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1 A dual-process approach to exploring the role of delay discounting in obesity

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8 Running title: Dual-parameter model for obesity related delay discounting

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20 Abstract

21 Delay discounting of financial rewards has been related to overeating and obesity.  
22 Neuropsychological evidence supports a dual-system account of both discounting and  
23 overeating behaviour where the degree of impulsive decision making is determined by the  
24 relative strength of reward desire and executive control. A dual-parameter model of  
25 discounting behaviour is consistent with this theory.

26 In this study, the fit of the commonly used one-parameter model was compared to a new  
27 dual-parameter model for the first time in a sample of adults with wide ranging BMI. Delay  
28 discounting data from 79 males and females (Males=26) across a wide age (M=28.44 years  
29 (SD=8.81)) and BMI range (M=25.42 (SD=5.16)) was analysed. A dual-parameter model  
30 (saturating-hyperbolic; Doya, 2008) was applied to the data and compared on model fit  
31 indices to the single-parameter model.

32 Discounting was significantly greater in the overweight/obese participants using both models,  
33 however, the two parameter model showed a superior fit to data ( $p<.0001$ ). The two  
34 parameters were shown to be related yet distinct measures consistent with a dual-system  
35 account of inter-temporal choice behaviour.

36 The dual-parameter model showed superior fit to data and the two parameters were shown to  
37 be related yet distinct indices sensitive to differences between weight groups. Findings are  
38 discussed in terms of the impulsive reward and executive control systems that contribute to  
39 unhealthy food choice and within the context of obesity related research.

40 Keywords: Obesity, delay discounting, dual-process, two-parameter, model

41

42 1. Introduction

43 The ability to delay gratification may be crucial for exerting self-control in a tempting food  
44 environment. The conflict between the delayed rewards of good health and weight  
45 maintenance versus the immediate reward of tasty foods is a dilemma well captured by the  
46 delay discounting task [1]. Typically, participants are presented with a choice between a  
47 small reward available immediately, or a larger reward available after a delay. Several trials  
48 are presented over a number of delay periods and an indifference point (IP) is calculated as  
49 the value at which the participant is indifferent to the reward being received now or after a  
50 delay. The lower the IP values, the less an individual is willing to wait for the reward,  
51 indicating a reduced ability to delay gratification. Discounting of the future on both money  
52 and food-based tasks has been related to over eating and obesity, albeit inconsistently [2-15].  
53 A commonly used model of discounting outcomes in obesity research is the single parameter  
54 (*k*) hyperbolic model [16] which is fitted to data using the formula:

$$V = \frac{A}{1 + kD}$$

55 Where: V is the Indifference Point (IP), A is the Larger Later Reward (LLR), D is the delay  
56 (days) and *k* is the free parameter for estimating steepness of temporal discounting.

57 As delays increase the IPs typically decrease as respondents are willing to accept less money  
58 immediately instead of waiting for the delayed reward. This decline is however time-  
59 inconsistent, being steeper when the delays are proximal (one day versus one week) and  
60 shallower when delays are more distal (six months versus nine months). This enhanced  
61 sensitivity to differences between shorter compared to longer delays may be reflecting a  
62 reduced ability to imagine distal time periods with the same clarity as the near future. For  
63 example, the greater the temporal distance to the time period being imagined, the less detail

64 or ‘pre-experiencing’ of that event that is reported [17]. The ability to imagine the future  
65 varies between individuals and is considered to be an important component of executive  
66 functioning related to activity in the prefrontal cortex [18].

67 Most reports of delay discounting applied to obesity have cited Mazur’s original paper to  
68 justify using the single parameter hyperbolic model [16], in which the model provided the  
69 best fit to data. However, Mazur examined discounting behaviour in rats, over very short  
70 delays (usually seconds or minutes), and the question arises of whether it is a suitable model  
71 for describing human discounting behaviour over longer delay periods.

