated cross-sections:

$$
\sigma = \vec{c} \cdot \vec{A} = \vec{c} \cdot \left( \vec{C}^{-1} \cdot \vec{\sigma}_{\text{simulated}} \right) = \sum_j \left( \vec{C}^{-1}_{j} \cdot \vec{c} \right) \sigma_j
$$

where the $w_j(\vec{c})$ are the weights to be applied to each of the simulated samples to obtain the signal prediction.

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These manifest in a rate change and can be factorised out of the consideration for the morphing method.
3 ATLAS detector

The ATLAS detector at the LHC is a multipurpose particle detector with a forward-backward symmetric cylindrical geometry and a near $4\pi$ coverage in solid angle.\(^4\) It consists of an inner tracking detector (ID) surrounded by a thin superconducting solenoid providing a 2 T axial magnetic field, electromagnetic and hadron calorimeters, and a muon spectrometer (MS). The ID covers the pseudorapidity range $|\eta| < 2.5$. It consists of silicon pixel, silicon microstrip, and transition radiation tracking detectors. Lead/liquid-argon (LAr) sampling calorimeters provide electromagnetic (EM) energy measurements with high granularity. A steel/scintillator-tile hadron calorimeter covers the central pseudorapidity range ($|\eta| < 1.7$). The endcap and forward regions are instrumented with LAr calorimeters for both the EM and hadronic energy measurements up to $|\eta| = 4.9$. The MS surrounds the calorimeters and is based on three large superconducting air-core toroidal magnets with eight coils each. The field integral of the toroids ranges between 2.0 and 6.0 Tm across most of the detector. The MS includes a system of precision tracking chambers and fast detectors for triggering. A two-level trigger system is used to select events. The first-level trigger is implemented in hardware and uses a subset of the detector information to accept events at a rate below 100 kHz. This is followed by a software-based trigger that reduces the accepted event rate to 1 kHz on average, depending on the data-taking conditions. An extensive software suite \([48]\) is used in data simulation, in the reconstruction and analysis of real and simulated data, in detector operations, and in the trigger and data acquisition systems of the experiment.

4 Data set and event simulation

This measurement uses data from proton-proton collisions with a centre-of-mass energy of 13 TeV collected between 2015 and 2018 using single-lepton, dilepton, and trilepton triggers \([49, 50]\) as detailed in ref. \([27]\). The combined efficiency of these triggers is approximately 98%, 99%, 97%, and 99% for the $4\mu$, $2e2\mu$, $2\mu2e$, and $4e$ final states,\(^5\) respectively, for the simulated $H \rightarrow ZZ^* \rightarrow 4\ell$ events passing the event selection described in section 5 (assuming $m_H = 125$ GeV). After data-quality requirements are imposed, the integrated luminosity of the data sample is 139 fb\(^{-1}\) \([51]\).

Details of the SM Higgs boson Monte Carlo (MC) samples used in this analysis can be found in refs. \([27, 36]\). Higgs boson production via the ggF process was modelled at next-to-leading-order (NLO) accuracy in the strong coupling constant $\alpha_s$ using the POWHEG NNLOPS generator \([52–60]\) with the PDF4LHC15NLO set of PDFs \([61]\). Higgs bosons produced via VBF or in association with a vector boson ($VH$) or in association with a top-quark pair ($ttH$), were simulated at NLO accuracy with the POWHEG BOX generator \([54–56]\), using the PDF4LHC15NLO PDF set. Higgs boson production in association with a top quark ($tH$)

\(^4\)ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the centre of the detector and the $z$-axis along the beam pipe. The $x$-axis points from the IP to the centre of the LHC ring, and the $y$-axis points upwards. Cylindrical coordinates ($r, \phi$) are used in the transverse plane, $\phi$ being the azimuthal angle around the $z$-axis. The pseudorapidity is defined in terms of the polar angle $\theta$ as $\eta = -\ln \tan(\theta/2)$. Angular distance is measured in units of $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$.

\(^5\)The final state notation represents the mass pair closest to the $Z$ mass followed but the other pair.
was simulated at NLO accuracy using the \textsc{MadGraph5}_\textsc{aMC}@NLO generator \cite{madgraph, aMC@NLO} with the NNPDF3.0 PDF set \cite{nnpdf30}. The production of a Higgs boson in association with a bottom quark pair (\(bbH\)) was simulated at NLO with \textsc{MadGraph5}_\textsc{aMC}@NLO \cite{madgraph, aMC@NLO}, using the CT10 NLO PDF \cite{ct10}. For all signal processes, the \textsc{EvtGen}1.6.0 generator \cite{evtgen} was used for the simulation of the bottom- and charm-hadron decays. Correspondingly, the \textsc{Pythia}8 generator \cite{pythia8} was used for the \(H \rightarrow ZZ^* \rightarrow 4\ell\) decay and for parton showering, hadronization, and simulation of the underlying event. These samples were normalized to cross-sections obtained from the most recent predictions provided by the LHC Higgs Working Group \cite{lhchiggs}.

BSM Higgs boson samples with active CP-odd EFT couplings were generated for different coupling values at leading order in \(\alpha_s\) with \textsc{MadGraph5}_\textsc{aMC}@NLO and the NNPDF2.3 PDF set. All diagrams contributing to the \(HVV\) vertex for both VBF/\(VH\) production and vector-boson decays (\(Z(Z^*)/\gamma^*\)) into four lepton final state were generated. The generation was performed using the effective Lagrangian of the SMEFT framework implemented via the SMEFTsim\_A\_U35\_MwScheme\_UFO\_v2.1 \cite{smear, smeftsim} model. The CKKW-L method \cite{ckkw} was used for the jet merging in the ggF process. The SMEFT v2 model with a U(3)\(^5\) flavour symmetry and the \(m_W\) input scheme was used. The EFT cutoff scale was set to \(\Lambda = 1\) TeV. Separate samples were generated for the ggF production mode and for the combination of the VBF and \(VH\) production modes. Each sample was generated at a three-dimensional coupling point for values of the Warsaw basis of table 1, which also corresponds to a single point in the three Higgs-basis couplings. The choice of simulated coupling values was optimized to maintain high statistical power throughout the three-dimensional coupling space using the morphing method described in section 2. The optimal observable matrix elements were evaluated with \textsc{MadGraph5}_\textsc{aMC}@NLO with the HC\_UFO model and LHAPDF6 \cite{lhapdf6}.

The non-resonant \((Z(Z^*)/\gamma^*)(Z(Z^*)/\gamma^*)\) background, hereafter denoted as \(ZZ^*\), is separated into quark-initiated \(q\bar{q} \rightarrow ZZ^*/gq \rightarrow ZZ^*\), gluon-initiated \(gg \rightarrow ZZ^*\), and vector-boson scattering (EW \(ZZ\)) production, and was modelled using the \textsc{Sherpa} 2.2.2 generator \cite{sherpa} with the NNPDF3.0NNLO \cite{nnpdf30} PDF set. The \(q\bar{q} \rightarrow ZZ^*/gq \rightarrow ZZ^*\) process was generated using matrix elements at NLO accuracy in QCD for up to one additional parton and at LO accuracy for up to three additional parton emissions. NLO EW corrections were applied as a function of the invariant mass of the \(ZZ^*\) system, \(m_{ZZ^*}\) \cite{ewcorr1, ewcorr2}. The samples for the gluon-induced processes \((gg \rightarrow ZZ^*)\) were generated using LO-accurate matrix elements for up to one additional parton emission. A NLO QCD calculation \cite{ewcorr3, ewcorr4} was used to correct the overall cross-section for this process. The EW \(ZZ\) contribution was simulated at LO precision in QCD.

These samples were normalized to cross-sections obtained directly from the \textsc{Sherpa} simulation. Alternative \(q\bar{q} \rightarrow ZZ^*\) samples, produced with the \textsc{Powheg Box} v2 and \textsc{MadGraph5}_\textsc{aMC}@NLO generators, are used to study the theoretical modelling of the systematic uncertainties. For the alternative samples, the \textsc{Pythia}8 generator was used for parton showering, hadronization, and simulation of the underlying event.

Background events from \(WZ\) and \(t\bar{t}\) processes were generated with \textsc{Powheg Box} v2, while contributions from \(Z\) bosons produced in association with jets were simulated using the \textsc{Sherpa} 2.2.1 generator. Minor contributions from processes with three electroweak bosons, denoted by \(VVV\), were modelled using \textsc{Sherpa} 2.2.2. Small backgrounds originating from
top-quark production in association with one or more electroweak bosons or additional top quarks, such as $t\bar{t}Z$, $tWZ$, $t\bar{t}WW$, $ttWZ$, $ttZZ$, $ttt$, and $tt\bar{t}$ (denoted by $tXX$), were simulated using the MadGraph5_aMC@NLO generator. The Pythia 8 generator was used for parton showering, hadronization, and simulation of the underlying event.

Generated events were processed through the ATLAS detector simulation [78] within the GEANT4 framework [79] and reconstructed in the same way as collision data. Additional proton-proton interactions in the same or neighbouring bunch crossings, referred to as pileup, were included in the simulation. The pileup events were generated using the Pythia 8 generator with the A3 set of tuned parameters [80] and the NNPDF2.3LO PDF set.