72 A number of psychological theories support a dual-process account of the ability to inhibit  
73 impulsive responses in favour of long-term gain [19]. Koffarnus and colleagues [20]  
74 reviewed delay discounting research in different impulsive populations, exploring the  
75 plausibility of a ‘Competing Neurobehavioural Decision Systems’ (CNDS) explanation of  
76 inter-temporal choice. The authors suggest that behaviours related to a reduced ability to  
77 delay rewards (including drug use, gambling and over eating) may be the result of a common  
78 underlying trait predisposing a person to choose immediate rewards over long term benefits.  
79 They discuss evidence favouring a role for two neural systems in trans-disease choice  
80 behaviour: an executive decision system correlating with lateral pre-frontal cortex (PFC)  
81 activation; and an impulsive system correlating with limbic reward activity. The CNDS  
82 model predicts that individual differences in one or both of these systems, determines choice  
83 behaviour. For example, it has been reported that that obese women gained more weight over  
84 the subsequent year if they showed reduced activation in brain areas associated with  
85 executive function when completing difficult discounting trials, compared to easy trials [21].  
86 This supports the idea that sub-optimal functioning of executive areas leads to reduced self-  
87 control and overeating behaviour. However, it has been found that a ‘dual-hit’ of reduced  
88 executive control *and* increased desire for food cues reflected in nucleus accumbens (NAcc)

89 reactivity, determined a vulnerability to over eating and higher BMI [22]. Hence, outcome  
90 behaviour in the delay discounting task may relate to activity in the reward system *and* the  
91 executive system. In support of this idea, Lopez et al [23] reported that NAcc activity in  
92 response to food cues predicted subsequent food desire and consumption over a week long  
93 period, but this was moderated by inferior frontal gyrus activity in a self-control task. Reward  
94 sensitive individuals displaying greater activity in this frontal region at baseline were more  
95 able to resist strong food temptations than those who showed lower activity. This evidence  
96 supports a dual-process approach to overeating and obesity [24]. Consistent with this,  
97 neuroscientific evidence indicates that discounting is sensitive to two separate considerations  
98 – time delay and reward magnitude, corresponding to PFC and Ventral Striatum (in particular  
99 NAcc) activity respectively [25-27]. Thus the one parameter hyperbolic model may not be as  
100 appropriate as a dual-parameter model, which is more in line with obesity related empirical  
101 research evidence and neuropsychological theory.

102 In behavioural economics and addiction research, two-parameter models have been applied to  
103 discounting data and compared favourably to single parameter models [28-30]. For example,  
104 McKercher and colleagues [28] showed that in a general undergraduate student sample, two  
105 hyperboloid models fitted with an additional power function showed superior fit to  
106 discounting data compared to one parameter exponential and hyperbolic models. However, as  
107 both two-parameter models showed equally good fit to data, the authors advise that model  
108 selection should be based on theoretical, rather than just empirical reasons in any given  
109 population. A two-parameter model which has two parameters that distinguish between  
110 immediately available and delayed rewards is the  $\beta\delta$  model [31]. However, Kable and  
111 Glimcher [32] have suggested that it is more likely that there is a single system underpinning  
112 desire for reward as soon as possible rather than a separate system for immediate versus  
113 delayed reward.

114 Therefore a novel two-parameter model that is consistent with evidence and theory is put  
115 forward. The saturating-hyperbolic model [33] is based on the premise that everyday decision  
116 making is difficult because decisions can result in rewards of different amounts at different  
117 timings. Within a delay discounting paradigm, the choice outcome behaviour is therefore  
118 dependent upon both temporal discounting and reward utility. This model has two free  
119 outcome parameters,  $k$  and  $Q$ , proposed to represent these processes respectively and is  
120 calculated using the equation:

$$V = A * \left( \frac{A}{A + Q} \right) * \left( \frac{1}{1 + kd} \right)$$

121 Where:  $V$  = Indifference Point (IP);  $A$  = Larger later reward;  $k$  = hyperbolic temporal  
122 discounting parameter;  $d$  = delay (days);  $Q$  = reward utility parameter.