5 Event reconstruction, selection and backgrounds

5.1 Object reconstruction

Muon candidates are reconstructed using a combination of different algorithms [81]. The reconstruction of muon candidates within $|\eta| < 2.5$ is primarily performed by a global fit to reconstructed tracks in the ID and the MS. In the central detector region ($|\eta| < 0.1$), where the MS has reduced geometrical coverage, muons are also identified by matching a reconstructed ID track to either an MS track segment (‘segment-tagged muons’) or a calorimetric energy deposit consistent with a minimum-ionising particle (‘calorimeter-tagged muons’). Calorimeter-tagged muons are required to have transverse momentum $p_T > 15$ GeV to avoid misidentifying leptons at low $p_T$. For both the segment-tagged and calorimeter-tagged muons, the muon momentum is measured from the ID track alone. In the forward MS region ($2.5 < |\eta| < 2.7$) outside the ID coverage, MS tracks with hits in three MS layers are accepted as ‘stand-alone muons’ and combined with track segments formed from hits in the silicon tracker, if they exist. Additionally, ‘loose’ muon-identification criteria [81] are applied to reject low-quality tracks that have missing hits in the MS or have poor agreement between the reconstructed MS and ID tracks. Muons are required to be isolated by using both calorimeter-based and track-based isolation variables and applying the ‘PFlowLoose’ criteria [81]. They are matched to the hard-scatter vertex candidate by imposing a requirement $|z_0\sin \theta| < 0.5$ mm on their longitudinal impact parameter $z_0$. Cosmic rays are removed using a criterion $|d_0| < 1$ mm on the transverse impact parameter $d_0$.

A reconstructed electron consists of a cluster of energy deposits in the calorimeter and a matched ID track [82]. Variable-size clusters are created dynamically from calorimeter-energy deposits, improving the invariant-mass resolution of the four-lepton system, especially when bremsstrahlung photons are present. Electron ID tracks are fitted using an optimized Gaussian-sum filter [83] that accounts for non-linear effects arising from energy loss through bremsstrahlung. Quality criteria are used to improve the purity of selected electron candidates. The quality of an electron candidate is evaluated by using a likelihood method that employs measurements from the tracking system and the calorimeter system, and quantities that combine both tracking and calorimeter information [83]. The ‘loose’ likelihood criteria, together with track hit requirements, are applied to electron candidates. Electrons are required to be isolated using both the calorimeter-based and track-based isolation variables as
discussed in ref. [27]. They are matched to the hard-scatter vertex using the same requirement as for the muons, $|z_0 \sin \theta| < 0.5 \text{mm}$.

Jets are reconstructed using a particle flow algorithm [84] from noise-suppressed positive-energy topological clusters [85] in the calorimeter using the anti-$k_t$ algorithm [86, 87] with a radius parameter $R = 0.4$. Energy deposited in the calorimeter by charged particles is subtracted and replaced by the momenta of tracks that are matched to those topological clusters. The jet four-momentum is corrected for the non-compensating calorimeter response, signal losses due to noise threshold effects, energy lost in non-instrumented regions, and contributions from pile-up [84, 88, 89]. Jets are required to have $p_T > 30 \text{GeV}$ and $|\eta| < 4.5$. Jets with $p_T$ ranging between 20–60 GeV for $|\eta| < 2.4$ and between 20–120 GeV for 2.5 < $|\eta| < 4.5$ are suppressed if tagged as pile-up using two jet-vertex-tagger multivariate discriminants [90–93].

To avoid the double-counting of particles, a range of overlap removal criteria are applied to the electrons, muons, and jets. If any two leptons share an ID track or, in case of two electrons, have overlapping associated calorimeter energy clusters, only one is retained. Preference is given to higher-$p_T$ leptons and to muons over electrons, unless the muon is identified using only the calorimeter, in which case the electron is maintained. Jets found within $\Delta R < 0.2$ of leptons are removed.

5.2 Event selection

Events are required to contain at least four isolated leptons emerging from a common vertex and forming two pairs of oppositely charged same-flavour leptons. Electrons are required to be within the geometrical acceptance of the ID ($|\eta| < 2.47$) and to have transverse energy $E_T > 7 \text{GeV}$, while muons must be within the geometrical acceptance of the MS ($|\eta| < 2.7$) and have $p_T > 5 \text{GeV}$ (except for calorimeter-tagged muons, as explained in section 5.1). At most one calorimeter-tagged or stand-alone muon is allowed per Higgs boson candidate. The three higher-($p_T$ or $E_T$) leptons in each quadruplet are required to satisfy thresholds of 20, 15, and 10 GeV, respectively. All lepton pairs within the quadruplet must have an angular separation, $\Delta R(\ell, \ell')$, larger than 0.1, and opposite-sign same-flavour pairs must have a mass above 5 GeV to avoid, for example, $J/\psi$ pairs. Contributions from misidentified leptons are reduced by requiring the lepton tracks to have low significances of their transverse impact parameters (less than 3 (5) for $e$ ($\mu$)) and to be compatible with originating from a common vertex. A detailed description of the event selection can be found in ref. [27].

The lepton pair with an invariant mass closest to the $Z$ boson mass in each quadruplet is referred to as the leading dilepton, while the remaining pair is referred to as the subleading dilepton. The selected quadruplets are separated into four subchannels, according to the flavour of the leading and subleading pairs. In order of decreasing expected selection efficiency, they are $4\mu$, $2e2\mu$, $2\mu2e$, and $4e$. Only one quadruplet is selected from each event, based on the mass of the leading dilepton, the final state, and, for events with additional leptons, the largest leading-order squared matrix element for the SM Higgs boson decay, as described in ref. [27]. Finally, final-state radiation photons are searched for in all events following the procedure described in ref. [27]. These photons are found in 4% of the events and their energy is included in the mass computation.
5.3 Backgrounds

The dominant background contribution is non-resonant \( ZZ^* \) production, accounting for approximately 30\% of events in the four-lepton invariant mass, \( m_{4\ell} \), signal region, 115–130 GeV. The evaluation of the non-resonant \( ZZ^* \) is based on MC simulation, with a data-driven normalization obtained using the side-bands of the \( m_{4\ell} \) distribution. The backgrounds from \( Z + \text{jets}, t\bar{t} \) and \( WZ \), denoted by ‘reducible’ in the following, are evaluated from data following the procedures described in [27, 36]. The tri-boson (\( WWZ, WZZ \) and \( ZZZ \)) and \( t\bar{t}X \) backgrounds are evaluated from simulation and together with the reducible backgrounds amount to about 5\% of the events in the signal region.

6 Overview of analysis

6.1 Direct coupling measurement

A binned maximum-likelihood fit to the observed distributions of optimal observables allows the EFT coupling parameters under consideration to be directly measured. The measurement targets CP-violating effects on the optimal-observable shapes and is optimized to be insensitive to any potential CP-even signature of BSM physics, which would only affect event rates. To achieve this, the impact of the EFT couplings on the event rates predicted by the signal model is not used in the fit, and only the change in the shapes of the optimal-observable distributions as a function of the BSM couplings is exploited. This is achieved by multiplying the predicted rates of the SM signal prediction and background by additional (a priori, unphysical) free parameters in the statistical model, and then allowing these to float when fitting the model to the data.

The optimal-observable distribution for the signal is predicted using the morphing method described in section 2. In the case of production-level optimal-observable distributions, only the VBF and \( VH \) Higgs boson production modes are sensitive to BSM effects and considered as signal. The observable shape for any combination of the three EFT couplings considered here is predicted using 35 simulated samples with different injected EFT coupling values covering both processes. The number of samples is determined by the number of unique coupling combinations for three BSM couplings and two (production and decay) \( HVV \) vertices as discussed for eq. (2.3) in section 2.3.

All Higgs boson production modes represent a signal when considering decay-level optimal-observable distributions. For \( ggF \), the shape of the observable distributions is predicted using a set of 10 simulated samples. Due to the negligible magnitude of the \( ttH, tH, \) and \( bbH \) contributions in the study of decay-level observable distributions, no dedicated morphing is performed for them, and their shape is taken from the \( ggF \) prediction, with the combined yield accounted for by the free signal rate in the fit. The shape of the decay observable distributions for VBF and \( VH \) events is predicted with the same 35 samples described above.

For most of the background processes, the optimal-observable shapes are derived directly from the SM MC samples described in section 4. This is the case for the dominant \( ZZ^* \) continuum background as well as the minor \( t\bar{t}Z/t\bar{t}WW \) and triboson background contributions. The background from events with non-prompt leptons has its optimal-observable shape derived from its data-driven analysis, but plays a negligible role in the measurement. When the \( ggF \),
Figure 1. Illustration of the regions used in the direct BSM coupling measurement. The horizontal axis represents the jet selection requirements ($\geq 2$ jets and $m_{jj} \geq 120\ GeV$) defining the VBF-enriched signal regions (SR), while the vertical axis depicts the separation of the $m_{4\ell}$ range into resonant and non-resonant regions. The 'inclusive SR' comprizes events populating either the 'VBF-depleted region' or any of the VBF signal regions. The side-band control region (CR), dominated by non-resonant $ZZ^*$ decays, is denoted by ‘$ZZ^*$ CR’.

Three different types of fits are performed: decay-only, production-only, and combined. In each case, events are categorized to maximize analysis sensitivity, and all categories are fitted simultaneously. These categories are described in the following and illustrated in figure 1.

$ttH$, $tH$ and $bbH$ production modes are taken as background processes in the production-level optimal-observable measurement, the corresponding shape predictions are taken from the SM Higgs bosons samples described in section 4, rather than from the BSM Higgs boson samples, to benefit from the higher theoretical precision of the prediction.

A decay-only fit exclusively targets CP-violating effects in the Higgs boson decay. Two event categories are used. The signal region, also referred to as ‘inclusive SR’ in the following, comprises all events with $115\ GeV < m_{4\ell} < 130\ GeV$. Events with invariant masses in the side-band of the resonance, $105\ GeV < m_{4\ell} < 115\ GeV$ or $130\ GeV < m_{4\ell} < 160\ GeV$, form the background-dominated control region. This side-band, dominated by non-resonant $ZZ^*$ decays, is denoted by ‘$ZZ^*$ CR’. The yield of the Higgs boson decay signal, independent of production mode, is parameterized with a normalization factor relative to the SM prediction. A second normalization factor scales the yield of the non-resonant $ZZ^*$ background relative...
to the SM prediction. In both cases, the relative distribution of the yield between the signal and control region is assumed to follow the SM prediction within uncertainties as described in section 7. Both normalization factors are free parameters in the fit. In this way, the background rate in the signal region is determined by the control region data yield. Decay-level optimal observables are considered in the signal region to test for signs of CP violation in the Higgs boson decay and to measure the BSM couplings under consideration.

A production-only fit searches for signs of CP-violation at the VBF production vertex. This fit uses events in the resonant $m_{4\ell}$ region ($115 \text{ GeV} < m_{4\ell} < 130 \text{ GeV}$) with at least two jets and $m_{jj} > 120 \text{ GeV}$ for the signal extraction. To further enhance the VBF signal over other Higgs boson production modes, four VBF signal regions are defined as ascending intervals of the VBF score of a three-output neural network discriminant [27] trained to distinguish between VBF, $VH$ and ggF events. The discriminant is trained on two-jet events using the di-jet mass, $m_{jj}$, the transverse momentum of the full system, $p_{T}^{4\ell jj}$, and the transverse momentum and $\eta$ position of the individual leptons and jets, $p_{T}^{\ell}$, $\eta_{\ell}$, $p_{T}^{j}$ and $\eta_{j}$. The discriminant interval boundaries are chosen to yield two regions with a large ggF admixture and two regions with a high VBF purity, while maintaining a steady variation in the event yield across categories. These are denoted by ‘VBF SR1’ through ‘VBF SR4’. The effect of $VH$ production on the production-only fit is small — after the $m_{jj} \geq 120 \text{ GeV}$ requirement it contributes less than 10% of the events in the background-dominated VBF SR1 bin. Although both VBF and VH production are affected by a non-zero $HVV$ CP-odd coupling, the VBF optimal observable exhibits little asymmetry for VH production.

In addition to the four signal regions, two control regions are used. The first is the same ZZ∗ CR as used in the decay-only fit, which allows the non-resonant background to be constrained. Events within the resonant $m_{4\ell}$ region that do not enter the VBF SR regions form a second control region, denoted by the ‘VBF-depleted region’. This is enriched in ggF events that represent the largest source of resonant background for this measurement. Three separate normalization factors relative to the SM prediction are assigned to the VBF/$VH$ signal process, the ggF/ttH/tH/bbH resonant background and the non-resonant ZZ∗ background. The factors are common across all categories, and the fraction of the total yield entering each of the analysis categories is taken from the SM prediction. All three factors are free in the fit. In addition, for the VBF/$VH$ signal process, the distribution of events among the four signal regions is allowed to vary in the fit, as BSM effects are expected to modify it. The fraction of VBF/$VH$ events in the first two VBF regions is allowed to float in the fit while the last two regions are scaled accordingly to conserve the total yield across the four regions. The floating fraction is forced to be positive to ensure numerical stability of the fit. Production-level optimal-observable distributions are used in the signal regions (VBF SR 1–4).

Finally, a combined fit closely follows the production-only strategy. The VBF-depleted region takes the role of an additional signal region, in which decay-level optimal-observable distributions are fitted. Production-level observable distributions are fitted to events populating the four VBF signal regions. The same normalization strategy as for the production-only fit is used. This fit targets BSM signatures that have sensitivity in both the production and decay vertices.

In all fits, the reducible background is obtained directly from collision data and its normalization constrained to the measured value within its uncertainty.
Figure 2. The composition of the predicted event yield in the event categories used for the direct EFT coupling measurements. The contribution from $bbH$ is negligible and not visible in the plot. The MC statistical uncertainty in the fraction of each component is not shown but is below the 1% level.

Figure 2 shows the composition of the predicted SM yield in each of the analysis categories. The $ZZ^*$ control region is highly pure in the non-resonant background. The VBF-depleted region and inclusive signal region are both dominated by the resonant signal, with a non-resonant admixture of the order of 30%. The VBF signal regions are increasingly pure in the resonant process, with a 30%-level non-resonant admixture in the first region. The purity of the VBF process relative to the ggF process increases across the four regions, up to a value of 90% in the final VBF SR 4 category.

In the signal regions of all three fits, the optimal-observable distributions are binned in 48 bins for the decay-level observables and in 12 bins for the production-level ones. The binning is optimized for each coupling assumption in the observable definition. The binning is constructed to yield an approximately flat distribution of expected events across the bins for a sample composed of 50% SM events and 25% events each simulated with a positive and a negative BSM coupling value close to the expected 68% C.L. limit.

To measure a given BSM coupling, the optimal observable evaluated with a BSM matrix element for the same coupling is used, separately for production ($jj$) and decay ($4\ell$). This provides optimal sensitivity, as discussed in section 2.2. When simultaneously measuring pairs of BSM couplings using decay-level optimal observables, a two-dimensional binning of the observables targeting the $c_{H\tilde{W}}$ and $c_{H\tilde{B}}$ couplings yields the largest sensitivity. In this case, six times six bins are used, optimized in the same way as for the one-dimensional binnings. Finally, when simultaneously measuring the $\tilde{c}_{zz}$ and $\tilde{c}_{\gamma\gamma}$ couplings using the combined fit set-up, production-level observables targeting the $\tilde{c}_{zz}$ coupling in the VBF signal regions are combined with decay-level observables targeting the $\tilde{c}_{\gamma\gamma}$ coupling in the VBF-depleted region. All control regions are treated as single-bin counting experiments.
Figure 3. Expected distributions of (a) the $OO_{jz}^{zz}$ observable for VBF-produced Higgs boson candidates combining VBF SR1 through SR4 for the SM and for BSM coupling parameter values of $\tilde{c}_{zz} = \pm 5$, and (b) the $OO_{4\ell, j}^{z_B}$ observable for the decay of ggF produced Higgs boson candidates in the inclusive SR for the SM and for BSM coupling parameter values of $c_{H\tilde{B}} = \pm 1.5$. (a) has 12 equal-size bins, and (b) has 48 equal population bins. In (b) the first and last bins extend up to ±40, but the bin range is truncated to ±4 in the plot for clarity. The lower panels show the ratio of the BSM to the SM optimal-observable distributions.

Figure 3 shows expected optimal-observable distributions for production-level $OO_{jz}^{zz}$ and decay-level $OO_{4\ell, j}^{z_B}$ for the SM and two BSM samples. The optimal-observable distributions are symmetric in the SM case and asymmetric for CP-odd couplings. The two distributions have different binning: 3(a) has equal size binning, and 3(b) has an equally populated one, for a distribution composed of 50% SM and 25% for both $c_{H\tilde{B}} = \pm 0.75$. Equally populated binning is used in the present analysis. The distributions of both plots, and the ratios of BSM to SM, clearly demonstrate the importance of the tails for a CP-asymmetry measurement.

6.2 Differential cross-section measurement

The main motivation for performing differential cross-section measurements is to have a model-independent result sensitive to possible deviations from the SM. The differential cross-section measurement of the optimal observables allows any CP-odd effects affecting the Higgs boson coupling to be probed. Unlike the direct coupling measurement, a differential cross-section measurement is sensitive to possible BSM effects on both the yields and the shape of the observable. The measurement is performed by unfolding the corresponding observable distribution within a fiducial phase space.

The fiducial phase space is defined using simulation at particle level and applying selection requirements to minimize model-dependent acceptance extrapolations. These are chosen to closely match the selection requirements of the detector-level analysis after the event
Leptons and jets

| Leptons | $p_T > 5\text{ GeV}, |\eta| < 2.7$ |
|---------|-----------------|
| Jets    | $p_T > 30\text{ GeV}, |y| < 4.4$ |

Lepton selection and pairing

<table>
<thead>
<tr>
<th>Lepton kinematics</th>
<th>$p_T &gt; 20,15,10\text{ GeV}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Leading pair ($m_{12}$)</td>
<td>SFOC lepton pair with smallest $</td>
</tr>
<tr>
<td>Subleading pair ($m_{34}$)</td>
<td>Remaining SFOC lepton pair with smallest $</td>
</tr>
</tbody>
</table>

Event selection (at most one quadruplet per event)

<table>
<thead>
<tr>
<th>Mass requirements</th>
<th>$50\text{ GeV} &lt; m_{12} &lt; 106\text{ GeV}$ and $m_{\text{threshold}} &lt; m_{34} &lt; 115\text{ GeV}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lepton separation</td>
<td>$\Delta R(\ell_i, \ell_j) &gt; 0.1$</td>
</tr>
<tr>
<td>Lepton/Jet separation</td>
<td>$\Delta R(\ell_i, \text{jet}) &gt; 0.1$</td>
</tr>
<tr>
<td>$J/\psi$ veto</td>
<td>$m(\ell_i, \ell_j) &gt; 5\text{ GeV}$ for all SFOC lepton pairs</td>
</tr>
<tr>
<td>Mass window</td>
<td>$105\text{ GeV} &lt; m_{\ell\ell} &lt; 160\text{ GeV}$</td>
</tr>
</tbody>
</table>

If an extra lepton with $p_T > 12\text{ GeV}$ is found, the quadruplet with the largest squared matrix element value is kept.

Table 2. List of event selection requirements that define the fiducial phase space for the cross-section measurement. SFOC lepton pairs are same-flavour opposite-charge lepton pairs. For the mass requirement of the subleading lepton pair, $m_{\text{threshold}}$ is $12\text{ GeV}$ for $m_{4\ell} < 140\text{ GeV}$ and rises linearly until reaching $50\text{ GeV}$ for $m_{4\ell} = 190\text{ GeV}$.

reconstruction. The fiducial phase space definition is the same as described in ref. [27] and summarized in table 2.

Furthermore, as mentioned in section 6.1, it is also interesting to investigate CP-odd effects using the VBF Higgs boson production vertex. For this reason, a fiducial cross-section is measured in a VBF-enriched phase space. In addition to the selections in table 2, the VBF-enriched fiducial region requires the presence of at least two jets with an invariant mass $m_{jj} \geq 400\text{ GeV}$, and a difference between the $\eta$ of the leading and of the subleading jet of $|\Delta \eta_{jj}| \geq 3.0$. These selections replace the neural network used to define the VBF SR regions of the direct coupling measurement. Two separate fiducial cross-sections are extracted from the VBF-enriched fiducial region, resulting in different levels of VBF purity. For the first, a ‘combined production mode’ Higgs boson signal is extracted with ggF, VBF, VH and $ttH$ considered as signal. For the second the Higgs boson signal is extracted while additionally removing the ggF production mode signal by treating it as background using the detector-level MC expectation. This VBF-enriched fiducial region has a signal composition of 59.3% VBF, 37.5% ggF, 1.7% VH and 1.5% $ttH$. The VBF purity increases to 95% if the ggF is removed as a background. Although the first fiducial cross-section is less pure in VBF signal, it is less model dependent because it has no assumption on the signal composition. The second fiducial cross-section relies on the assumption of SM ggF production.