123 The  $k$  parameter reflects the extent to which an individual discounts rewards over time. This  
124 is identical to the single parameter hyperbolic function  $k$  and represents the relative steepness  
125 of discounting at proximal versus distal delays. It is theorised to represent the ability to  
126 imagine the future which relies on activity in executive decision systems [18]. The  $Q$   
127 parameter is called the reward utility function. This is typically a nonlinear function with a  
128 sigmoid shape with a threshold and saturation point [33, 34]. It is hypothesised to represent  
129 impulsive needs and desires, with variation in  $Q$  values indicating variation in nonlinear  
130 valuation [33]. A larger  $Q$  value indicates a shallow reward utility curve and signals that the  
131 reward is less appealing, whereas a smaller  $Q$  value indicates a steep reward curve and  
132 signals that the reward is more appealing. When combined with the hyperbolic function  $k$ , the  
133  $Q$  parameter reflects the overall utility of the reward after a delay. If the reward is desired as  
134 soon as possible then the  $Q$  value will be large, indicating that any delay very rapidly  
135 devalues the reward. Therefore, the curve becomes saturated by enhanced proximal reward  
136 utility and the value of  $Q$  describes the extent of this saturation. In descriptive terms this is

137 seen as a 'flattening' of the discounting curve where there is an immediate drop in where the  
138 curve starts on the y-axis. The larger the Q value, the larger the 'drop' and therefore the  
139 greater the emphasis on receiving the reward immediately.

140 To sum up, Q is theorised as a related yet distinct process to  $k$ , where the  $k$  parameter is a  
141 measure of 'temporal discounting' and is theorised to represent the ability to imagine the  
142 future and the Q parameter is a measure of reward utility, theorised to represent the impulsive  
143 need and desire for reward. When combined into a single model, the Q value represents the  
144 utility of the rewards as a function of delay, with higher values representing an emphasis on  
145 receiving that reward as soon as possible. Therefore, Q affects the overall valuation of the  
146 delayed reward being examined, contrasting with the single parameter model which only  
147 considers the steepness of discounting across indifference points. The saturating-hyperbolic  
148 model was selected because 1) it is directly comparable with the commonly used (nested)  
149 one parameter hyperbolic model, and 2) it is consistent with dual-process theories and  
150 neuropsychological evidence emphasising the importance of separate executive and reward  
151 functions in determining delay discounting in obesity research [21-23].

152 Although there have been numerous studies of delay discounting in obesity research, the  
153 relative fit of a dual-parameter model in an adult sample with wide ranging BMI is yet to be  
154 tested. The aim of the current study was to apply the commonly used one-parameter  
155 hyperbolic and the theory consistent, two-parameter saturating-hyperbolic model to  
156 discounting data from a sample of males and females with a wide BMI and age range. We  
157 predicted that the two-parameter model would show superior fit to data, and that Q and  $k$   
158 would be related but independent constructs. In addition, the parameters were compared  
159 across weight groups to assess if they were sensitive to differences in discounting behaviour  
160 between lean and overweight/obese participants. We also included self-report measures of  
161 hedonic response to palatable food (Power of Food Scale [35]), disinhibited and restrained



162 eating (Dutch Eating Behaviour Questionnaire [36]), and perceived control over food intake  
163 (Yale Food Addiction Scale [37]) to describe the population in terms of eating behaviour  
164 dimensions.

## 165 2. Method

### 166 2.1 Participants:

167 One hundred and one participants were recruited from the student and staff population at  
168 Swansea University and from professional/administration staff working for the local authority  
169 via email and poster advertisement. A pre-screening questionnaire was administered to ensure  
170 an equal distribution of lean and overweight/obese participants. Delay discounting and self-  
171 report data were collected from each participant. After applying Johnson and Bickel's [38]  
172 algorithm for identifying non-systematic delay discounting responders, and the removal of  
173 one outlier (with an area under the curve greater than 2.5 standard deviations from the mean),  
174 data from seventy nine participants was included for analysis (for sample characteristics, see  
175 Table 1).

176 Written consent was obtained from all participants and consent and all study procedures were  
177 granted departmental ethical approval by the Swansea University, Department of Psychology  
178 Research Ethics Committee.