To extract the number of signal events in each bin of a differential distribution, invariant mass templates for the Higgs boson signal and the background processes are fitted to the $m_{4\ell}$ distribution in data, following the same strategy as used in ref. [27]. The non-resonant $ZZ^*$ background is fitted simultaneously with the signal and constrained by extending the $m_{4\ell}$ fit range from 115–130 GeV to 105–160 GeV, similar to the control region used in the direct coupling measurement. Furthermore, the SM $ZZ^* \rightarrow 4\ell$ decay fractions are assumed. To reduce the effects of bin-to-bin statistical fluctuations of the non-resonant $ZZ^*$ background,
neighbouring bins are combined for this background estimate. The overall normalization and shape of the reducible background from a data-driven evaluation (section 5.3) are allowed to vary within their associated systematic uncertainties (section 7).

The expected number of events $N_i$ in each detector-level observable bin $i$, expressed as a function of $m_{4\ell}$, is given by

$$N_i(m_{4\ell}) = \sum_j r_{ij} \cdot (1 + f_{\text{nonfid}}^i) \cdot \sigma_{j}^{\text{fid}} \cdot \mathcal{P}_i(m_{4\ell}) \cdot L + N_{i\text{bkg}}(m_{4\ell})$$

(6.1)

with the fiducial cross-section in each fiducial bin $j$ given by

$$\sigma_{j}^{\text{fid}} = \sigma_j \cdot A_j \cdot B$$

where $A_j$ is the acceptance in the fiducial phase space for a total cross-section $\sigma_j$ in fiducial bin $j$, $L$ is the integrated luminosity, $B$ is the decay branching ratio and $N_{i\text{bkg}}(m_{4\ell})$ is the background contribution. The index $j$ runs over all observable bins in the fiducial phase space. The term $\mathcal{P}_i(m_{4\ell})$ is the $m_{4\ell}$ signal shape containing the fraction of events as a function of $m_{4\ell}$ expected in each reconstruction bin, taken from SM MC simulation. The term $r_{ij}$ represents the detector response matrix, created with SM simulated signal samples and averaged across the different production modes using the expected SM cross-sections [43]. These factors correspond to the probability that an event generated within the fiducial volume in the observable bin $j$ is reconstructed in bin $i$. The normalization, $f_{\text{nonfid}}^i$, represents the fraction of events that are outside of the fiducial region but are reconstructed within the SR. This ranges from 1.1% to 1.7% depending on the bin of the unfolded observable or the final state. The detector response matrix accounts for bin-to-bin migrations in the unfolding of the signal. The binning choice made for all observables ensures a statistical significance of more than two standard deviations for the SM signal process. The binning is also chosen to minimize migrations between bins. In most cases, the bin width is more than twice the experimental resolution.

For the VBF-enriched fiducial cross-section measurements, the signal is extracted by unfolding the two-dimensional distribution $m_{jj}$ versus $|\Delta\eta_{jj}|$ that is divided into three bins (see figure 14), following the strategies explained previously. The difference for the second measurement is that the ggF is considered to be a background and the expected ggF signal is moved from $\mathcal{P}_i(m_{4\ell})$ to $N_{i\text{bkg}}(m_{4\ell})$ of eq. (6.1).

7 Systematic uncertainties

The statistical uncertainty in the data is generally dominant in all aspects of the analysis, and systematic uncertainties play a minor role. Systematic uncertainties arise from experimental sources, such as lepton and jet momentum scales, resolutions and reconstruction efficiencies, and theoretical uncertainties related to the modelling of the signal and background processes. In addition, a set of uncertainties specific to the cross-section extraction method affect the differential cross-section measurement.

As the rates of all key contributing processes are determined using the collision data, normalization uncertainties affecting their total calculated cross-sections have no impact.
Uncertainties in the determination of the kinematic observables characterising the final state, in particular jet and lepton momentum scale and resolutions, affect the analysis in the most direct way through the reconstructed value of the optimal observables. Uncertainties in the relative rates between the various categories, arising for example from theoretical sources, affect the results indirectly via changes in the process composition in the signal regions and migration effects in the cross-section measurement. While still small compared to statistical uncertainties, these composition uncertainties are the leading source of systematic uncertainty in the direct coupling measurement. The measured differential cross-sections are also sensitive to luminosity and lepton reconstruction and isolation efficiency uncertainties, which play a negligible role for the direct coupling measurement.

When predicting BSM effects in the direct coupling measurement, theoretical uncertainties due to the PDF, parton shower, and QCD scale variations are assigned to the signal predictions based on SM signal samples, which are simulated with higher-order precision. The same uncertainties are assigned to all corresponding BSM signal predictions, since it is observed using the MC signal samples simulated at leading-order accuracy that the uncertainties change negligibly as a function of the Wilson coefficients.

An overview of the main sources and their impact on the analysis is provided below. When quantifying the impact of uncertainties on the direct coupling measurement, where no evidence for a non-zero coupling value is obtained in the fit to collision data, the impacts on a hypothetical BSM signal obtained using simulation are provided instead.

### 7.1 Experimental uncertainties

The uncertainty in the measured differential cross-sections due to pile-up modelling is of the order of 1%. The uncertainty in the combined 2015–2018 integrated luminosity is 1.7% [94], obtained using the LUCID-2 detector [95] for the primary luminosity measurements. The luminosity uncertainty directly propagates to the measured cross-sections. Neither source affects the direct coupling measurement.

The electron (muon) reconstruction and identification efficiency uncertainties in the extracted cross-sections are of the order of 1–2% (≤1%). Isolation efficiency uncertainties affect the results at a similar magnitude. Lepton efficiencies have a negligible impact on the direct coupling measurement since they do not induce asymmetries in the CP-sensitive observables.

Lepton energy, momentum scale and resolution uncertainties affect both the direct coupling measurement and the extracted cross-sections at the order of 1–2% level due to their relation to the reconstructed rest-frame kinematics determining the optimal observables.

The impact of uncertainties in the jet energy scale and resolution is only relevant for production-level optimal observables. There, they affect the differential cross-sections at the 1–5% level and the directly extracted coupling values at the 1–3% level.

The impact of the precision of the Higgs boson mass measurement [96] on the signal acceptance due to the signal region mass-window requirement is considered for the cross-section extraction, but found to have a negligible impact (<1%).

For the data-driven measurement of the reducible background, three sources of uncertainty are considered: statistical uncertainty, overall systematic uncertainty for muon and electron...
background fake estimates [27], and a shape systematic uncertainty that varies with the
differential variable [36]. All of these have a negligible impact on the analysis.

7.2 Theoretical uncertainties

The theoretical modelling of the signal and background processes is affected by uncertainties
due to missing higher-order corrections, modelling of parton showers and the underlying
event, and PDF plus $\alpha_s$ uncertainties.

One of the dominant sources of theoretical uncertainty is the prediction of the ggF process,
in particular its contribution to the dijet signal regions targeting production observables.
To estimate the variations due to the impact of higher-order contributions not included
in the calculations, the approach described in refs. [43, 97] is used, which exploits the
latest predictions for the inclusive jet cross-sections. In particular, the uncertainty from
the choice of factorization and renormalization scales, the choice of resummation scales,
and the migrations between the 0-jet and 1-jet phase space bins or between the 1-jet and
$\geq$ 2-jet bins are considered. The detailed procedure is described in ref. [27]. The impact
of these uncertainties can reach 5% of the directly measured coupling value and 1–2% of
the measured differential cross-sections.

The uncertainties in the acceptance and distribution of yields among the analysis regions
due to the modelling of parton showers and the underlying event are estimated with AZNLO
tune [98] eigenvector variations and by comparing the results using the parton showering
algorithm from PYTHIA8 with that from HERWIG 7 [99] for all signal processes. The eigenvector
variations are correlated between the Higgs boson production modes, while the algorithm
uncertainty is treated as uncorrelated. This is the largest individual systematic uncertainty
source when considering production-level optimal observables, with a magnitude in the range
of 2–10% of the measured cross-sections in the differential measurement and 1–5% of the
directly measured BSM coupling values.

For the VBF, VH and ttH production modes, the uncertainty due to missing higher
orders in QCD is parameterized using the scheme outlined in ref. [100]. Compared to the
uncertainties in the ggF contribution, both the scale and the shower uncertainties in these
predictions are negligible.

The impact of the PDF uncertainty is estimated with the 30 eigenvector variations of
the PDF4LHCnlo30 Hessian PDF set following the PDF4LHC recommendations [61]. The
modification of the predictions originating from each eigenvector variation is added as a
separate source of uncertainty in the model. The same procedure is applied for the ggF,
VBF, VH and ttH processes. PDF uncertainties have a negligible impact.

Beside the resonant process, uncertainties in the prediction of the main non-resonant
$q\bar{q} \rightarrow ZZ^*$ background process affect the analysis. As the normalization of this background
is obtained from collision data, the main impact is from migration effects between various
regions. The uncertainties due to missing higher-order effects in QCD are estimated by
varying the factorization and renormalization QCD scales by a factor of two; the impact of
the PDF uncertainty is estimated by using the MC replicas of the NNPDF3.0 PDF set.
Uncertainties due to parton shower modelling for the ZZ* process are considered as well.
For the differential cross-section measurement, a comparison of the ZZ* predictions of the
The $m_{4\ell}$ spectrum used to normalize this background to the ones obtained using the alternative generators described in section 4 is used to define an additional systematic uncertainty. The impact of these uncertainties is very small, less than 2% on the directly measured couplings and negligible for the differential cross-sections.