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184 Table 1: Sample characteristics for the Lean and Overweight/obese groups.

Demographic Characteristics	Lean (BMI 18-24.9): Mean (Range (SD))	Overweight/Obese (BMI 25+): Mean (Range (SD))
N	41	38
Age (years)	26.76 (19-46(7.9))	30.11 (18-51(9.5))
Males (N)	9	16
Females (N)	32	22
BMI	21.6 (18.3-24.8(1.9))	29.6 (25.4-43.6(4.4))
PFS	2.86 (1.3-4.3(.9))	2.54 (1.3-4(.8))
YFAS	1.49 (0-4(1.1))	1.89(0-6(1.5))
DEBQext	3.25 (1.8-4.4(.66))	2.93 (1.7-3.9(.56))
DEBQem	2.65 (1-4.2(.76))	2.35 (1-4.8(.89))
DEBQrest	1.51 (1-2(.51))	1.5(1-2(.51))

185 BMI (Body Mass Index); PFS (Power of Food Scale); YFAS (Yale Food Addiction Scale);  
 186 DEBQ (Dutch Eating Behaviour Questionnaire) ext (External eating), em (Emotional eating),  
 187 rest (Restrained eating).

188

189

190 2.1 Procedure:

191 Participants were invited to attend a study ostensibly investigating ‘mood and decision  
 192 making’. Each participant completed the delay discounting task, followed by the Power of  
 193 Food Scale [35], Dutch Eating Behaviour Questionnaire [36] and Yale Food addiction Scale  
 194 [37]. Height and weight was recorded by the researcher using the SECA laboratory scales in  
 195 order to calculate body mass index (BMI) using the standard formula ( $\text{kg/m}^2$ ). Participants  
 196 were then debriefed, thanked and assigned course credit if they were students or £5 if they  
 197 were members of the community.

198 2.2 Measures

199 2.2.1 Delay discounting task: A computer-based monetary delay discounting task with nine  
 200 delays ranging from one day to one year. The larger, later amount was constant at £100 and  
 201 the smaller, sooner amount varied using a random adjusting procedure, until the indifference  
 202 point (IP) was calculated (the point at which the participant became indifferent to receiving  
 203 the reward now or later). The IP for each delay was plotted as an indicator of the subjective

204 value of that reward at the given delay. The lower the value, the less willing a participant is to  
205 wait for the reward. The plotted IPs can then be used to calculate a given outcome measure  
206 for discounting behaviour. A detailed description of the task can be found in McHugh and  
207 Wood's original paper [1].

208 2.2.2 Power of food scale (PFS): The PFS (Short version) is a 15 item questionnaire  
209 measuring participants' appetite at three levels: when food is available, present and tasted.  
210 The scale has been shown to predict food craving [39] and intake [40] in previous studies and  
211 is included here as a general measure of appetite for palatable foods readily available in the  
212 environment. Cronbach's alpha for the original scale was reported as 0.91 [35]. For group  
213 means see Table 1.

214 2.2.3 Dutch Eating Behaviour Questionnaire (DEBQ): The DEBQ is a commonly used self-  
215 report measure with three sub-scales. The external eating and emotional eating sub-scales  
216 measure readiness to eat in response to external and emotional cues (disinhibited eating) and  
217 the dietary restraint sub-scale measures the extent to which a person restricts their food intake  
218 in order maintain/lose weight. The scale is commonly used and was included to allow cross-  
219 comparison of sample characteristics with related research. Cronbach's alpha for the original  
220 scales were reported as between 0.8-0.95 [36]. For group means see Table 1.

221 2.2.4 Yale Food Addiction Scale (YFAS): The YFAS is a 25 item self-report measure of  
222 'food addiction'. It attempts to identify those who have truly lost control over their eating  
223 behaviour. Participants receive a continuous score relative to the number of addiction criteria  
224 that have been met (for example, use continues despite knowledge of adverse consequences)  
225 with a maximum score of seven. The scale was included here as recent research has shown it  
226 to be a direct predictor of BMI [41], and a mediator between general impulsivity and BMI

227 [42]. Good internal reliability for the original scale was reported as Kuber-Richardson  
228  $\alpha=0.86$  [37]. For group means see Table 1.

### 229 3. Analysis:

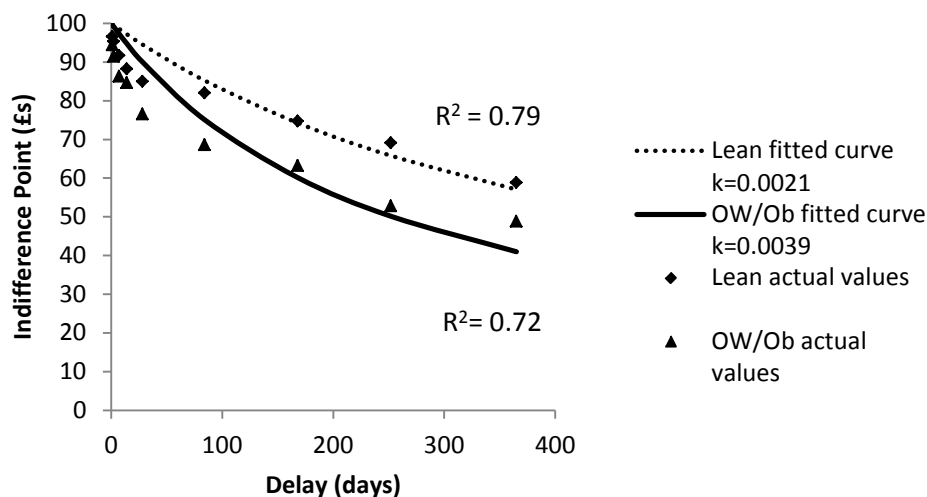
230 The one-parameter hyperbolic model was applied to the data using a least squares procedure  
231 on Gnuplot open source software [43], to estimate a  $k$  value for each participant. The  
232 saturating-hyperbolic model was applied to the delay discounting data using both Excel  
233 solver and Gnuplot software. Both fit the two parameters simultaneously and produced  
234 identical values. As a result the  $Q$  and  $k$  values were considered to be reliable.

235 The  $R^2$  value for both models was calculated for descriptive purposes. Although often  
236 reported, the use of  $R^2$  as a unit of comparison is more appropriate for linear regression  
237 models and has been argued to have little meaning for non-linear models [38]. As a result, the  
238 Sum of Squared Residuals (SSR) for both models were calculated and used for comparison  
239 analysis. The SSR is equivalent to a chi-square ( $\chi^2$ ) measure of model fit, and reflects the  
240 total deviation of the response values from the fit to the response values. As with  $\chi^2$ , goodness  
241 of fit is indicated by lower values reflecting a smaller random error component. Given that a  
242 two-parameter model will always be expected to have a superior fit to a single parameter  
243 model, a comparison method accounting for this difference is necessary. The two indices that  
244 account for the number of parameters in each model and employed here were: Reduced SSR  
245 (RSSR) and Root Mean Square (RMS) of RSSR. RSSR is calculated by dividing the SSR by  
246 the number of degrees of freedom in the model, and the RMS (RSSR) is simply the square  
247 root of this. The degrees of freedom were calculated by subtracting the number of parameters  
248 from the number of data points (in this case there were nine data points, one for each delay  
249 period). In each case lower values indicate a better fit. A significantly better fit can be  
250 determined using a  $\chi^2$  difference test, as the models are nested.

251 Bivariate correlations were used to test if the parameters represented related or distinct  
252 processes. All analyses were conducted using IBM SPSS 20.0 software. All effect sizes were  
253 calculated post hoc using G\* Power3 software [44].