7.3 Uncertainties specific to the differential cross-section extraction

Unfolding-related uncertainties arise from the production mode composition that determines the average response matrices, and from residual biases introduced by the unfolding method [36]. For the former, an uncertainty is assessed by varying the production cross-sections within their measured uncertainties taken from ref. [101], with an impact of less than 1%. The uncertainty arising from unfolding biases is obtained independently for each bin by comparing the unfolded cross-section from simulation with that expected when varying the underlying particle-level cross-sections of the simulated data sample within the expected statistical error. In the same way, the uncertainty is extended to also account for differences that arise from using an SM response matrix to measure observable distributions possibly affected by BSM behaviour by means of signal injection (up to 95% C.L. of a possible CP-odd coupling). The impact of this uncertainty is typically around 1–2% in the decay optimal observable, where the response matrix is largely diagonal, and increases up to 7% in the production optimal-observable distributions, which have larger bin migrations.

7.4 Monte Carlo statistics

The effect of MC statistical uncertainties is included in the statistical model used for the measurement, as the direct coupling measurement relies on precise shape predictions for the optimal observables and other systematic uncertainties are very small. The signal modelling technique results in a negligible impact of statistical uncertainties on the prediction of BSM effects. The largest contribution to the MC statistical uncertainty is linked to the non-resonant $q\bar{q} \rightarrow ZZ^*$ background prediction, affecting the measured coupling values at the level of few percent. This is negligible compared to statistical uncertainties in the data, but comparable (1–2% impact) to the leading systematic uncertainty sources for coupling measurements using decay-level observables, due to the small size of the systematic uncertainties in these measurements.

8 Results

8.1 Direct coupling measurement results

The number of events observed and the expected (pre-fit) contributions in each of the categories used in the coupling measurements, described in section 6.1 and figure 1, are shown in figure 4 and table 3. Combined statistical and systematic uncertainties are included for the predictions (see section 7). As discussed in section 6.1, the $ZZ^*$ CR and Inclusive SR contribute to the decay observable fits, and the rest contribute to the production-only and combined observable fits. In all categories, the number of events observed and the expectation agree within one to two standard deviations. The largest difference occurs in
Table 3. The numbers of expected and observed events in the event categories for the direct CP measurement, within the mass range 115 GeV < $m_{4\ell}$ < 130 GeV. The sum of the number of expected SM Higgs boson events and the estimated background yields is compared with the data. Combined statistical and systematic uncertainties are included for the predictions. The Inclusive SR, used in the decay-only fit, is composed of the VBF-depleted Region and VBF SR1 to SR4.

<table>
<thead>
<tr>
<th></th>
<th>ZZ* CR</th>
<th>Inclusive SR</th>
<th>VBF-depleted Region</th>
<th>VBF SR1</th>
<th>VBF SR2</th>
<th>VBF SR3</th>
<th>VBF SR4</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ggF$</td>
<td>8.2 ± 1.3</td>
<td>181 ± 12</td>
<td>165 ± 12</td>
<td>7.5^{+3.0}_{-2.4}</td>
<td>5.6^{+1.8}_{-1.5}</td>
<td>2.2 ± 0.6</td>
<td>0.49 ± 0.17</td>
</tr>
<tr>
<td>$bbH$</td>
<td>0.087^{+0.065}_{-0.015}</td>
<td>1.85 ± 0.05</td>
<td>1.65 ± 0.05</td>
<td>0.11 ± 0.01</td>
<td>0.072^{+0.010}_{-0.009}</td>
<td>0.020 ± 0.003</td>
<td>&lt; 0.01</td>
</tr>
<tr>
<td>VBF/VH</td>
<td>1.39 ± 0.16</td>
<td>23.8 ± 0.7</td>
<td>13.8 ± 0.6</td>
<td>1.60^{+0.09}_{-0.08}</td>
<td>1.89 ± 0.11</td>
<td>3.01 ± 0.18</td>
<td>3.5 ± 0.4</td>
</tr>
<tr>
<td>$ttH,tH$</td>
<td>0.22^{+0.03}_{-0.04}</td>
<td>1.89^{+0.21}_{-0.22}</td>
<td>0.44 ± 0.05</td>
<td>1.22 ± 0.14</td>
<td>0.179 ± 0.023</td>
<td>0.046^{+0.009}_{-0.010}</td>
<td>&lt; 0.01</td>
</tr>
<tr>
<td>$VVV$</td>
<td>6.79 ± 0.13</td>
<td>1.31 ± 0.06</td>
<td>0.62 ± 0.04</td>
<td>0.53 ± 0.04</td>
<td>0.150 ± 0.020</td>
<td>&lt; 0.01</td>
<td>&lt; 0.01</td>
</tr>
<tr>
<td>$ZZ^*$</td>
<td>229^{+20}_{-25}</td>
<td>98^{+6}_{-9}</td>
<td>92^{+6}_{-8}</td>
<td>3.5^{+1.3}_{-1.7}</td>
<td>1.7 ± 0.6</td>
<td>0.48^{+0.16}_{-0.15}</td>
<td>0.086^{+0.025}_{-0.026}</td>
</tr>
<tr>
<td>$Z_{jet},t\bar{t},WZ$</td>
<td>21 ± 5</td>
<td>13 ± 4</td>
<td>12 ± 3</td>
<td>0.8 ± 0.9</td>
<td>0.3 ± 0.6</td>
<td>0.07 ± 0.26</td>
<td>0.01 ± 0.09</td>
</tr>
<tr>
<td>Total SM</td>
<td>267^{+21}_{-26}</td>
<td>321^{+14}_{-15}</td>
<td>286^{+14}_{-15}</td>
<td>15 ± 3</td>
<td>9.9^{+2.0}_{-1.7}</td>
<td>5.9 ± 0.7</td>
<td>4.1 ± 0.5</td>
</tr>
<tr>
<td>Data</td>
<td>294</td>
<td>311</td>
<td>276</td>
<td>14</td>
<td>9</td>
<td>4</td>
<td>8</td>
</tr>
</tbody>
</table>

Figure 4. The number of observed events and the expected contributions in each of the categories used in the decay-only, production-only, and combined observable fits for the coupling measurements. The contribution from $bbH$ is negligible and not visible in the plot. The lower panel shows the ratio of data to expectation. The shaded bands in both the upper and lower panels correspond to the combined statistical and systematic uncertainties in the predictions.
the most sensitive VBF category, VBF SR4, where the small number of observed events exceeds the expectation by about a factor of two.

The observed and expected distributions for the production-level observable $OO\tilde{c}_{zz}$ in each of the four VBF signal regions are shown in figure 5. The corresponding observed and expected distributions for the decay level observables $OO\tilde{c}_{d}^{\ell}$, $OO\tilde{c}_{u}^{\ell}$, $OO\tilde{c}_{W}^{\ell}$, and $OO_{\tilde{c}}^{\ell}$ are shown in figure 6. The expected distributions for the SM are shown as stacked histograms, and the two lines show the expectation for an additional positive or negative CP-odd BSM coupling that has a clear excess in the tail. The combined statistical and systematic uncertainties are shown in the ratio plot below each distribution. Overall there is good agreement between data and the SM expectation. The mean value for the data is given for each distribution, calculated from the observable value for each event. All mean values are compatible with zero, indicating that the data exhibit no measurable asymmetry.

In absence of positive evidence for BSM physics, 68% and 95% confidence intervals on the CP-odd couplings ($c_{BSM}$) are extracted with the profile likelihood ratio [102] statistical test, using the negative-log likelihood (NLL) test statistic:

$$-2 \ln \lambda(x|c_{BSM}) = -2 \ln \frac{L(x|\hat{c}_{BSM}, \hat{\theta})}{L(x|\hat{c}_{BSM}, \hat{\theta})}$$

where $\theta$ corresponds to the set of systematic uncertainties, or nuisance parameters. The numerator denotes the conditional likelihood estimator of $\theta$, (i.e., $\hat{\theta}$ is the value of $\theta$ that maximizes the likelihood function for a given $c_{BSM}$), and the denominator denotes the maximized likelihood estimator (i.e., $\hat{c}_{BSM}$ and $\hat{\theta}$ are the values of $c_{BSM}$ and $\theta$ that maximize the unconditional likelihood function). The effect of the nuisance parameters is to broaden the profile likelihood ratio reflecting the loss of information originating from the inclusion of systematic uncertainties. For each BSM coupling, a scan across the values of $c_{BSM}$ of the NLL is performed by fitting all other parameters (normalization parameters, other BSM couplings, and nuisance parameters) to obtain the values that minimize the NLL for the current value of the coupling being scanned, or couplings for two-dimensional scans. This result relies on the assumption that for any value of the coupling being scanned, the NLL behaves as a $\chi^2$ distribution with one degree of freedom (asymptotic approximation [103]). Based on this, the confidence intervals are constructed from the scan parameter values for which the NLL crosses the 68% and 95% quantile locations of a $\chi^2$ distribution with one degree of freedom. The validity of the asymptotic approximation for this measurement was confirmed by sampling the distribution of the test statistic observed on toy datasets obtained by random sampling from the predicted likelihood model.