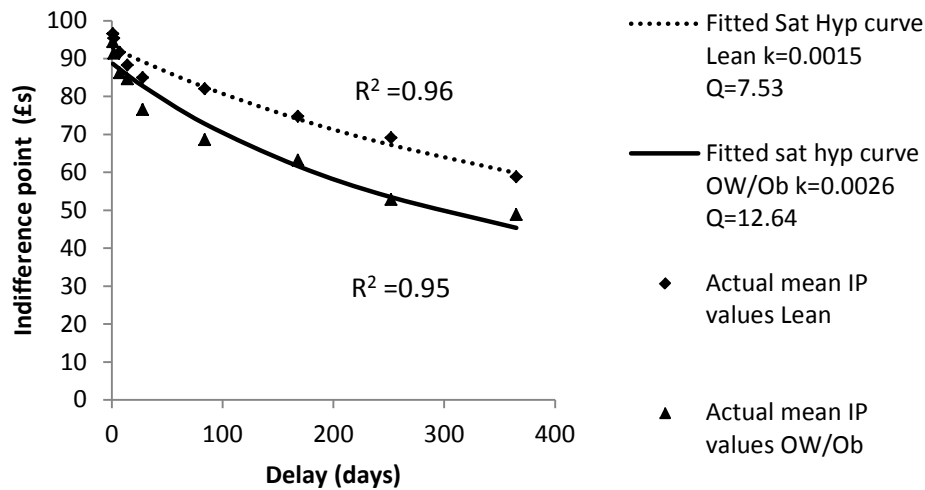
254 4. Results:

255 The single parameter ( $k$ ), and two-parameter ( $Q$  and  $k$  ( $satk$ )) curves were fit to data from  
256 each participant and to the mean indifference points for the lean and overweight/obese groups  
257 for descriptive purposes (see Figures 1 & 2 respectively). The saturating-hyperbolic shows a  
258 visually superior fit to data (especially at the shorter delay periods) and has a markedly  
259 improved  $R^2$  value for both weight groups. However, for a valid comparison, the SSR, RSSR  
260 and RMS (RSSR) were calculated for both models for each participant. Table 2 shows the  
261 mean fit indices for each model, along with the  $\chi^2$  difference test results. The SSR, RSSR and  
262 RMS (RSSR) values are smaller for the saturating-hyperbolic model, and the difference test  
263 is significant, indicating a statistically superior fit to data.



264

265 Figure 1: Graph to show the  $k$  values and one-parameter hyperbolic curves fitted to mean  
266 indifference points for lean and overweight/obese (Ow/Ob) participants (N=79).



267

268 Figure 2: Graph to show the Q and satk values and saturating-hyperbolic curves fitted to the  
 269 mean indifference points for lean and overweight/obese (OW/Ob) participants (N=79).

270 Table 2: Mean (SD) values, for goodness of fit indices for the one-parameter hyperbolic  
 271 model and the saturating-hyperbolic model.

Model/ Fit index	One parameter hyperbolic	Saturating- hyperbolic	X <sup>2</sup> Difference test (Df difference=1)
SSR	879.40 (1020.11)	528.24 (642.44)	351.16*
RSSR	109.93 (127.51)	75.46 (96.78)	
RMS (RSSR)	8.96 (5.48)	7.27 (4.77)	

272 SSR (Sum of Squared Residuals); RSSR (Reduced Sum of Square Residuals); RMS (RSSR)  
 273 (Root Mean Square (RSSR)); Df (degrees of freedom); \*p<0.0001. (p=0.35).

274 In order to explore the relationship between the two parameters Q and satk, from the  
 275 saturating-hyperbolic model, and the original k value from the one parameter model, they  
 276 were entered into a bivariate correlation matrix (see Table 3). Results confirm that the k  
 277 parameter in both models showed a near perfect correlation (r=.97). The Q parameter  
 278 however, shows only a moderate correlation (r=.22) and so it is likely to represent a related  
 279 yet distinct function.