The expected sensitivity of the seven couplings explored in this analysis (section 2.3) are given in table 4. The expected 95% confidence intervals estimated separately for either VBF production or Higgs boson to four-lepton decay and as well for their combination are shown for each coupling. There are about ten VBF events expected in the signal region and over 200 expected Higgs boson decays from all production modes in the inclusive signal region, giving a significant statistical advantage to the decay observable fits. For the Higgs basis that has couplings in the mass Lagrangian, production is predominantly sensitive to the $\tilde{c}_{zz}$ coupling with a limited sensitivity to $\tilde{c}_{z\gamma}$, and decay is sensitive to both $\tilde{c}_{z\gamma}$ and $\tilde{c}_{\gamma\gamma}$. This can
Figure 5. The observed and expected distributions for the production-level observable $OO^c_{\tilde{c}}$ in each of the four VBF signal regions: (a) SR1, (b) SR2, (c) SR3, and (d) SR4. The expected distribution for the VBF signal and the backgrounds from ggF, ZZ*, and reducible backgrounds are shown as a stacked histogram. Also shown are the expected distributions in presence of CP-odd contributions for $\tilde{c}_z = \pm 2.0$, assuming the VBF/VH event rate remains that of the SM. The bin size is variable, optimized for an approximately flat distribution for the SM combined with a positive and negative BSM scenario. All events have optimal observable values within the limits of the plots. The mean value of the optimal observable across the data events is given with its standard deviation. The lower panels show the ratio of data to expectation and the shaded band corresponds to the combined statistical and systematic uncertainties in the predictions.
Figure 6. The observed and expected distributions for the decay level observables: (a) $OO_{4b}^{cB}$, (b) $OO_{4b}^{cWB}$, (c) $OO_{4b}^{cW}$ and (d) $OO_{4b}^{d}$. The expected distribution for the ggF and VBF signals and the backgrounds from $ZZ^*$ and reducible backgrounds are shown as a stacked histogram. Also shown are the expected distributions in presence of CP-odd contributions for (a) $c_{HB} = \pm 1.5$, (b) $c_{WB} = \pm 1.25$, (c) $c_{WW} = \pm 1.5$ and (d) $d = \pm 1.25$, assuming the signal event rate remains that of the SM. The bin size is variable, optimized for an approximately flat distribution for the SM combined with a positive and negative BSM scenario. There are no observed events that fall outside the optimal-observable distribution range, with rate expectations below 0.1%. The mean value of the optimal observable across the data events is given with its standard deviation. The lower panels show the ratio of data to expectation and the shaded band corresponds to the combined statistical and systematic uncertainties in the predictions.
Table 4. The expected 95% confidence intervals of production-only, decay-only and combined production and decay likelihood scans for the CP-odd Wilson coefficients in the Warsaw and Higgs bases for an integrated luminosity of 139 fb\(^{-1}\) at \(\sqrt{s} = 13\) TeV. Only one Wilson coefficient is fitted at a time while all others are set to zero. Limits denoted by ‘\(\sim\)’ indicate no sensitivity or no observable gain for the combined fits. All couplings scale as \(1/\Lambda^2\) with the assumed value of \(\Lambda = 1\) TeV.

<table>
<thead>
<tr>
<th>EFT coupling</th>
<th>Expected 95% C.L.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>production-only</td>
</tr>
<tr>
<td>(c_{H\tilde{B}})</td>
<td>—</td>
</tr>
<tr>
<td>(c_{H\tilde{W}B})</td>
<td>—</td>
</tr>
<tr>
<td>(c_{H\tilde{W}})</td>
<td>±4.8</td>
</tr>
<tr>
<td>(\tilde{d})</td>
<td>±0.63</td>
</tr>
<tr>
<td>(\tilde{c}_{zz})</td>
<td>±2.4</td>
</tr>
<tr>
<td>(\tilde{c}_{z\gamma})</td>
<td>±6.6</td>
</tr>
<tr>
<td>(\tilde{c}_{\gamma\gamma})</td>
<td>—</td>
</tr>
</tbody>
</table>

be understood from the fact that the VBF production includes also W-boson diagrams and occurs at larger energy scales compared to the decay vertex, which happens at the scale of the Higgs mass and exclusively via neutral gauge bosons, enhancing the role of virtual photon diagrams. For the Warsaw basis that has couplings in the interaction Lagrangian before SU(2) symmetry breaking, the physical interpretation is less intuitive, as all operators mix the effects of \(Z^{(*)}\) and \(\gamma^*\) propagators on both legs of the HVV vertex. \(c_{H\tilde{W}}\) has sensitivity to both production and decay with the latter having improved sensitivity due to the larger number of events, \(c_{H\tilde{B}}\) and \(c_{H\tilde{W}B}\) are both only sensitive to the decay. Finally \(\tilde{d}\), which is proportional to \(c_{H\tilde{B}}\) with the constraints \(c_{H\tilde{B}} = c_{H\tilde{W}}\) and \(c_{H\tilde{W}B} = 0\), is mostly sensitive to the decay. The combined observable fits use the VBF SR1 to VBF SR4 for the production observable and the VBF-depleted signal region for the decay observable. This reduces by about 10% the number of events entering the decay observable fit, i.e., those in VBF SR1 to VBF SR4, and can lead to a degraded sensitivity of the combined fit compared to the decay fit in the inclusive signal region. This is the case for \(\tilde{c}_{z\gamma}\) and \(\tilde{d}\), since their production sensitivity is poor. Whereas for \(c_{H\tilde{W}}\), which has a more balanced sensitivity for production and decay, the combination limits improve over either production or decay only.

The expected and observed distributions for the \(\tilde{c}_{zz}\) coupling NLL production scans are shown in figure 7(a). The observed central value for \(\tilde{c}_{zz}\) at 0.78 and the non-parabolic shape of the NLL is due to the small excess of VBF candidates at positive \(\tilde{c}_{zz}\) in SR1 (figure 5(a)). The effect of systematic uncertainties, primarily jet-related, is about 15% for the expected 95% C.L. In the observed NLL scan, a local enhancement of the impact of systematic uncertainties for small absolute values of the BSM coupling is driven by the ggF parton-shower uncertainty, which primarily affects the migration of ggF events between the control region and the VBF-enriched signal regions, as discussed in section 7.2. For small couplings, where the VBF optimal-observable distribution is like the SM, this uncertainty allows the fit model to adapt to the observed local downward fluctuation in the central bins.
of the VBF SR1, leading to a comparably large impact of this uncertainty. In figure 7(b), the observed NLL distributions are shown for $c_{\widetilde{H}W}$ for production, decay and their combination, as well as the expected distribution for the combination. The observed central value at 1.5 of the production-only $c_{\widetilde{H}W}$ scan arises from the same excess of VBF candidates as for $\tilde{c}_{zz}$. Combining with the decay-only scan (central value about 0.1), reduces the combined central value to 0.6. There is a small effect of systematic uncertainties on the production-only limits, with a local increase of their impact around zero originating from the same effect described above for the $\tilde{c}_{zz}$ coupling. The $c_{\widetilde{H}W}$ decay-only scan has a better statistical precision than the production-only scan and relies only on the well-measured lepton kinematics, so the effect of systematic uncertainties is negligible.

The observed and expected NLL observable scans for the decay level couplings for the Warsaw basis $c_{H\tilde{B}}$, $c_{\widetilde{H}W}\tilde{B}$, $c_{\widetilde{H}W}$ and $\tilde{d}$ are shown in figure 8, and for the Higgs basis $\tilde{c}_{\gamma\gamma}$ and $\tilde{c}_{\gamma\gamma}$ are shown in figure 9. Similarly to the combined scan of $c_{\widetilde{H}W}$ in figure 7(b), the decay-only optimal-observable fits have a negligible contribution from systematic uncertainties. Due to the small upward fluctuation of the data in the first and last observable bins in figure 6 the observed NLL scans for $OO_{\tilde{H}W}\tilde{B}$, $OO_{\widetilde{H}W}\widetilde{B}$ and $OO_{\tilde{d}}$ are less constraining than expected. The small upward fluctuation around zero for $OO_{\widetilde{H}W}\tilde{d}$ leads to tighter limits than expected. In the Higgs basis, the observed decay-only scans for $OO_{\tilde{d}\gamma}$ and $OO_{\tilde{d}\gamma}$ are also less constrained.

The observed and expected 68% and 95% C.L. two-dimensional contours for all three pairings of the Warsaw-basis couplings, $c_{H\tilde{B}}$, $c_{\widetilde{H}W}\tilde{B}$ and $c_{\widetilde{H}W}$, are shown in figures 10(a)–10(c).
Figure 8. The NLL observable scans for the Warsaw-basis couplings for decay-only fits: (a) $c_{H B}$ $(O_{44}^{m n})$, (b) $c_{H W B}$ $(O_{44}^{m n} \tilde{w} B)$, (c) $c_{H W}$ $(O_{44}^{m n} \tilde{w})$, and (d) $\tilde{d}$ $(O_{04}^{0})$. The expected and observed distributions are shown with (long-dashed/solid lines) and without (dashed line) systematic uncertainties. The effect of systematics is small for decay-only fits, so that the two sets of lines largely overlap. The $p$-values for agreement with the SM are 0.86, 0.98, 0.90 and 0.86 for the $c_{H B}$, $c_{H W B}$, $c_{H W}$, and $\tilde{d}$ coupling NLL scans, respectively. All couplings scale as $1/\Lambda^2$ with the assumed value of $\Lambda = 1$ TeV.
The two-dimensional observable $OO_{\tilde{c}^{\gamma\gamma}}^\gamma \tilde{c}^{\gamma\gamma}$ vs. $OO_{\tilde{c}^{\gamma\gamma}}^\gamma \tilde{c}^{\gamma\gamma}$ is used for these decay-only contours. This observable pair is found empirically to have the best expected sensitivity compared with any of the individual observables or other observable pairings. The observed minima in figures 10(a)–10(c) all lie along the diagonals of the confidence interval ellipses, well within the 68% C.L. These diagonals are relatively flat in terms of the likelihood minima. Figure 10(d) shows the two-dimensional contours for scans along $\tilde{c}_{z\gamma}$ versus $\tilde{c}_{\gamma\gamma}$, where $\tilde{c}_{z\gamma}$ is sensitive only to the production and $\tilde{c}_{\gamma\gamma}$ is sensitive only to the decay. For $\tilde{c}_{z\gamma}$, the events in VBF SR1 to SR4 are used with the observable $OO_{\tilde{c}^{\gamma\gamma}}^{\gamma \gamma}$ in 12 bins, as shown in figure 7(a), and for $\tilde{c}_{\gamma\gamma}$ the events in the VBF-depleted region are used with $OO_{\tilde{c}^{\gamma\gamma}}^{\gamma \gamma}$ in 48 bins as shown in figure 9(b). As shown in eq. (2.1), all couplings of figures 7–10 scale as $1/\Lambda^2$ with the assumed value of $\Lambda = 1$ TeV.