280 Table 3: Spearmans correlation coefficients for the model parameters

	1	2	3
1. Q			
2. <i>satk</i>	0.22*		
3. <i>k</i>	0.41**	0.97**	

281 Q (Saturating-hyperbolic model); *satk* (Saturating-hyperbolic model); *k* (one-parameter  
 282 hyperbolic model) \* $p < 0.05$  \*\* $p < 0.01$

283 The *k*, Q and *satk* values were also compared across weight groups. The one parameter *k*  
 284 values were significantly positively skewed ( $z_{skewness} > 1.96$ ;  $p < .05$ ) and so analysis was  
 285 performed on log transformed data. ANOVA showed that the  $\log k$  values were significantly  
 286 higher for the overweight/obese group compared to the lean group ( $F(1,77) = 8.016$ ;  $p = .006$ ;  
 287  $f = 0.51$ ). Demographic variables age and gender were compared across weight groups and  
 288 although there were no significant differences ( $p > .05$ ) there was a trend for the  
 289 overweight/obese group to be older and include more males ( $p < .10$ ). Therefore, the  
 290 comparison was also run using ANCOVA, controlling for age and gender, however the  
 291 outcomes did not change significantly. The overweight/obese group still showed significantly  
 292 higher discounting rates than the lean group ( $F(1,75) = 7.09$ ;  $p = .009$ ).

293 As a result of the significantly skewed nature of the *satk* and Q values, and the fact that log  
 294 transformation did not correct this, non-parametric tests were applied to the data. The Mann-  
 295 Whitney U test of independent samples showed that the overweight/obese sample ( $N = 38$ ) had  
 296 significantly ( $t = 2.25$ ;  $p = .025$ ;  $d = 0.8$ ) higher *satk* values ( $M = 0.0042$ ;  $SD = 0.004$ ) than the lean  
 297 sample ( $N = 41$ ;  $M = 0.0032$ ;  $SD = 0.004$ ), as found with the original one parameter model. This  
 298 is interpreted as particularly robust as the populations do not represent top and bottom  
 299 quartiles, but a separation of those with a BMI below 25 and those with a BMI of 25 and  
 300 above. There was also a significant difference between the weight groups for Q values

301 (t=2.23; p=.026; d=0.8), where the overweight/obese group showed significantly greater Q  
302 values (M=12.8; SD=16.7) than the lean group (M=5.4; SD=6.1). For consistency, the raw *k*  
303 values from the single parameter model were also compared using the Mann-Whitney U test,  
304 and were once again significant (t=2.82, p=.005, d=.9), with the overweight/obese group  
305 displaying higher *k* values (M=.01; SD=.02) than the lean group (M=.005; SD=.01).

306

## 307 5. Discussion

308 Delay discounting has been related to obesity and has typically been modelled using a single  
309 hyperbolic parameter (*k*) representing the relative steepness of temporal discounting.

310 However, neuropsychological research supports a dual-process account of discounting  
311 behaviour. The saturating-hyperbolic model has two parameters, *satk* and *Q*, which are  
312 related but distinct indices proposed to represent temporal discounting and reward utility  
313 respectively. The model was therefore deemed consistent with the neuropsychological  
314 evidence and theory. The model was applied to discounting data from a sample with a wide  
315 range of BMIs and compared to the original single-parameter hyperbolic model. The new  
316 model showed a superior ‘goodness of fit’ to current discounting data and has therefore been  
317 shown to be a more accurate model of discounting behaviour in the current population.

318 The almost perfect correlation between the one parameter *k* value and the *satk* value indicates  
319 that both parameters are measuring the same process and are therefore directly comparable.

320 The more modest correlations between *k* and *Q* indicate that *Q* is measuring a related but  
321 distinct process to *k*. The parameters from both models were shown to be significantly higher  
322 in overweight/obese versus lean participants. This supports previous findings using the single  
323 parameter model, that delay discounting is an important component of obesity  
324 [3,4,6,7,8,10,11], but shows for the first time that the saturating-hyperbolic model is not only



325 a better fit to data but maintains sensitivity to these differences. It is therefore a valid model  
326 for future use in obesity research. Indeed, very recently, Franck and colleagues [45] published  
327 a paper indicating that different models of discounting may best describe different  
328 populations and provide a tool for allowing different models to be compared. The saturating-  
329 hyperbolic model was not included in Franck and colleagues' [45] paper and would make a  
330 useful addition if applied to obesity research.