Figure 11 and table 5 summarize the expected and observed confidence intervals at 68% and 95% C.L. for the CP-odd Wilson coefficients. The limits for the Higgs-basis Wilson coupling $\tilde{c}_{z\gamma}$ are from a production-only observable fit. Those for the coupling $c_{H\bar{W}}$ are from a combined-observable fit as this coupling has sensitivity in both production and decay. The rest of the couplings are from a decay-only observable fit, having little sensitivity to the VBF production, as previously shown in table 4.

The prediction of the optimal-observable distribution using the morphing method described in section 2.3 includes both a linear and quadratic dependence on the BSM matrix element (see eq. (2.2)). Only the linear term generates an asymmetry of the optimal-observable distribution, while the quadratic term leads to a symmetric shape modification. The normalization of the signal is left to float in the statistical model to allow a shape-only analysis,
Figure 10. The observed and expected 68% and 95% C.L. two-dimensional contours for all three pairings of the Warsaw-basis couplings: (a) $c_{H\tilde{W}B}$ versus $c_{H\tilde{B}}$, (b) $c_{H\tilde{W}}$ versus $c_{H\tilde{B}}$ and (c) $c_{H\tilde{W}}$ versus $c_{H\tilde{W}B}$. These use the two-dimensional observable $OO_{4\ell}$ versus $OO_{4\ell}^{\tilde{W}B}$. In (d), the two-dimensional contours for scans along $\tilde{c}_{\gamma\gamma}$, sensitive only to the decay, and $\tilde{c}_{zz}$, sensitive only to the production are shown, where the observable $OO_{4\ell}^{\tilde{c}_{\gamma\gamma}}$ is used for the decay and $OO_{4\ell}^{\tilde{c}_{zz}}$ for the production. All couplings scale as $1/\Lambda^2$ with the assumed value of $\Lambda = 1$ TeV.
Table 5. The expected and observed confidence intervals at 68% and 95% C.L. for the CP-odd Wilson coefficients for an integrated luminosity of 139 fb$^{-1}$ at $\sqrt{s} = 13$ TeV. Only one Wilson coefficient is fitted at a time while all others are set to zero. The observed best fit value and $p$-value for agreement with the SM is provided. The last column indicates whether the limits come from production (prod), decay or a combination of production and decay (comb). All couplings scale as $1/\Lambda^2$ with the assumed value of $\Lambda = 1$ TeV.
but since the quadratic terms contribute to the shapes in a symmetric way, they can still influence the measurements. Their impact on the results is tested for $c_{H\tilde{B}}$ decay-only and $c_{H\tilde{W}}$ production and decay by repeating the analysis when including only linear terms in the morphing method. For the two couplings investigated, the 68% C.L. (95% C.L.) limits with linear-only terms change by $\sim 1\%$ ($\sim 3\%$), indicating a negligible impact of the quadratic terms on the exclusion limits.

The effect of the choice to perform a shape-only analysis instead of additionally constraining the BSM couplings using the total cross-section predicted for each coupling value is also investigated using simulation. The measurement is repeated on simulated data, with the predicted signal event yield parametrised as a function of the coupling parameters instead of being left a free parameter. This parameterisation takes into account the effect of the BSM couplings on the production cross-section (for VBF), the decay branching fraction through the modification of the Higgs boson partial and total decay widths resulting from the quadratic EFT terms, and the detector event acceptance. For example, the predicted yield decreases by less than 10% relative to the SM yield for $c_{H\tilde{W}}$ at its 95% C.L. limit value of table 5 from the combination of the three effects. The cross-section change caused by the BSM couplings has a small effect on the decay-only limits as the predicted 68% (95%) C.L. exclusion limits would improve by less than 5% (10%). There would be an important effect for production-only measurements with the expected limits tightening by 10% (50%). The cross-sections are CP-even quantities and are only affected by the quadratic term, as the linear term integrates to zero over the optimal-observable distribution. Therefore the larger coupling values compatible with the data shape in the production scans result in a more pronounced effect on the limits from the quadratic term driving the rate change.

Finally, the present analysis assumes the presence of no other active CP-even BSM couplings in its signal model. The effects of a potential CP-even BSM admixture are evaluated in simulation by injecting simulated signals with additional active $c_{HB}$, $c_{HWB}$ and $c_{HW}$ SMEFT couplings on the order of the current experimental limits [104]. The effect on the production-only limits is negligible. For the decay analysis, a CP-even coupling of the magnitude investigated would weaken the limits and increase an observed non-zero CP-odd value by a few percent.

Figure 12 provides a comparison of the present measurements with those from [15, 27, 38]. The 68% confidence levels are compared for the Warsaw-basis couplings ($c_{H\tilde{B}}$, $c_{H\tilde{W}}$, and $c_{H\tilde{W}}$) and the $\tilde{d}$ coupling. The $H \rightarrow ZZ^* \rightarrow 4\ell$ simplified-template-cross-section (STXS) measurements [27] provide two degenerate positive/negative values as the measured cross-sections are only sensitive to the BSM quadratic terms ($|M_{BSM}|^2$ of eq. (2.2)). The STXS measurements are based on event rates in CP-insensitive categories and so cannot distinguish between a CP-even and CP-odd effect. This also explains the higher expected sensitivity of the present measurement that includes the four-lepton decays. The expected values for the present measurement are the most sensitive, except for $c_{H\tilde{W}}$ of the VBF $H \rightarrow \gamma\gamma$ decay channel measurement [38] that has a larger number of VBF produced events. For $\tilde{d}$, the improved sensitivity of the present measurement over the ATLAS $H \rightarrow \gamma\gamma + H \rightarrow \tau\tau$ measurement arises from the contribution of the $H \rightarrow ZZ^* \rightarrow 4\ell$ decays.

Two CMS measurements, $H \rightarrow ZZ^* \rightarrow 4\ell$ [18] and $H \rightarrow \tau\tau$ [22], provide results for CP-odd couplings with a similar approach as the present analysis. The CMS results, however,
Figure 12. Comparison of results for the present measurement, the ATLAS $H \to ZZ^* \to 4l$ STXS cross-section measurement of ref. [27], the ATLAS $H \to \gamma\gamma$ VBF measurement [38] of $c_{HHW}$, and the combined ATLAS VBF measurement of $\tilde{d}$ in $H \to \gamma\gamma$ and $H \to \tau\tau$ decay channels [15, 38]. The data points and 68% C.L. uncertainty bars show the observed values with statistical and systematic uncertainties. The $\tilde{d}$ best fit points and uncertainty bars are scaled by a factor of ten.

are not directly comparable to the present Warsaw basis results due to different assumptions applied on the CP-odd couplings. The assumptions of [18] and [22] are compatible with those of the present $\tilde{c}_{zz}$ measurement, however results in terms of the $\tilde{c}_{zz}$ coupling are not provided in [22].

In conclusion, the results of the coupling measurement are all in agreement with the SM. A fluctuation in the optimal observables leads to a slight preference for a non-zero BSM coupling in the production-level analysis, which is compatible with the SM at better than two standard deviations and not confirmed by the decay-level analysis.

8.2 Differential optimal-observable cross-section results

The differential cross-sections for the optimal observables are measured using a binned profile likelihood ratio fit, fitting simultaneously the $m_{4l}$ distribution in each bin across all bins of a given distribution, as described in section 6.2.

The measured differential cross-section for the production optimal observable $OO_{jj}^{C_{HHW}}$ and those for the decay optimal observables $OO_{4l}^{C_{HHW}}, OO_{4l}^{C_{H\tilde{u}\tilde{u}}}$ and $OO_{4l}^{C_{H\tilde{W}B}}$ are shown in figure 13. The couplings used for these optimal observables correspond to those with good expected sensitivity for VBF production or four-lepton decay of the direct coupling measurement, as previously described. The first bin of figure 13(a) is not part of the $OO_{jj}^{C_{HHW}}$ differential distribution but rather contains events with fewer than two selected jets with $p_T > 30$ GeV. These events are included as part of the fiducial distribution unfolding as they have a
correlation of up to 15% with the cross-section measurements of the $O \tilde{c}_4^H \tilde{w}_-^4$ differential bins as can be seen in figure 15(a) of appendix B. This correlation arises from the jet energy resolution. The larger number of decay events and the relatively better resolution for leptons allows a finer binning for the decay observable differential distributions. The correlation between neighboring bins is up to 30% for $O \tilde{c}_4^H \tilde{w}_-^4$ with 12 bins, and up to 20% for the six bin distributions of $O \tilde{c}_4^H \tilde{b}_-^4$ and $O \tilde{d}_4^H \tilde{w}_-^4$, as shown in appendix B.

These figures show the measured differential cross-section compared with SM predictions for ggF production provided by NNLOPS and MadGraph5_aMC@NLO_FxFx (MG5 FxFx), which are both normalized to the N3LO calculation \cite{105, 106}. The other Higgs boson production modes, denoted by $XH$, are normalized to the most accurate predictions available, as given in \cite{36}. All of the figures include the p-values that quantify the probability of compatibility of the measurements and the corresponding SM prediction for ggF + $XH$, including the theoretical uncertainties in the ggF predictions. For the p-value estimations, QCD scale and PDF uncertainties for NNLOPS are evaluated individually for each bin; however for MG5 FxFx only total QCD scale and PDF uncertainties are available for all bins. In both cases the theoretical uncertainties are treated as correlated across the bins. All p-values reveal a good compatibility of the data with the SM predictions. For $O \tilde{c}_4^H \tilde{w}_-^4$ in figure 13(b), the lower p-value is from a large fluctuation in one differential bin.