331 The CNDS model of delay discounting maintains that poor choices like over eating are the  
332 result of a high impulsive reward system, low executive system functioning or a combination  
333 of both. In the current sample, the overweight/obese group had significantly higher  $satk$  and  
334  $Q$  parameter values on the discounting task and it is theorised that the parameters may  
335 represent functioning of the executive and impulsive reward systems respectively. This is  
336 consistent with findings that it is the 'dual hit' of (food) reward desire and poor executive  
337 control that leads to over eating [22]. The saturating-hyperbolic model proposes that the two  
338 parameters represent temporal discounting ( $satk$ ) and reward utility ( $Q$ ) which is consistent  
339 with neuropsychological research showing that delay discounting involves two related yet  
340 distinct processes [26]. The use of the saturating-hyperbolic model to measure these  
341 processes separately using the discounting task would be of great advantage in more precisely  
342 elucidating the factors that contribute to overeating. However, it would be informative to  
343 investigate the specific nature of the underlying processes by testing convergent validity of  
344  $satk$  and  $Q$  with neural responsivity in pre-frontal and reward areas and with measures of  
345 executive function and reward utility.

346 Carr et al. [50] coined the term 'reinforcement pathology' to describe the extent to which  
347 food is a reinforcer but also the degree of impulse control a person has. A strong motivation  
348 for food, measured using the Relative Reinforcement Value (RRV) of food task, has been  
349 shown to predict BMI and intake particularly in those who discount the future more steeply

350 [12, 51]. This suggests that food responsiveness is an important contributor to overeating in  
351 those with poor impulse control [49]. Research has also shown the discounting of food to be  
352 steeper in overweight/obese groups [13, 47] and so it would now be useful to apply the  
353 saturating-hyperbolic to food-related discounting behaviour. Findings from such research  
354 would allow us to begin to assess the relative influence of a general, trans-disease tendency to  
355 discount the future and a food specific tendency to discount the future in relation to  
356 overeating and obesity.

357 A few limitations are notable. Firstly, socio-economic indicators (income, IQ and education)  
358 were not recorded, but have previously been shown to be related to discounting behaviour [4,  
359 53]. However, the majority of participants were recruited from the university student and  
360 staff population or local authority professional employees. Significant socio-economic-status  
361 (SES) differences between the weight groups were deemed unlikely. Future studies would  
362 benefit from a valid measure of SES in this context and from extending the sample to include  
363 a wider SES range (especially given the association between SES and obesity). Secondly, the  
364 sample was quite small for cross-sectional research however the predicted effects for  $Q$  and  $k$   
365 emerged nonetheless, suggesting a robust finding. Future studies may benefit from a larger,  
366 more representative cohort. Lastly, the (sat)  $k$  parameter has been theorised to be  
367 representative of the ability to imagine the future and that this is an important aspect of  
368 executive control. But the fact that pigeons demonstrate hyperbolic discounting behaviour  
369 [57] and that dopaminergic activation of the reward circuitry also decreases in hyperbolic  
370 proportion to reward delay length in rhesus monkeys [59], suggests that other mechanisms  
371 may be responsible for discounting behaviour. However, human evidence showing that  
372 episodic future thinking (EFT) reduces  $k$  values [58], supports the idea that the ability to  
373 imagine the future might be one factor that underlies  $k$ , in humans at least.

374 As discounting is mutable under certain circumstances [54], it is a viable target for weight  
375 loss intervention research. Application of the two-parameter model could expand our  
376 understanding of exactly how an intervention exerts its influence. Recently, it was found that  
377 EFT reduces both discounting behaviour and food intake in lean and obese individuals [55,  
378 56], presumably through enhancing the valence of future time periods and making  
379 discounting of the future less likely. Application of the saturating-hyperbolic to such data  
380 would further inform us of whether EFT is enhancing executive consideration of the future  
381 (satk), reducing immediate reward utility (Q) or both? Application of this model in future  
382 research may enhance our understanding of which system underlies over eating in different  
383 individuals and contribute towards behavioural interventions that can be targeted effectively.

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