### 8.3 VBF-enriched fiducial cross-section results

As described in section 6.2, the VBF-enriched fiducial cross-section measurement is performed by dividing the two-dimensional plane $m_{jj}$ versus $|\Delta \eta_{jj}|$ into three bins with a signal region defined by $m_{jj} \geq 400$ GeV and $|\Delta \eta_{jj}| \geq 3.0$, and two control regions outside this selection. The expected and observed events in this two-dimensional plane can be seen in figure 14. Events are unfolded to the corresponding fiducial phase space and two VBF-enriched fiducial cross-sections are extracted: with the ggF expectation treated as part of the signal region and with it considered as background at the detector-level. The results for these two measurements are presented in table 6.

For both cases, the measured fiducial cross-section is larger than the expected, with a signal strength of about 1.6 and 2, but remain compatible with the SM as evaluated from p-values. In the first scenario the p-value compatibility with NNLOPS and MG5 FxFx is 82% and 80%, respectively. In the second scenario, where the ggF is treated as background, the p-value compatibility with the SM predictions for the remaining three production modes is 19%.

<table>
<thead>
<tr>
<th>VBF-enriched region</th>
<th>Signal for cross-section estimates</th>
<th>Purity of Expected Observed cross-section [fb] cross-section [fb]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{jets} \geq 2$, $m_{jj} \geq 400$ GeV</td>
<td>All production modes</td>
<td>59%</td>
</tr>
<tr>
<td>$</td>
<td>\Delta \eta_{jj}</td>
<td>\geq 3.0$</td>
</tr>
</tbody>
</table>

Table 6. Expected and observed VBF fiducial cross-sections measured in a VBF-enriched fiducial region with and without including the ggF contribution as part of the signal region.
Figure 13. Results for differential fiducial cross-section for the optimal observables (a) $OO_{\tilde{W}W}$, (b) $OO_{4\ell}$, (c) $OO_{4l}$ and (d) $OO_{4\ell}$. The first bin of $OO_{4\ell}$ distribution contains events with fewer than two jets that satisfy the jet selection requirements. The error bars on the data points show the total uncertainties, while the systematic uncertainties are indicated by the boxes. The shaded bands on the expected differential cross-sections indicate the PDF and scale systematic uncertainties. The central panel shows the ratio of different predictions to the data, and the grey area represents the total uncertainty in the measurement. The bottom panel shows the ratios of the fitted values of the $ZZ^*$ normalization factors to the predictions from MC simulation. As indicated by the horizontal error bars, the same $ZZ^*$ normalizations are estimated for different cross-section bins of the distributions.
Figure 14. The expected and observed events in the $m_{jj}$ vs. $|\Delta\eta_{jj}|$ two-dimensional plane for the VBF-enriched fiducial cross-section. The dots depict data and the shaded areas represent the simulated signal for VBF, ggF, and other backgrounds, respectively. The lines depict the bin boundaries for unfolding into the corresponding fiducial phase space.

These measured fiducial cross-sections can be compared with the VBF production cross-section of $H \to ZZ^* \to 4\ell$ decay channel measured in the context of the STXS framework [27]. The STXS measurement has a relative observed cross-section times branching ratio $(\sigma \cdot B)/(\sigma \cdot B)_{SM}$ of $1.21 \pm 0.45$ for the VBF production mode. The STXS measurement extracts the VBF signal using neural networks, similar to the direct measurement above, and combines VBF signals from several kinematic bins separated according to the number of jets and $p_T^{\ell\ell}$. The present fiducial analysis instead applies explicit selections on $m_{jj}$ and $|\Delta\eta_{jj}|$ for events with two jets, which selects events in a different phase space. All three measurements yield cross-sections that are compatible with the SM expectations.

9 Conclusion

A measurement searching for CP violation in VBF Higgs boson production and its decay into four leptons is presented based on proton-proton collision data produced at the LHC at a centre-of-mass energy of 13 TeV and recorded by the ATLAS detector from 2015 to 2018, corresponding to an integrated luminosity of 139 fb$^{-1}$. The measurement is performed using optimal observables defined as the ratio of the interference term between the SM and CP-odd BSM matrix elements to the SM matrix element squared. Limits are obtained in
both the Higgs and Warsaw bases using the SMEFT. They are dominated by the interference term between the SM and BSM contributions linear in the Wilson coefficients, \( \mathcal{O}(\Lambda^{-2}) \) in the cross-section, with only a small sensitivity to the pure BSM contributions quadratic in the Wilson coefficients, \( \mathcal{O}(\Lambda^{-4}) \). This qualitatively implies a low expected sensitivity to missing dimension-eight contributions that also enter at \( \mathcal{O}(\Lambda^{-4}) \) in the cross-section, and it is therefore an improvement on analyses relying on rates rather than shapes. Measurements of fiducial differential cross-sections of the optimal-observable distributions are also presented, completing the set of fiducial differential cross-section measurements in the Higgs boson to four-lepton channel. In addition, fiducial cross-sections for VBF production are measured for a VBF-enriched fiducial region for two scenarios: with and without the explicit subtraction of the ggF background. All measurements are consistent with the SM expectation of a CP-even Higgs boson. No significant CP-odd component is observed.

The data for all tables and the figures with differential distributions can be viewed at HEPData.

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A Conversion between Warsaw and Higgs bases

The CP-odd operators studied in the present analysis are given in table 1. The couplings of the two bases

- Warsaw basis: $c_{H\tilde{W}}, c_{H\tilde{B}}, c_{H\tilde{W}B}$
- Higgs basis: $\tilde{c}_{zz}, \tilde{c}_{z\gamma}, \tilde{c}_{\gamma\gamma}$

can be expressed as linear combination of each other:

$$\tilde{c}_{zz} = 4 \left( g^2 c_{H\tilde{W}} + g'^2 c_{H\tilde{B}} + gg' c_{H\tilde{W}B} \right) \frac{v^2}{\Lambda^2}$$  \hspace{1cm} (A.1)

$$\tilde{c}_{z\gamma} = 4 \left( \frac{c_{H\tilde{W}} - c_{H\tilde{B}} - g^2 - g'^2}{g^2 + g'^2} c_{H\tilde{W}B} \right) \frac{v^2}{\Lambda^2}$$  \hspace{1cm} (A.2)

$$\tilde{c}_{\gamma\gamma} = 4 \left( \frac{1}{g^2} c_{H\tilde{W}} + \frac{1}{g'^2} c_{H\tilde{B}} - \frac{1}{gg'} c_{H\tilde{W}B} \right) \frac{v^2}{\Lambda^2}$$  \hspace{1cm} (A.3)

and

$$\frac{v^2}{\Lambda^2} c_{H\tilde{W}} = \frac{g^2}{4(g^2 + g'^2)^2} \left( (g^2 + g'^2)^2 \tilde{c}_{zz} + 2(g^2 + g'^2)g^2 \tilde{c}_{z\gamma} + g'^4 \tilde{c}_{\gamma\gamma} \right)$$  \hspace{1cm} (A.4)

$$\frac{v^2}{\Lambda^2} c_{H\tilde{B}} = \frac{g'^2}{4(g^2 + g'^2)^2} \left( (g^2 + g'^2)^2 \tilde{c}_{zz} - 2(g^2 + g'^2)g^2 \tilde{c}_{z\gamma} + g'^4 \tilde{c}_{\gamma\gamma} \right)$$  \hspace{1cm} (A.5)

$$\frac{v^2}{\Lambda^2} c_{H\tilde{W}B} = \frac{gg'}{2(g^2 + g'^2)^2} \left( (g^2 + g'^2)^2 \tilde{c}_{zz} - (g^4 - g'^4) \tilde{c}_{z\gamma} - g^2 g'^2 \tilde{c}_{\gamma\gamma} \right)$$  \hspace{1cm} (A.6)

where $g$ and $g'$ are the gauge couplings of the SU(2) and SU(1) local symmetries, respectively, $v$ is the Higgs boson vacuum expectation value and $\Lambda$ is the energy cutoff scale of the effective field theory.

B Additional differential cross-section results

This appendix shows additional results of the differential fiducial cross-section measurements presented in section 8.2.

Figure 15 shows the correlation matrices for the differential fiducial cross-sections presented in figure 13. Non-negligible anti-correlations exist between the cross-sections in neighbouring bins due to detector resolution effects. In addition, there are anti-correlations between the cross-section for $N_{jets} < 2$ and the four optimal observable bins in the $O\tilde{O}^{\tilde{W}}$ measurement shown in figure 15(a), driven by jet energy resolution. Finally, the normalization
The bin labeled $\sigma_0$ of (a) is not part of the $OO_{jj}^{\tilde{t} \tilde{w}}$ differential distribution, but contains events with fewer than two selected jets with $p_T > 30\text{ GeV}$.

of the $q\bar{q} \to ZZ^*$ background is anti-correlated with the signal cross-sections measured in the respective bins.

Figure 16 shows the differential fiducial cross-section for the $OO_{jj}^{\tilde{t} \tilde{w}}$ observable and the associated correlation matrix. This observable is strongly correlated with $OO_{jj}^{\tilde{t} \tilde{t} W}$ and the two measurements thus share many features.

Figure 17(a) shows the per-bin fiducial cross-section values and the correlation matrix for the extraction of the VBF-enriched fiducial cross-section described in section 8.3.
**Figure 16.** (a) Results for the differential fiducial cross-section for the $O_{jj}^{\tilde{c}\tilde{c}}$ optimal observable, along with (b) the corresponding correlation matrix between the measured cross-sections and the $ZZ^*$ background normalization factors. The first bin of (a) is not part of the $O_{jj}^{\tilde{c}\tilde{c}}$ differential distribution, but contains events with fewer than two selected jets with $p_T > 30$ GeV. This bin corresponds to $\sigma_0$ of (b).

**Figure 17.** (a) Results for the VBF-enriched fiducial cross-section measurement extracted from the double-differential fiducial cross-section for $m_{jj}$ versus $|\Delta\eta_{jj}|$, along with (b) the corresponding correlation matrix between the measured cross-sections and the $ZZ^*$ background normalization factors.
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